

User's Manual

# multiPlas

Release 4.1.8 for ANSYS 14.5

January 2013, Rev. 1

Elasto-plastic material models for ANSYS  
General multisurface plasticity

multiPlas

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## CONTENT

|        |   |    |
|--------|---|----|
| 1      | INTRODUCTION.....   | 5  |
| 2      | INSTALLATION INSTRUCTIONS .....   | 6  |
| 2.1    | How to start ANSYS Mechanical APDL with multiPlas .....   | 6  |
| 2.2    | How to use ANSYS Workbench with multiPlas.....  | 6  |
| 3      | THEORY OF THE MULTIPLAS MATERIAL MODELS IN ANSYS .....  | 7  |
| 3.1    | Basics of elasto-plasticity in multiPlas.....   | 7  |
| 3.2    | Multisurface plasticity .....   | 8  |
| 3.3    | Computed yield surfaces.....  | 9  |
| 3.3.1  | Introduction yield surfaces of basic material models .....  | 9  |
| 3.3.2  | MOHR-COULOMB isotropic yield criterion .....  | 10 |
| 3.3.3  | MOHR-COULOMB anisotropic yield criterion .....  | 12 |
| 3.3.4  | Yield criterion according to DRUCKER-PRAGER .....   | 14 |
| 3.3.5  | Combination of flow condition according to MOHR-COULOMB and DRUCKER-PRAGER or TRESCA and von MISES.....   | 15 |
| 3.3.6  | Concrete modelling using modified DRUCKER-PRAGER model.....   | 16 |
| 3.3.7  | Simulation of regular masonry using the Ganz yield condition .....  | 22 |
| 3.3.8  | Wood modelling using a boxed-value-model.....   | 25 |
| 3.4    | Dilatancy.....  | 28 |
| 4      | COMMANDS.....   | 29 |
| 4.1    | Material Models .....   | 29 |
| 4.2    | TBDATA-Declaration .....  | 30 |
| 4.2.1  | LAW = 1, 10 – Mohr Coulomb.....   | 30 |
| 4.2.2  | LAW = 2 – Modified Drucker-Prager .....   | 31 |
| 4.2.3  | LAW = 5 – Modified Drucker-Prager, temperature dependent .....  | 32 |
| 4.2.4  | LAW = 8 – Modified Drucker-Prager, calibrated stress dependent nonlinear hardening (Mortar / Cement)..... | 33 |
| 4.2.5  | LAW = 9 – Concrete .....  | 35 |
| 4.2.6  | LAW = 11 – Fixed Crack Model .....  | 37 |
| 4.2.7  | LAW = 20 – Masonry Linear Softening .....   | 38 |
| 4.2.8  | LAW = 22 – Masonry Nonlinear Hardening/Softening .....  | 40 |
| 4.2.9  | LAW = 33 – Orthotropic Boxed Value Model .....  | 42 |
| 4.2.10 | LAW = 40 – Geological Drucker-Prager .....  | 43 |
| 4.2.11 | LAW = 41 – Combination Mohr-Coulomb and Drucker-Prager resp. TRESCA vs. MISES.....                        | 44 |
| 4.3    | Numerical control variables .....   | 45 |
| 4.3.1  | Choice of the numerical control variables .....   | 45 |
| 4.3.2  | Remarks for choosing the material parameters .....  | 46 |
| 4.3.3  | Remarks and tips for using multiPlas in nonlinear structural analysis .....                               | 46 |
| 4.4    | Remarks for Postprocessing .....  | 48 |
| 5      | VERIFICATION EXAMPLES .....   | 50 |
| 5.1    | Example 1 – Earth pressure at rest.....   | 50 |
| 5.2    | Examples 2 to 4 - Earth pressure at rest and active earth pressure.....                                   | 52 |
| 5.3    | Examples 5 to 8 - Kienberger Experiment G6 [6-13] .....   | 56 |
| 5.4    | Example 9 - MOHR-COULOMB anisotropic .....  | 62 |
| 5.5    | Example 10 – Concrete-model DRUCKER-PRAGER singular (LAW=9) .....   | 63 |
| 5.6    | Example 11 – Concrete-model DRUCKER-PRAGER singular (LAW=9) .....   | 65 |
| 5.7    | Example 12 – Masonry-model with softening (LAW=20) .....  | 67 |
| 5.8    | Example 13 – Masonry-model with softening (LAW=20) .....  | 68 |
| 5.9    | Example 14 – Masonry-model with hardening and softening (LAW=22).....                                     | 69 |
| 5.10   | Example 15 – Masonry-model with hardening and softening (LAW=22).....                                     | 70 |
| 5.11   | Example 16 – Masonry-model with hardening and softening (LAW=22).....                                     | 71 |
| 5.12   | Example 17 – Masonry-model with hardening and softening (LAW=22).....                                     | 72 |
| 5.13   | Example 18 – Masonry-model (LAW=20) shear test 1 .....  | 73 |
| 5.14   | Example 19 – Masonry-model (LAW=20) Shear test 2 .....  | 74 |
| 5.15   | Example 20 – Wood-model (LAW=33) uniaxial compressive tests .....   | 75 |
| 5.16   | Example 21 – Wood-model (LAW=33) uniaxial tensile tests .....   | 77 |
| 5.17   | Example 22 – Single Joint Shear-Test (LAW=1, 10) .....  | 79 |
| 5.18   | Example 23 – Single Joint Tensile-Test (LAW=1, 10) .....  | 80 |

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|       |  |    |
|-------|--|----|
| 6     | REFERENCES .....                         | 81 |
| 7     | APENDIX USER INTERFACE - USERMPLS.....   | 83 |
| 7.1.1 | LAW = 99 – User-Material.....            | 83 |
| 7.1.2 | Requirements of ANSYS (Release 13) ..... | 83 |
| 7.1.3 | User materials in multiPlas.....         | 84 |

# 1 INTRODUCTION

This manual describes the use of Dynardo's software product **multiPlas** for ANSYS. multiPlas is a library of elasto-plastic material models for ANSYS.

The elasto-plastic material models in multiPlas, enable the user to simulate elasto-plastic effects of artificial materials, e.g. steel or concrete, and natural born materials, e.g. soil or rock, in geotechnics, civil engineering - as well as - mechanical engineering.

In the context of finite element calculations with ANSYS, multiPlas provides an efficient and robust algorithm for the handling of single and multi-surface plasticity. The material models are based on elasto-plastic flow functions with associated and non-associated flow rules. One special feature of the multiPlas material models is the combination of isotropic and anisotropic yield conditions.

The multiPlas material models are available for structural volume elements (e.g. SOLID 45, SOLID 95), for structural shell elements (e.g. SHELL 43, SHELL 93) and structural plane elements (e.g. PLANE 42, PLANE 82).

The following material models and features are provided:

| Model                        | Application                                     | Flow Rule       | Stress-Strain Response                       | Temperature Dependency |
|------------------------------|---|-----------------|--|------------------------|
| isotropic Material Models:   |   |                 |  |                        |
| Tresca                       | Steel, ...                                      | associative     | bilinear,<br>ideal elastic-plastic           |                        |
| Mohr-Coulomb                 | Soil, Rock, Stone,<br>Masonry, ...              | non-associative | bilinear,<br>residual strength               | yes                    |
| von Mises                    | Steel, ...                                      | associative     | bilinear,<br>ideal elastic-plastic           |                        |
| Drucker-Prager               | Soil, Stone, ...                                | associative     | bilinear,<br>ideal elastic-plastic           |                        |
| modified Drucker-Prager      | Stone, Cement,<br>Concrete, ...                 | associative     | bilinear,<br>ideal elastic-plastic           | yes                    |
| Concrete                     | Concrete, Cement,<br>Stone, Brick, ...          | non-associative | nonlinear hardening<br>and softening         | yes                    |
| Tension cut off              | rotated cracking                                | associative     | residual strength                            |                        |
| anisotropic Material Models: |   |                 |  |                        |
| Mohr-Coulomb                 | Joints, jointed<br>Rock, Cohesive<br>Zones, ... | non-associative | bilinear,<br>residual strength               |                        |
| Masonry_Ganz                 | Masonry, ...                                    | non-associative | nonlinear hardening<br>and softening         | yes                    |
| Tsai / Wu                    | Wood, ...                                       | associative     | bilinear,<br>ideal elastic-plastic           |                        |
| boxed value                  | Wood, ...                                       | associative     | multilinear hardening<br>and softening       |                        |
| Tension cut off              | fixed cracking,<br>Cohesive Zones               | associative     | residual strength /<br>exponential softening |                        |

Additionally, all Mohr-Coulomb Models are coupled with a tension cut-off yield surface.

In simulations of joint materials (e.g. jointed rock), it is possible to arrange the joint sets arbitrarily. Isotropic and anisotropic Mohr-Coulomb yield surfaces can be combined in manifold ways. Up to 4 joint sets can be associated with an isotropic strength definition.

MultiPlas has been successfully applied in nonlinear simulations of concrete as well as in stability analysis of soil or jointed rock.

## 2 INSTALLATION INSTRUCTIONS

multiPlas provides a customized executable (ANSYS.EXE) for ANSYS. The multiPlas package is delivered as a single zip-file, e.g. multiPlas\_418\_ansys145\_64bit.zip. Please extract this file into an arbitrary directory, e.g. C:\Program Files\ANSYS Inc\v145. A new sub-directory, multiPlas\_4.1.8 is created. Please notice the full path to your multiPlas installation. There is no further installation required for multiPlas.

In addition the multiPlas license file, e.g. *dynardo\_client.lic*, must be copied into one of the following directories:

- the application installation directory
- the "%Program Files%\Dynardo\Common files" directory (Unix: "~/.config/Dynardo/Common")
- the users home directory (Unix: \$HOME, Windows: %HOMEPATH%)
- the current working directory

For any further questions of licensing, please contact your system administrator or write an E-mail to [support@dynardo.de](mailto:support@dynardo.de)

### 2.1 How to start ANSYS Mechanical APDL with multiPlas

The ANSYS Mechanical APDL Product Launcher can be used to start ANSYS Mechanical APDL with multiPlas. After starting the launcher, choose the “Customization/Preferences” tab. In the field “Custom ANSYS executable” browse to the ANSYS.EXE in your multiPlas installation directory. This procedure is summarized in Fig. 2-1.

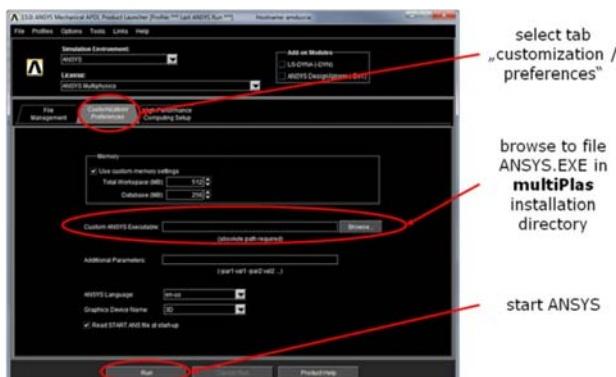


Fig. 2-1: start multiPlas in ANSYS Mechanical APDL via launcher

Another possibility is to start ANSYS Mechanical APDL from command line using the option “–custom <multiPlasDir>\ANSYS.EXE”, where <multiPlasDir> must be replaced by the full (absolute) path to your multiPlas installation.

The following command line starts ANSYS Mechanical APDL with multiPlas in graphical mode:  
 "C:\Programme\ANSYS Inc\v145\ansys\bin\winx64\ansys.exe" –g –custom "<multiPlasDir>\ANSYS.EXE"

The corresponding command line for batch mode is:

"C:\Programme\ANSYS Inc\v145\ansys\bin\winx64\ansys.exe" –b –i <InputFile> -o <OutputFile> –custom "<multiPlasDir>\ANSYS.EXE"

An example of the windows-batch script is included in the shipment.

Note: The path to the customized multiPlas executable must be enclosed in quotation marks.

For any further command line options please take a look at the ANSYS operations guide:

Operations Guide, chapter 3, Running the ANSYS Program, 3.1.

Starting an ANSYS Session from the Command Level

### 2.2 How to use ANSYS Workbench with multiPlas

In order to enable multiPlas in ANSYS Workbench the solver settings in Mechanical must be customized. In ANSYS Mechanical:

- Select “**Solve Process Settings...**“ from menu “**Tools**“
- Choose the solver settings to be modified and select “**Advanced...**“
- Add the following option to the field “**Additional Command Line Arguments**”: –custom “<multiPlasDir>\ANSYS.EXE”

### 3 THEORY OF THE MULTIPLAS MATERIAL MODELS IN ANSYS

#### 3.1 Basics of elasto-plasticity in multiPlas

The material models in multiPlas uses a rate-independent plasticity. The material models are characterized by the irreversible strain that occurs once yield criteria are violated. It is assumed that the total strain vector can be divided into a elastic and a plastic component.

$$\{\varepsilon\}^{tot} = \{\varepsilon\}^{el} + \{\varepsilon\}^{pl} \quad (3-1)$$

where:

$\{\varepsilon\}^{el}$  – elastic strain vector (EPEL)  
 $\{\varepsilon\}^{pl}$  – plastic strain vector (EPPL)

The plastic strains are assumed to develop instantaneously, that is, independent of time.

The yield criterion

$$F(\{\sigma\}, \kappa) \leq 0 \quad (3-2)$$

where:

$\{\sigma\}$  - stress vector  
 $\kappa$  - hardening parameter

limit the stress domain. If the computed stress, using the elastic deformation matrix, exceeds the yield criteria ( $F>0$ ), then plastic strain occurs. Plastic strains will be computed by flow rule

$$d\varepsilon^{pl} = \lambda \frac{\partial Q}{\partial \sigma} \quad (3-3)$$

where:

$\lambda$  - plastic multiplier (which determines the amount of plastic straining)  
 $Q$  - plastic potential (which determines the direction of plastic straining)

The plastic strains reduce the stress state so that it satisfies the yield criterion ( $F=0$ ). By using associated flow rules, the plastic potential is equal the yield criterion and the vector of plastic strains is arranged perpendicularly to the yield surface.

$$Q = F \quad (3-4)$$

By using non-associated flow rules

$$Q \neq F \quad (3-5)$$

effects that are known from experiments like dilatancy can be controlled more realistically.

The hardening / softening function  $\Omega(\kappa)$  describes the expansion and the reduction of the initial yield surface dependant on the load path, as well as the translation of the yield criterion in the stress domain. For the strain driven hardening/softening equations in multiPlas the scalar value  $\kappa$  serves as a weighting factor for plastic strain.

$$d\kappa = d\kappa(\varepsilon^{pl}) = d\varepsilon_{eq}^{pl} \quad (3-6)$$

The introduction of a separate softening function for each strength parameter made it possible to formulate an orthotropic softening model that is dependent from the failure mode. Existing relations, for example shear-tension interaction (mixed mode), were recognised.

The numerical implementation of the plasticity models is carried out using the return-mapping method [6-17], [6-18], [6-22]. The return mapping procedure is used at the integration point for the local iterative stress relaxation. It consists of two steps:

1. elastic predictor step:

$$\sigma_{i+1}^{\text{trial}} = \sigma_i^* + D d\epsilon_{i+1}^{\text{tot}} \quad (3-7)$$

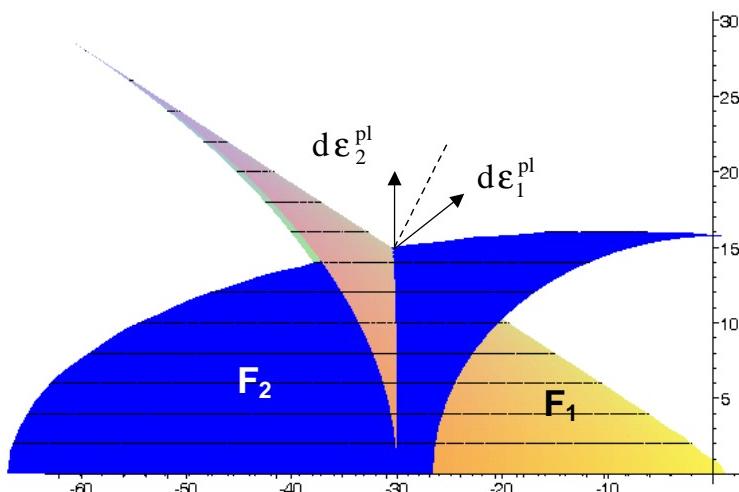
2. plastic corrector step (local iterative procedure):

$$\frac{d\sigma}{d\lambda} = -D \frac{\partial Q}{\partial \sigma} \quad (3-8)$$

### 3.2 Multisurface plasticity

The consideration of different failure modes resp. failure mechanisms of a material is possible by a yield surface built up from several yield criteria. In the stress domain then a non-smooth multisurface yield criterion figure develops.

The elastic plastic algorithm has to deal with singularities at intersections from different yield criteria (e.g. F1 to F2 as represented in Fig. 3-1).



**Fig. 3-1 Intersection between the two flow criteria F1 and F2**

The consistent numerical treatment of the resulting multi-surface plasticity must deal with the possibility that many yield criteria are active simultaneously. This leads to a system of  $n=j$  equations:

$$\left\{ \frac{\partial F_n}{\partial \sigma} \right\}^T D d\epsilon = \sum_{j=1}^{\text{Set of active YC}} \left[ \left\{ \frac{\partial F_n}{\partial \sigma} \right\}^T D \frac{\partial Q_j}{\partial \sigma} - \frac{\partial F_n}{\partial \kappa_n} \frac{\partial \kappa_n}{\partial \lambda_j} \right] d\lambda_j \quad (3-9)$$

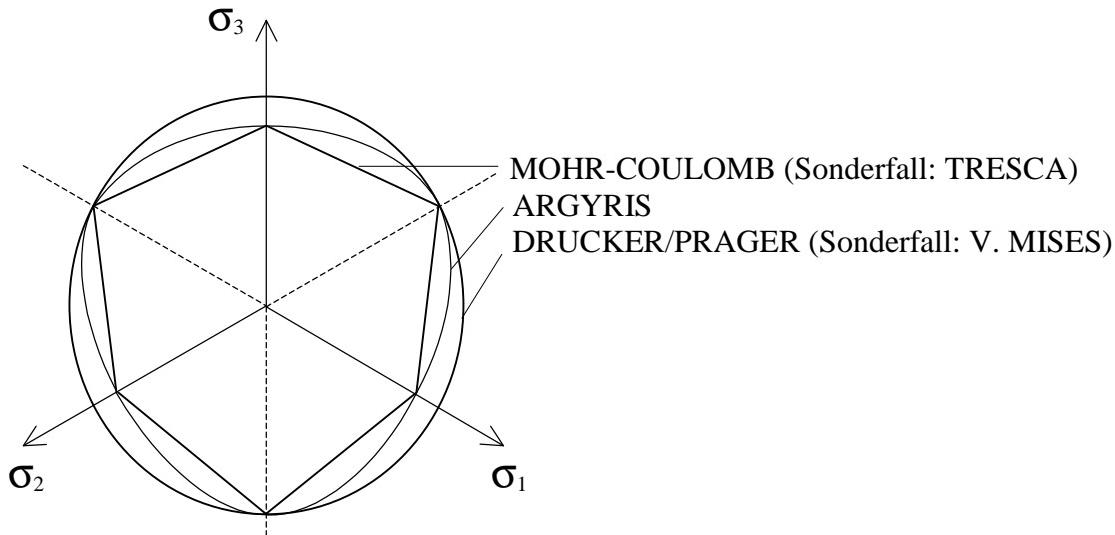
The solution of this system of equations generates the stress return to flow criteria or within the intersection of flow criterias. Contrary to single surface plasticity exceeding the flow criterion is no longer a sufficient criterion for activity of the plastic multiplier for each active yield criterion. An activity criterion needs to be checked.

$$d\lambda_j \geq 0 \quad (3-10)$$

This secures that the stress return within the intersection is reasonable from a physical point of view.

### 3.3 Computed yield surfaces

#### 3.3.1 Introduction yield surfaces of basic material models



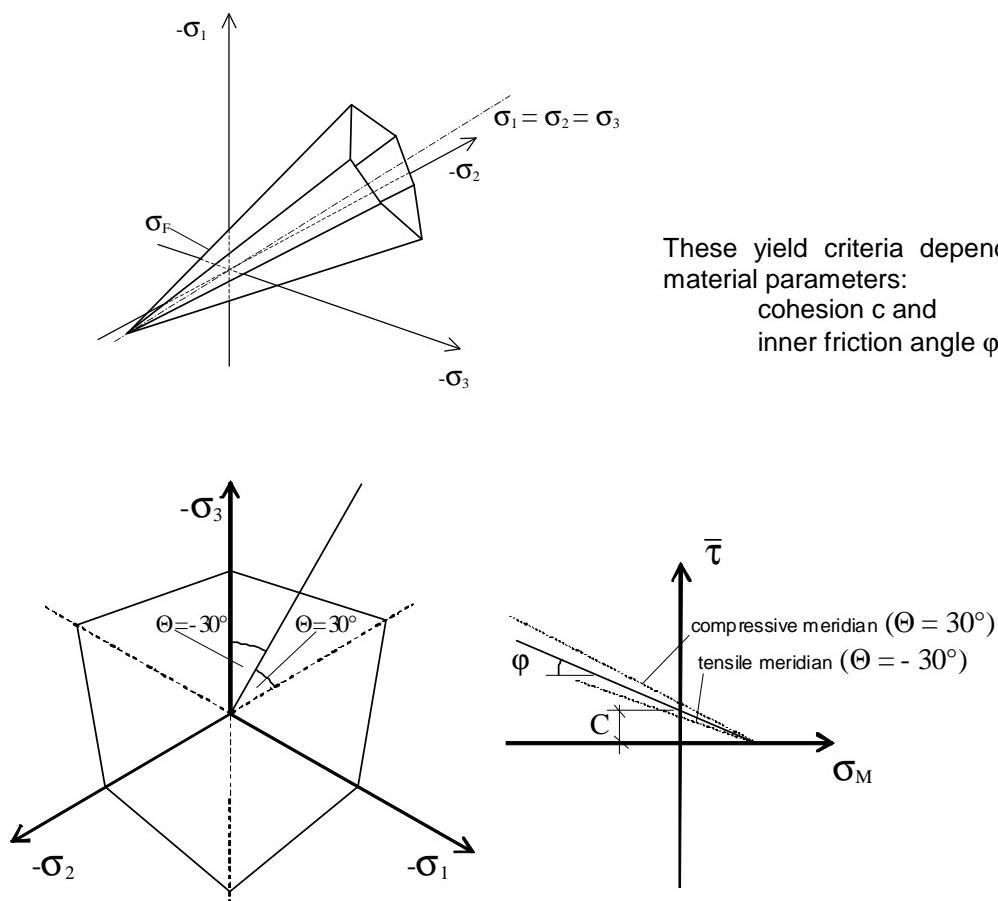
**Fig. 3-2 Cut in the deviator plane of different flow figures**

Miscellaneous yield criteria of soil or rock mechanics generally describe flow figures which lie in between the flow figure of Mohr-Coulomb and of Drucker-Prager. . The difference in the area, surrounded by the yield surface (elastic stress domain) in the deviator-cut-plane, is 15% at its maximum.

In the standard literature of soil mechanics, the general usage of Mohr-Coulomb material models is suggested. Yield graphs according to Drucker and Prager do in fact generally overestimate the bearing strength.

For brittle materials (concrete/rock) composite flow conditions on the basis of Mohr-Coulomb as well as composite flow conditions on the basis of Drucker-Prager are used in the standard literature.

### 3.3.2 MOHR-COULOMB isotropic yield criterion



**Fig. 3-3 MOHR-COULOMB isotropic yield criterion**

The yield criterion is:

$$F = \sigma_m \sin \varphi + \sigma_s \left( \cos \Theta - \frac{\sin \Theta \sin \varphi}{\sqrt{3}} \right) - c \cos \varphi \quad (3-11)$$

where:

$$\sigma_m = \frac{\sigma_x + \sigma_y + \sigma_z}{3} \quad (3-12)$$

$$\sigma_s = \sqrt{I_2} \quad (3-13)$$

$$\sin(3\Theta) = -\frac{3\sqrt{3}}{2} \frac{I_3}{I_2^{3/2}} \quad (3-14)$$

|            |  |
|------------|--|
| $\sigma_m$ | hydrostatic stress                               |
| $I_2$      | second invariant of the deviatoric main stresses |
| $I_3$      | third invariant of the deviatoric main stresses  |
| $\Theta$   | Lode-angle                                       |

---

Necessary material parameters in the ANSYS material model MOHR-COULOMB isotropic:

- φ – inner friction angle (phi)
- C – cohesion
- $f_t$  – tensile strength (in case of tension cut off)
- ψ – dilatancy angle (psi)

The residual strength can be defined. The residual strength is initiated after the yield strength has been exceeded.

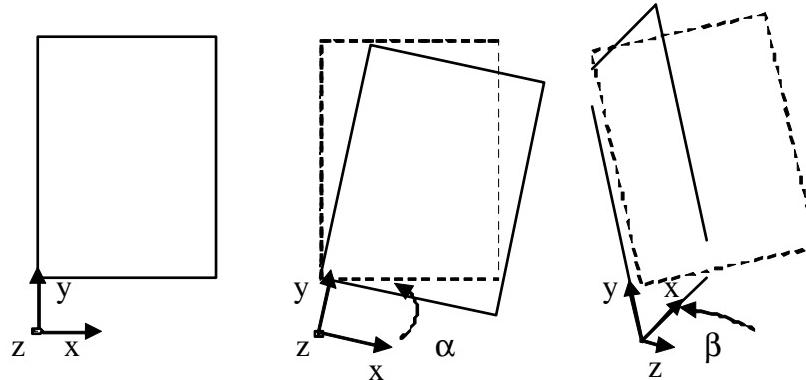
The uniaxial compressive strength corresponds with the friction angle and cohesion as shown below:

$$f_c = c \frac{2 \cos \varphi}{1 - \sin \varphi} = 2c \tan\left(45 + \frac{\varphi}{2}\right) \quad (3-15)$$

### 3.3.3 MOHR-COULOMB anisotropic yield criterion

For the definition of joints, separation planes or strength anisotropies the position of the yield surface depends on the position of the two joint-angles:

The two angles „First Angle“ ( $\alpha$ ) and „Second Angle“ ( $\beta$ ) describe the position of the joint / separation plane.

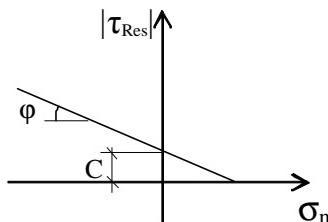


1.  $\alpha$  - rotation against positive rotational direction about the z-axis
2.  $\beta$  - rotation in positive rotational direction about the y-axis

**Fig. 3-4 Angle definition of the joint**

The yield criterion is:

$$|\tau_{\text{Res}}| - \sigma_n \cdot \tan \varphi - C = 0 \quad (3-16)$$



**Fig. 3-5 MOHR-COULOMB anisotropic yield criterion**

where:

$\tau_{\text{Res}}$  – shear stress in the joint

$\sigma_n$  – normal stress perpendicular to the joint

Necessary material parameters in the ANSYS material model MOHR-COULOMB anisotropic:

$\alpha, \beta$  – position angle of the family or separation planes

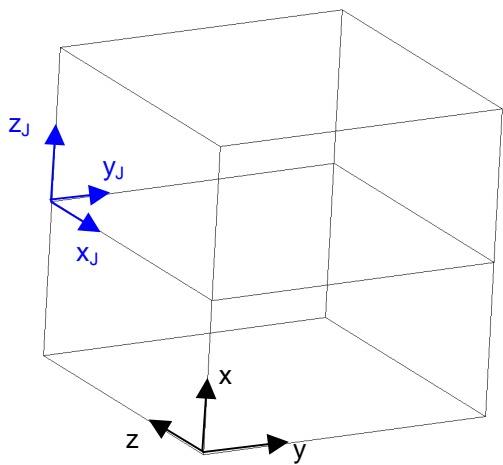
$\varphi$  – friction angle

$C$  – cohesion

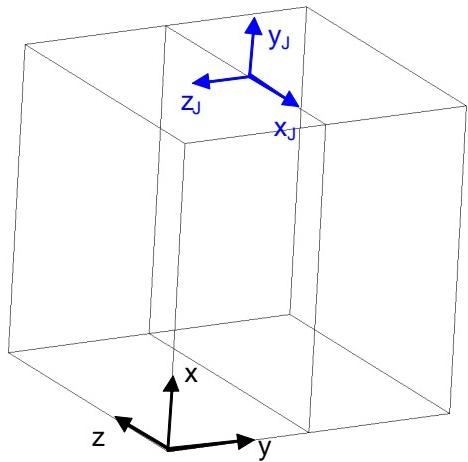
$f_t$  – tensile strength (in case of tension cut off)

$\psi$  – dilatancy angle

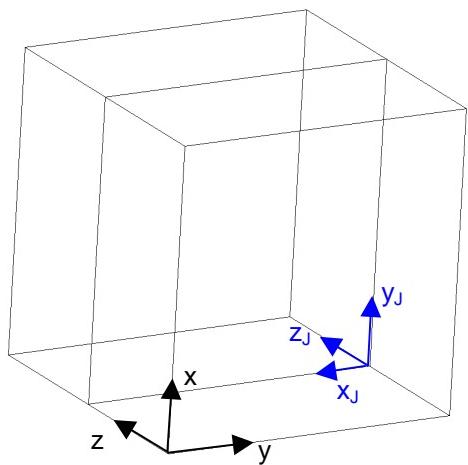
Residual strength can be defined. The residual strength is initiated after the yield strength has been exceeded.



$$\alpha=0^\circ, \beta=90^\circ$$



$$\alpha=90^\circ, \beta=90^\circ$$



$$\alpha=90^\circ, \beta=0^\circ$$

$x, y, z$  – Element coordinate system  
 $x_J, y_J, z_J$  – joint coordinate system

**Fig. 3-6 Examples for the angle definition of joints**

### 3.3.4 Yield criterion according to DRUCKER-PRAGER

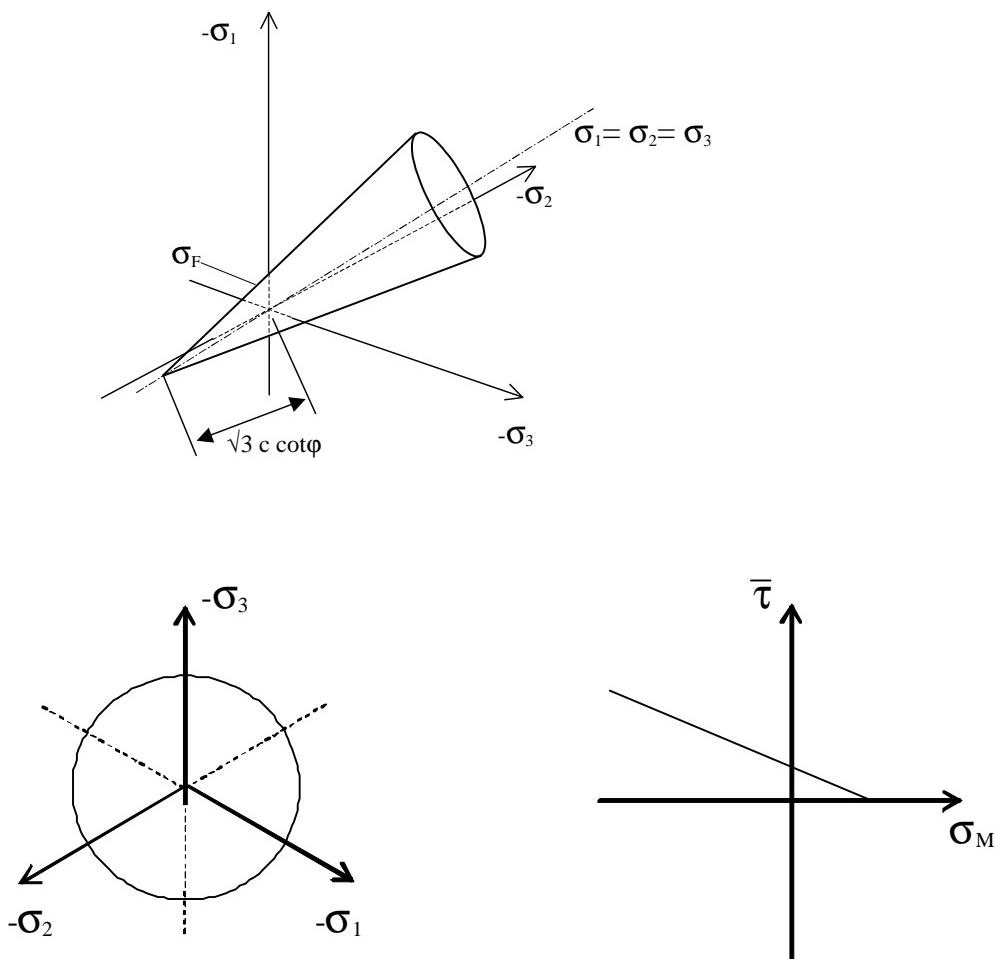


Fig. 3-7 Flow conditions according to DRUCKER-PRAGER

The Drucker-Prager yield criterion is:

$$F = \sigma_s + \beta \sigma_m - \tilde{\sigma}_{yt} \quad (3-17)$$

The plasticity potential is:

$$Q = \sigma_s + \beta \delta \sigma_m \quad (3-18)$$

where:

- |            |  |
|------------|--|
| $\sigma_m$ | hydrostatic stress s. (3.12)                               |
| $I_2$      | second invariant of the deviatoric main stresses s. (3.13) |
| $\delta$   | dilatancy factor   |

The Drucker-Prager yield criterion can approximate the Mohr-Coulomb failure condition as circumlocutory cone or as inserted to a cone (see Fig. 3-8). Using the material library multiPlas calculation of arbitrary

interim values or blending with Mohr-Coulomb failure conditions are possible as well. Necessary material parameters in the ANSYS multiPlas material model DRUCKER/PRAGER are

$\beta$  and  $\tilde{\sigma}_y$ .

Both parameters are connected to cohesion and angle of friction by the following formula:

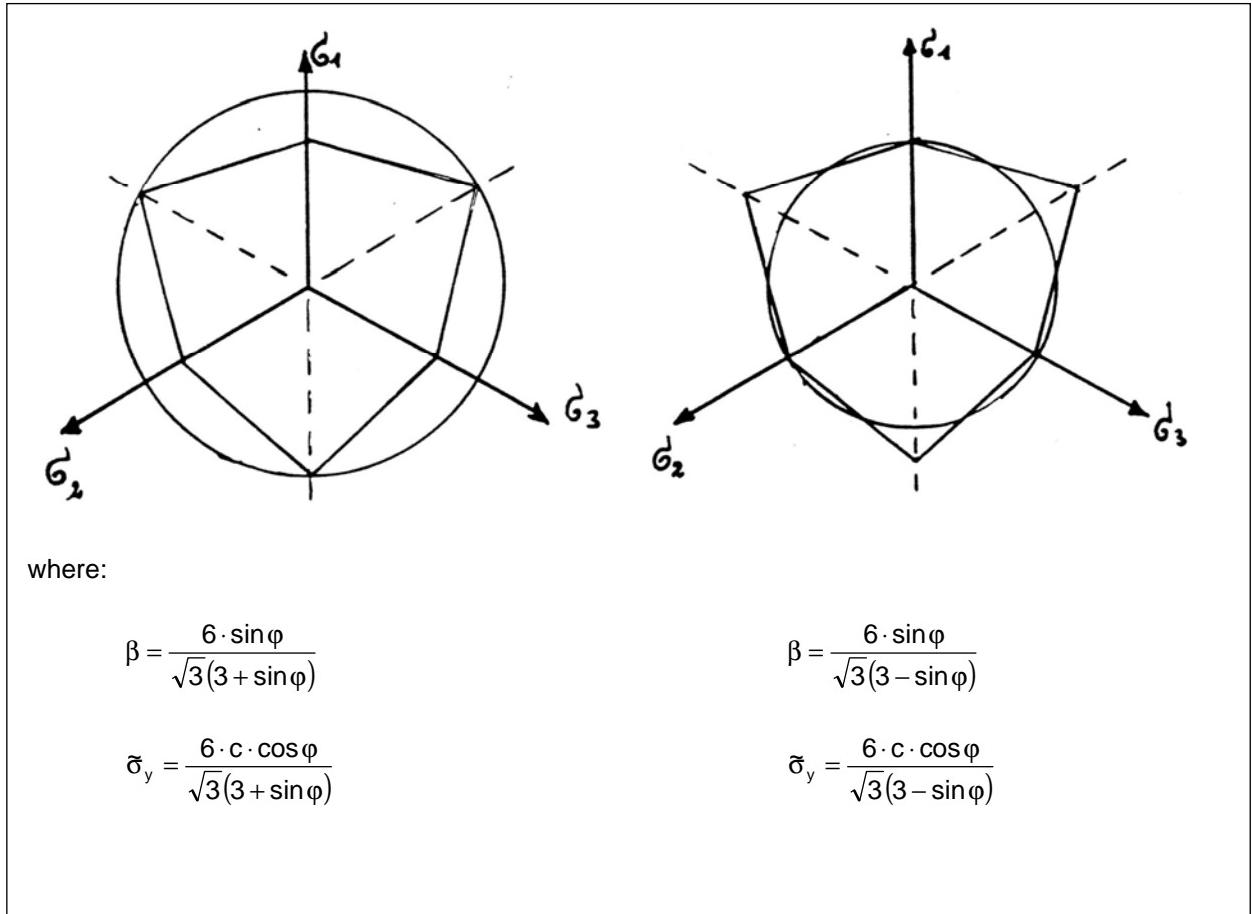


Fig. 3-8 Drucker-Prager yield criterion as circumlocutory cone (left) or inserted to a cone (right).

### 3.3.5 Combination of flow condition according to MOHR-COULOMB and DRUCKER-PRAGER or TRESCA and von MISES

As shown in

Fig. 3-8 the MOHR-COULOMB and the DRUCKER-PRAGER yield criterion differ in the elastic stress domain. The difference of the surrounded area in the deviator cut plane is 15% at the maximum.

For some problem formulations it can be necessary to limit the elastic stress domain to the area given by the MOHR-COLOUMB yield criterion. In cases if MOHR-COULOMB or TRESCA alone lead to poor convergence or even divergence, it can be reasonable to use a combination of the yield criteria to stabilize the numerical computation.

It has to be kept in mind that this combination is reasonable only for numerical stabilization. It leads inevitably to differences in the results contrary to the sole usage of the yield criterion by MOHR-COULOMB. The return-mapping of the stress is not commutated exactly for both criteria – MOHR-COULOMB and DRUCKER-PRAGER. Therefore, the permissibility of these result has to be checked individually!

### 3.3.6 Concrete modelling using modified DRUCKER-PRAGER model

The yield condition consists of two yield criteria (equations (3-19), (3-20)), whereby the concrete strength can be described closed to the reality as well in the compressive as in the tensile domain.

$$F_1 = \sigma_s + \beta_t \sigma_m - \tilde{\sigma}_{yt} \Omega_1 \quad (3-19)$$

$$\beta_t = \frac{\sqrt{3} (R_d - R_z)}{R_d + R_z} \quad \tilde{\sigma}_{yt} = \frac{2 R_d R_z}{\sqrt{3} (R_d + R_z)}$$

$$F_2 = \sigma_s + \beta_c \sigma_m - \tilde{\sigma}_{yc} \Omega_2 \quad (3-20)$$

$$\beta_c = \frac{\sqrt{3} (R_u - R_d)}{2 R_u - R_d} \quad \tilde{\sigma}_{yc} = \frac{R_u R_d}{\sqrt{3} (2 R_u - R_d)}$$

where:

- $\sigma_m$  hydrostatic stress
- $I_2$  second invariant of the deviatoric main stresses
- $R_z$  uniaxial tensile strength
- $R_d$  uniaxial compression strength
- $R_u$  biaxial compression strength
- $\Omega$  hardening and softening function (in the pressure domain  $\Omega_1 = \Omega_2 = \Omega_c$ , in the tensile domain  $\Omega_1 = \Omega_t$ ).

The plasticity potentials are:

$$Q_1 = \sigma_s + \delta_t \beta_t \sigma_m \quad \text{where: } \delta_t, \delta_c \text{ are dilatancy factors} \quad (3-21)$$

$$Q_2 = \sigma_s + \delta_c \beta_c \sigma_m$$

The yield condition is shown in Fig. 3-9 and Fig. 3-10 in different coordinate systems. The comparison with the concrete model made by Ottosen [6-15] is shown in Fig. 3-9 and illustrates the advantages of the Drucker-Prager model consisting of two yield criteria. While there is a very good correspondence in the compressive domain, the chosen Drucker-Prager model can be well adjusted to realistic tensile strength. In opposite to that, the Ottosen model overestimates these areas significantly! A further advantage lies within the description of the yield condition using the three easily estimable and generally known parameters  $R_z$ ,  $R_d$  and  $R_u$ .

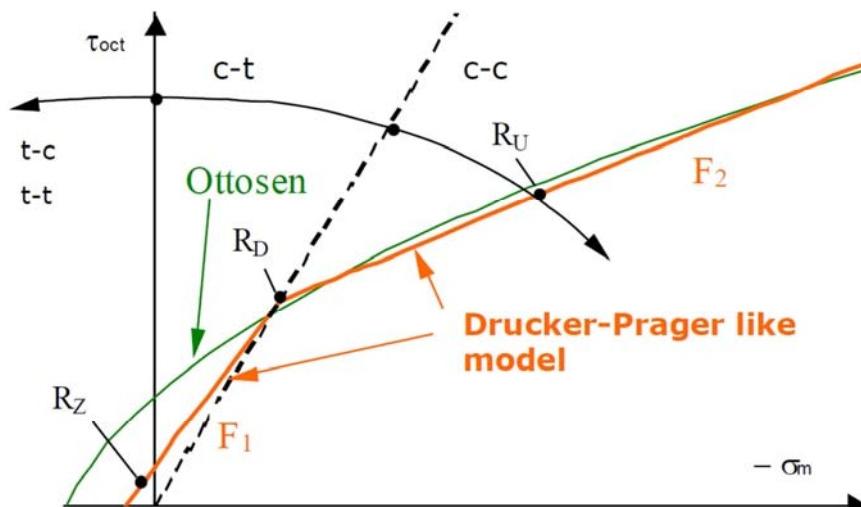
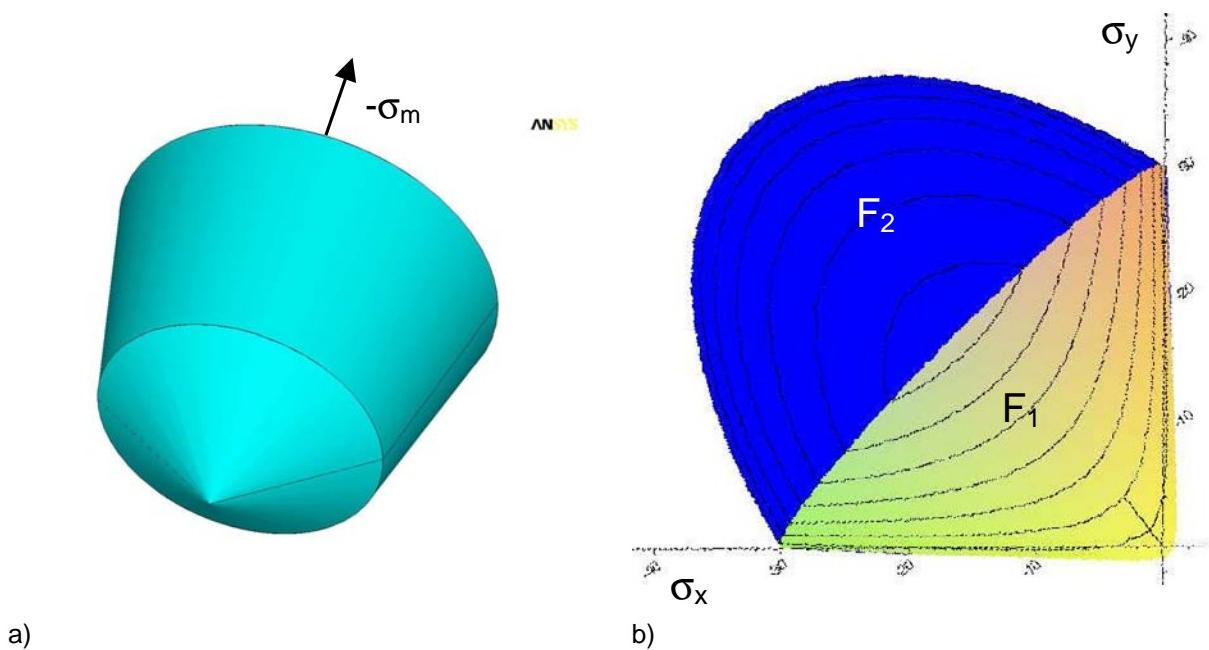


Fig. 3-9 Singular Drucker-Prager flow conditions – Illustrated in the octaeder system



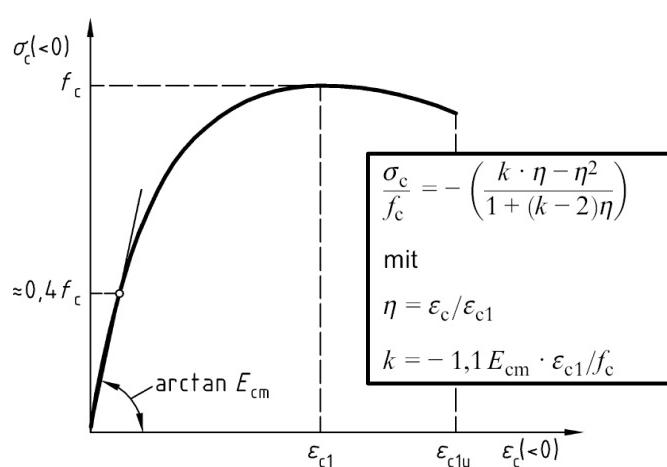
**Fig. 3-10 Singular Drucker-Prager flow condition:**  
a) yield surface in the main stress domain; b) illustration in the  $\sigma_x$ - $\sigma_y$ - $\tau_{xy}$ -space

### 3.3.6.1 Nonlinear deformation behaviour in case of pressure load

In general the uniaxial stress-strain relationship of concrete is characterized by three domains:

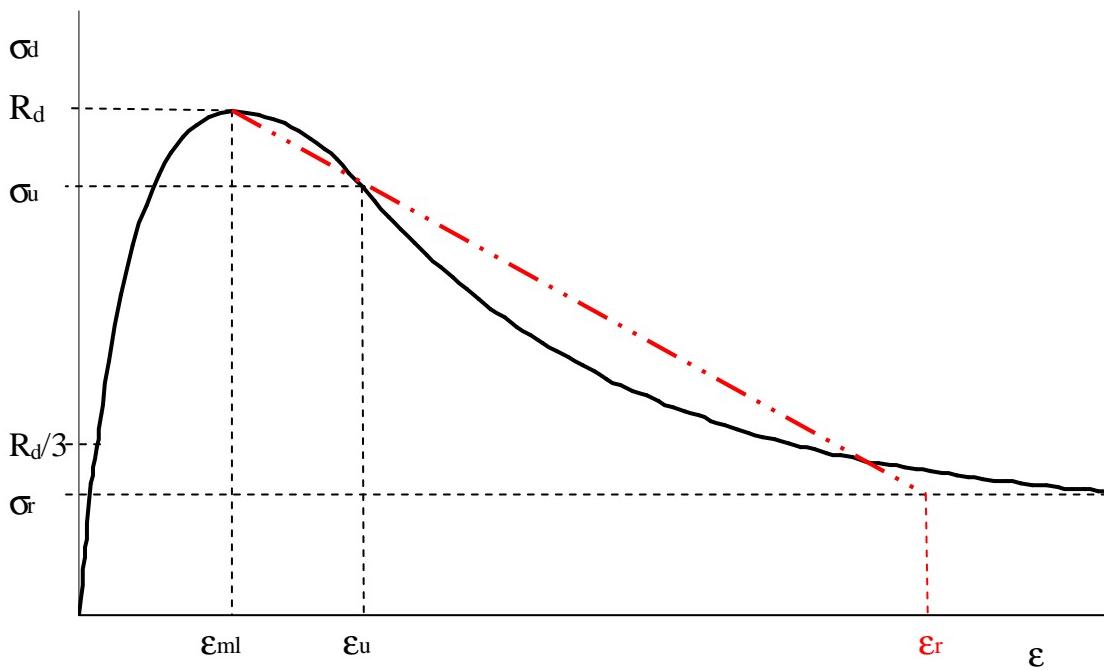
- A linear elastic domain which generally reaches up to about a third of the compressive strength.
- This is followed by an increasingly bent run until the compressive strength is reached. The nonlinear relation between stress and strain is caused by an initially small number of micro-cracks which merge with higher stress levels.
- The achievement of the compressive strength is associated with the forming of fracture surfaces and cracks which are aligned parallel to the largest main stress.
- The softening area is characterized by a decreasing strength. Finally, it leads to a low residual strain level. The slope of the decreasing branch is a measure for the brittleness of the material.

Fig. 3-11 shows the typical nonlinear stress-strain relation of normal concrete in uniaxial compressive tests [6-9].



**Fig. 3-11 Nonlinear stress-strain relation (uniaxial compression test) of normal concrete used in codes (DIN 1045-1 [6-9] and EC2 [6-10])**

In Fig. 3-12 the stress-strain relation which is available in multiPlas is shown. Thereby linear softening (mlaw = 0, 2) or parabolic-exponential softening (mlaw = 1) can be chosen. Up to reaching the strain  $\varepsilon_u$  the parabola equation (as seen in Fig. 3-11) is used.



**Fig. 3-12 stress-strain relation in multiPlas (mlaw=0,2; mlaw = 1)**

### 3.3.6.2 Nonlinear deformation behaviour during tensile load

Concrete tends to soften relatively brittle with local appearances of cracks. For including this into the context of a continuum model, a homogenized crack and softening model is needed. The crack itself does not appear in the topology description of the structure - but is described by its impact on stress and deformation state [6-16],[6-21].

The softening process is formulated respectively to the energy dissipation caused by the occurrence of cracks. For the complete cracking, the fracture energy concerning the crack surface has to be  $G_f$ -dissipated.

The used model has its origin within the crack band theory of Bažant / Oh [6-6]. It states that cracks develop within a local process zone. Its width  $h_{PR}$  (crack band width) is a material specific constant. To avoid a mesh dependency of the softening and to assess the fracture energy correctly, a modification of the work equation is necessary. For a given width of the crack band and a given fracture energy, the volume fracture energy can be computed via:

$$g_f = \frac{G_f}{h_{PR}} \quad (3-22)$$

where:

- |          |                        |
|----------|------------------------|
| $g_f$    | volume fracture energy |
| $G_f$    | fracture energy        |
| $h_{PR}$ | crack band width       |

For meshing of the structure with elements which are larger than the expected width of the crack band the stress-strain relationship has to be modified in such a way that the volume fracture energy reaches the following value:

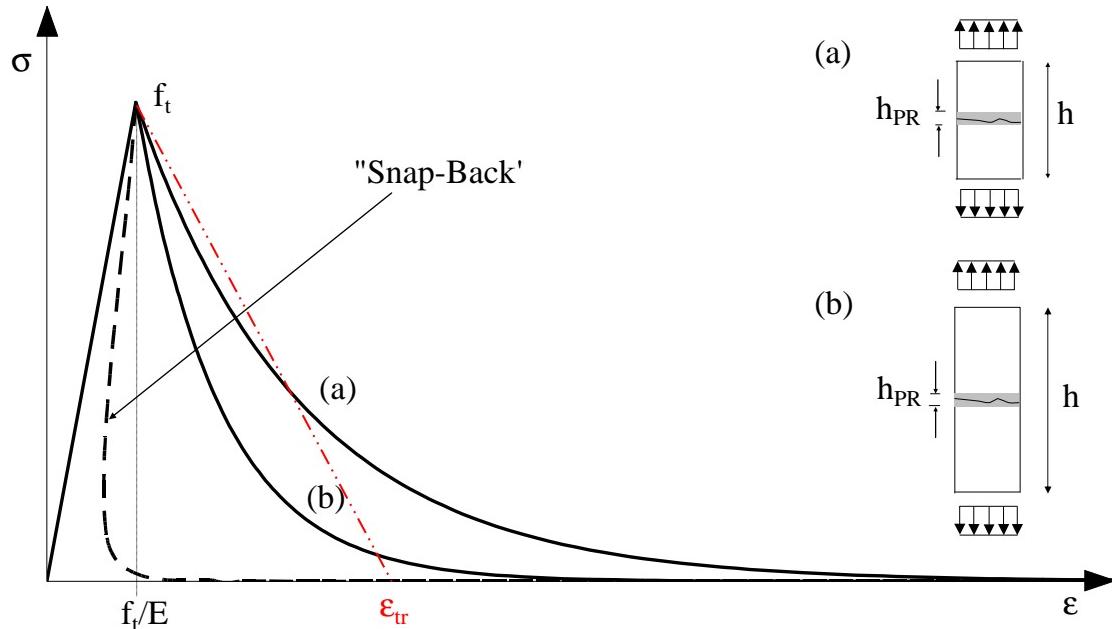
$$g_{f,INT} = \frac{h_{PR}}{h} g_f = \frac{G_f}{h} \quad (3-23)$$

where:  $g_{f,INT}$  volume fracture energy at the integration point  
 $h$  equivalent length

This model guarantees a consistent dissipation of fracture energy during the softening process for different sizes of elements. The stress-strain lines available in multiPlas are shown in Fig. 3-13. Thereby, a linear elastic behaviour is assumed until the tensile strength is reached. After that, one of the following is assumed as consequence of tensile fracturing:

\*\* linear softening until the strain limit is reached  $\varepsilon_{tr}$  (mlaw = 0, 2) or

\*\* exponential softening (mlaw = 1)



**Fig. 3-13 Stress-strain relation in multiPlas (mlaw=0, 2; mlaw = 1)**

For the exponential softening model (mlaw = 1) one should assume

$$h \leq \frac{G_f E}{f_t^2} \quad (3-24)$$

for the length  $h$  in order to avoid the numerically unstable „snap-back“ phenomena. This is preferably achieved by choosing a proper mesh size. In multiPlas, the equivalent length will be calculated automatically.

### 3.3.6.3 Temperature dependency

Information on the temperature dependencies of the material behaviour are included in DIN EN 1992-1-2 [6-11]. As an example the temperature dependencies from pressure level are shown in Fig. 3-14, Fig. 3-15 and Tab. 3-1.

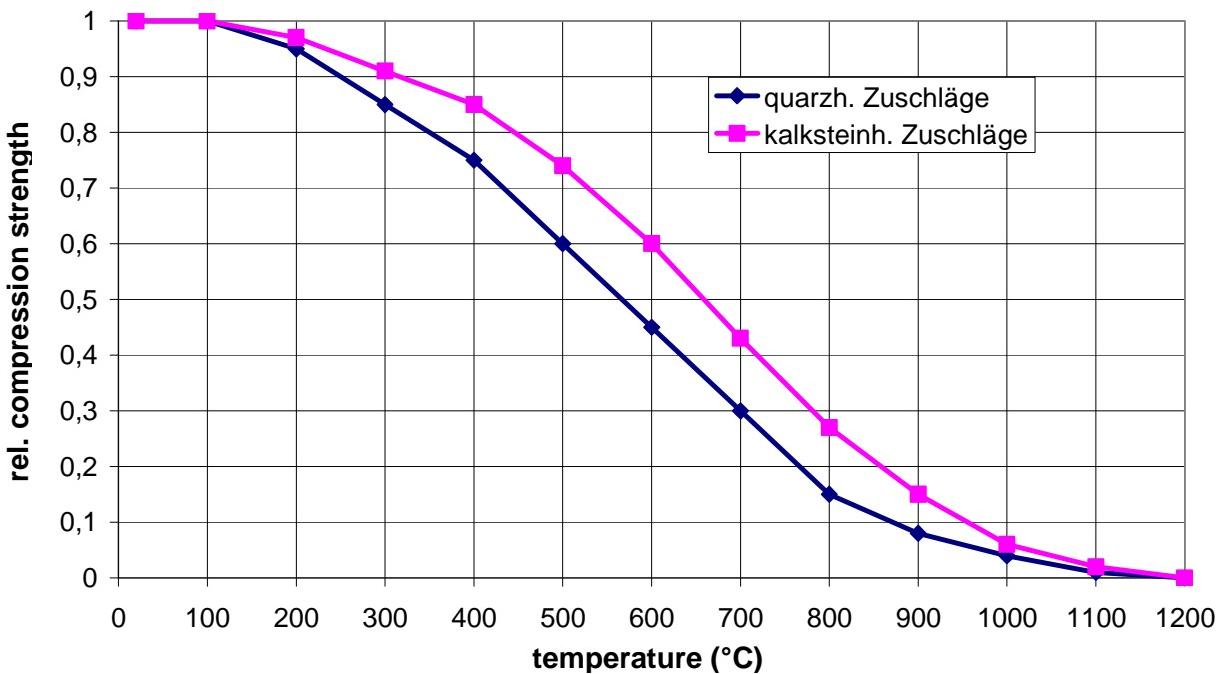


Fig. 3-14 Temperature dependency of concrete pressure resistance from [6-11]

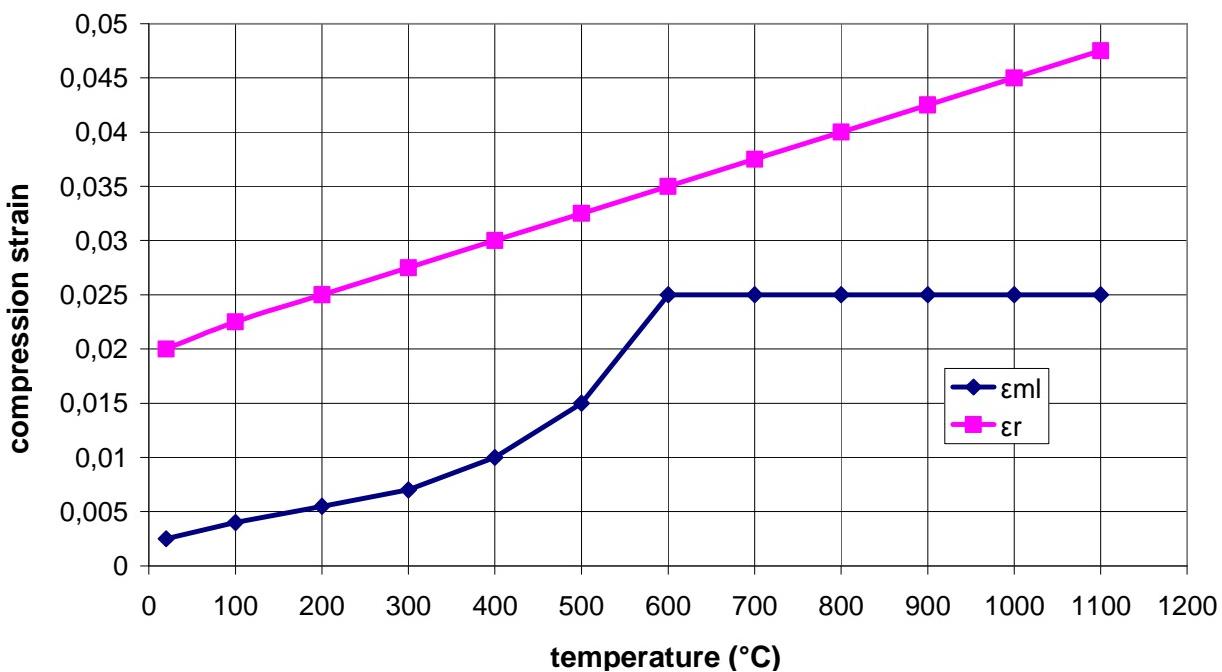


Fig. 3-15 Temperature dependency of concrete compression strain from [6-11]

| Beton  | quarzh. Zuschläge |                 |              | kalksteinh. Zuschläge |                 |              |  |
|--------|-------------------|-----------------|--------------|-----------------------|-----------------|--------------|--|
| T (°C) | R_d(T)/R_d        | $\epsilon_{ml}$ | $\epsilon_t$ | R_d(T)/R_d            | $\epsilon_{ml}$ | $\epsilon_t$ |  |
| 20     | 1                 | 0,0025          | 0,02         | 1                     | 0,0025          | 0,02         |  |
| 100    | 1                 | 0,004           | 0,0225       | 1                     | 0,004           | 0,0225       |  |
| 200    | 0,95              | 0,0055          | 0,025        | 0,97                  | 0,0055          | 0,025        |  |
| 300    | 0,85              | 0,007           | 0,0275       | 0,91                  | 0,007           | 0,0275       |  |
| 400    | 0,75              | 0,01            | 0,03         | 0,85                  | 0,01            | 0,03         |  |
| 500    | 0,6               | 0,015           | 0,0325       | 0,74                  | 0,015           | 0,0325       |  |
| 600    | 0,45              | 0,025           | 0,035        | 0,6                   | 0,025           | 0,035        |  |
| 700    | 0,3               | 0,025           | 0,0375       | 0,43                  | 0,025           | 0,0375       |  |
| 800    | 0,15              | 0,025           | 0,04         | 0,27                  | 0,025           | 0,04         |  |
| 900    | 0,08              | 0,025           | 0,0425       | 0,15                  | 0,025           | 0,0425       |  |
| 1000   | 0,04              | 0,025           | 0,045        | 0,06                  | 0,025           | 0,045        |  |
| 1100   | 0,01              | 0,025           | 0,0475       | 0,02                  | 0,025           | 0,0475       |  |
| 1200   | 0                 |                 |              | 0                     |                 |              |  |

Tab. 3-1 Temperature dependency of concrete material values from [6-11]

In multiPlas up to 11 temperatures-pressure points and respective strains  $\epsilon_m$  can be predefined. The associated limit strains are assumed according to Tab. 3-1. Interim values are linearly interpolated. The temperature dependency of the concrete tensile strength is implemented in multiPlas using the Data from [6-11] (s. Fig. 3-16).

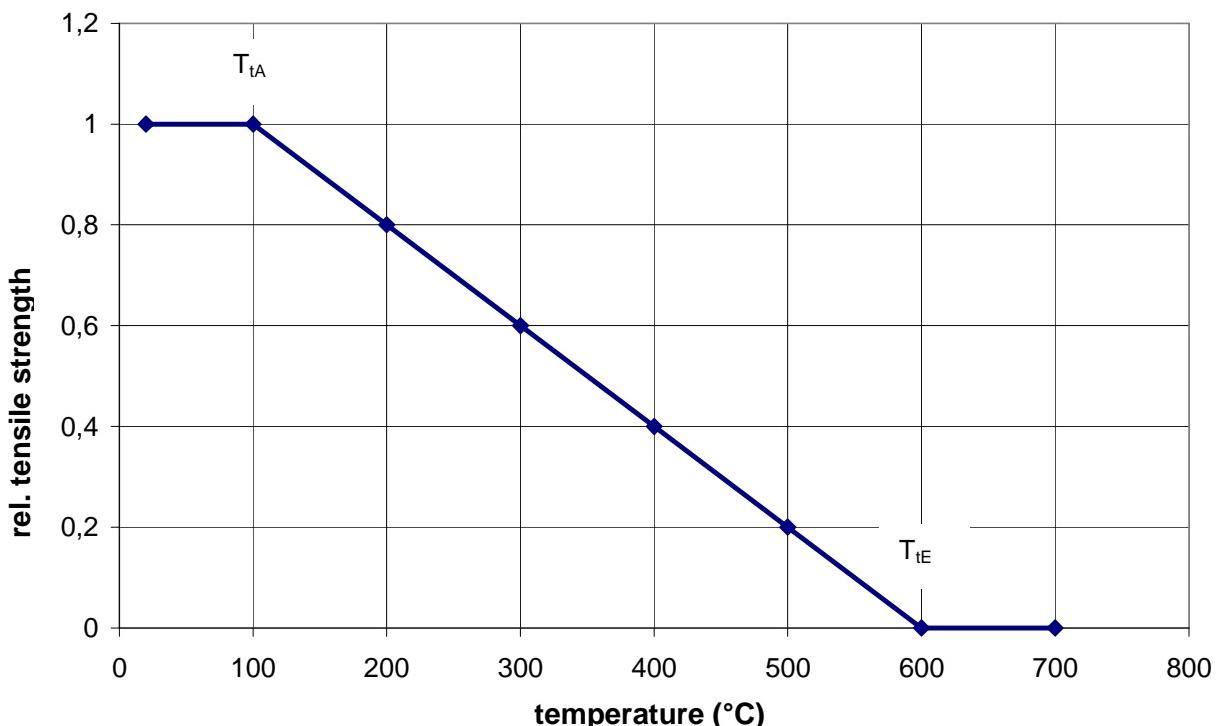


Fig. 3-16 Temperature dependency of the tensile strength of concrete from [6-11]

For the temperature dependency of steel reinforcement we refer to [6-11]. It can be taken into account by the standard parameters of ANSYS (tb,bkin oder tb,mkin).

### 3.3.7 Simulation of regular masonry using the Ganz yield condition

For describing the orthotropic strength of a regular masonry, an extended spatial masonry model was implemented which uses the Ganz yield criterion [6-23], [6-17]. It is the foundation of the Swiss masonry norm SIA 177/2 and complies with the fracturing model of Mann contained in DIN 1053 [6-24] as well as with the natural stone masonry model suggested by Berndt [6-25]. In the Ganz masonry model, an additionally interaction with a horizontal load (parallel to the longitudinal joint) is considered. The necessary material parameters of this model are compression- and tensile strength of the masonry, the friction angle and the cohesion between brick and joint as well as the brick dimensions. The multisurface yield condition (Fig. 3-17) represents the different failure mechanisms of regular masonry formation. The meaning of the yield criteria are given in Tab. 3-2.

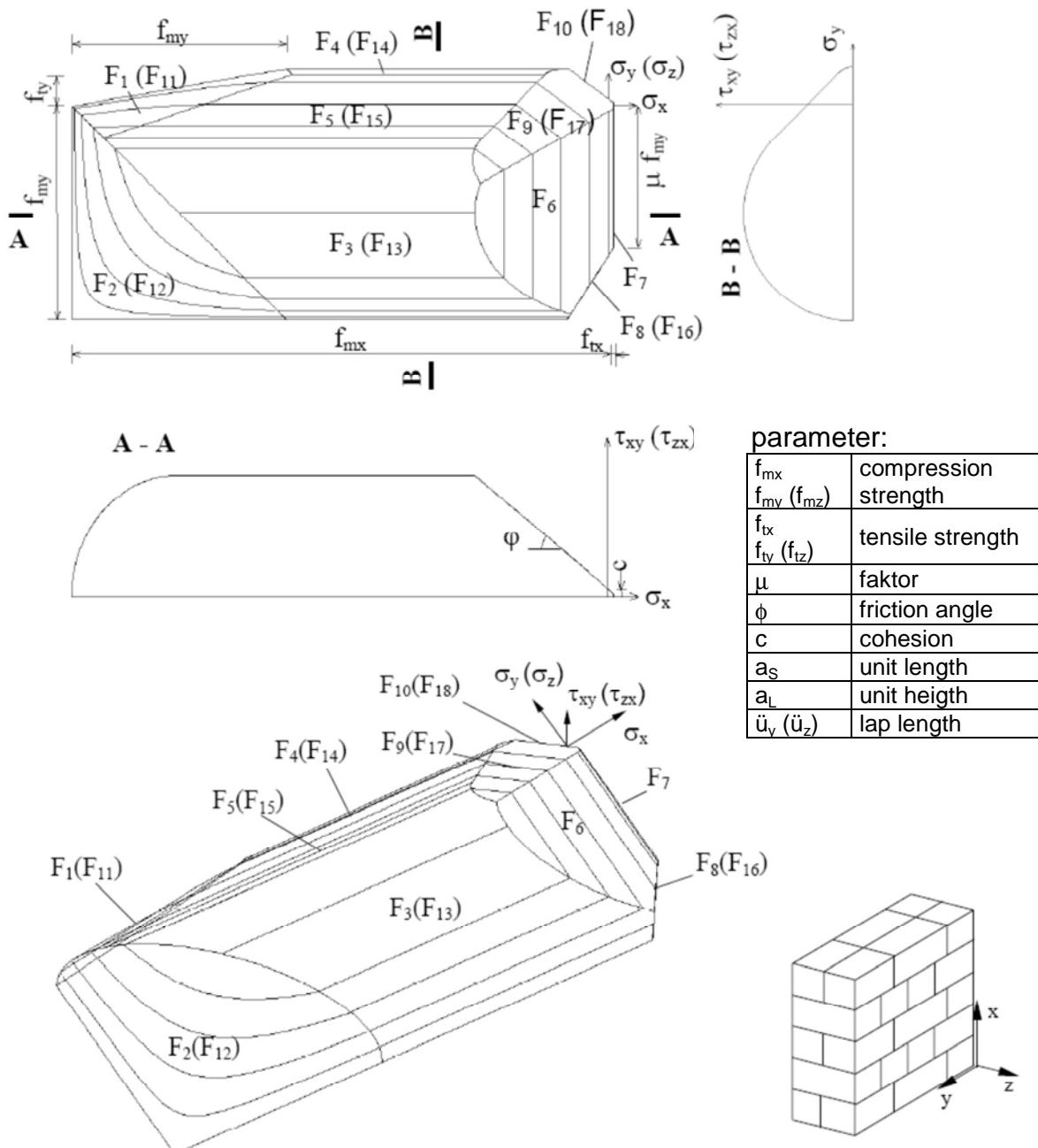


Fig. 3-17 Ganz material model for masonry [6-17]

|           |   |
|-----------|---|
| F1 (F11)  | Tension failure brick   |
| F2 (F12)  | Compressive failure masonry                                       |
| F3 (F13)  | Shear failure masonry (brick failure)                             |
| F4 (F14)  | Tension failure parallel to bed joint (brick failure)             |
| F5 (F15)  | Shear failure masonry   |
| F6        | Shear failure bed joint   |
| F7        | Tension failure bed joint   |
| F8 (F16)  | Tension failure bed joint under high horizontal pressure          |
| F9 (F17)  | Staircase-shaped shear failure                                    |
| F10 (F18) | Tension failure of masonry parallel to bed joints (joint failure) |

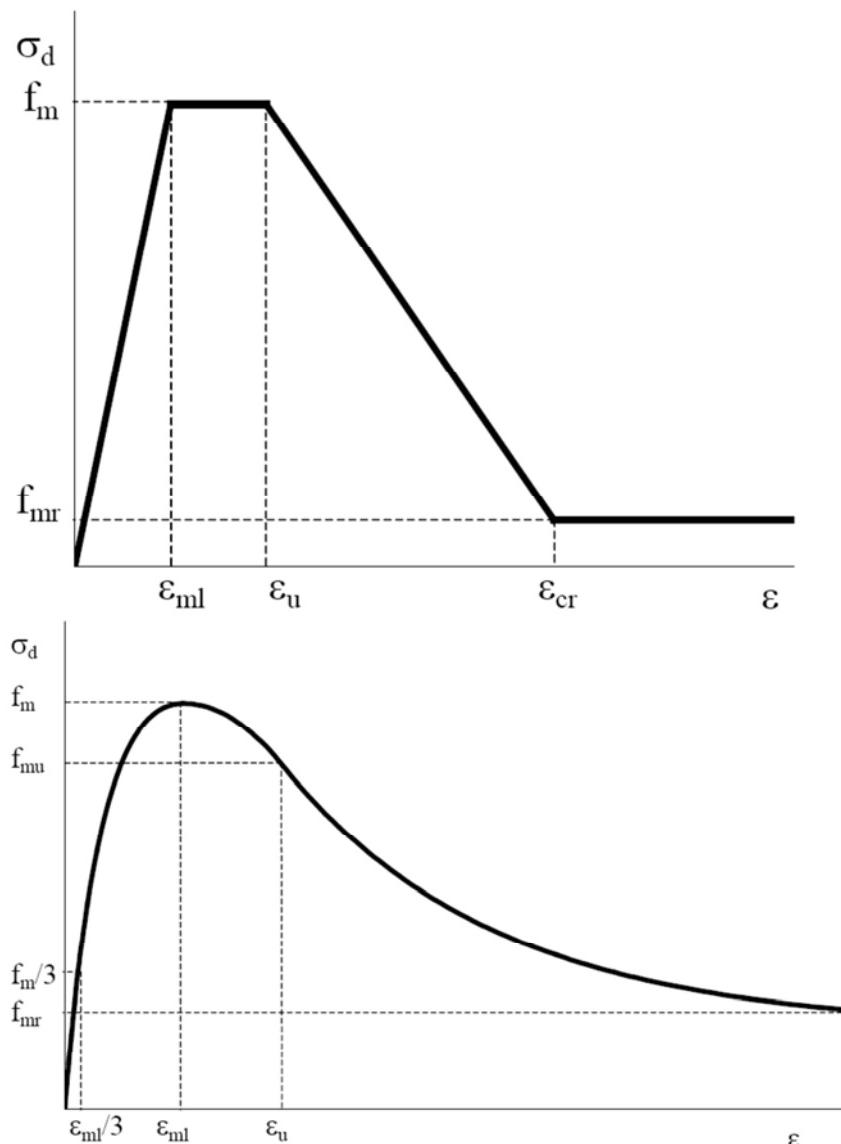
**Tab. 3-2 Material model for masonry – meaning of the flow criteria**

The orthotropic nonlinear stress-strain behaviour of masonry is described using the corresponding softening and hardening models [6-17].

### 3.3.7.1 Nonlinear stress-strain relation under pressure load

For simulation of a nonlinear stress-strain relation under pressure load two models are available (s. Fig. 3-18). The stress-strain relation complies with the DIN 1045-1 [Law 22] model for concrete shown in chapter 3.3.6.1 which also applies for vertical pressure load.

The model [Law 20] within Fig. 3-18 is often sufficiently accurate for practical applications.



**Fig. 3-18 models of the stress-strain relation in case of pressure load, above: LAW 20, below: LAW 22**

### 3.3.7.2 Nonlinear stress-strain relation under tensile load perpendicular to the bed joints

For the behaviour under tensile stress perpendicular to the bed joints a stress-strain relation with exponential softening is available. The stress-strain relation is shown in Fig. 3-19. The conclusions, that are done in 3.3.6.2 are valid here as well.

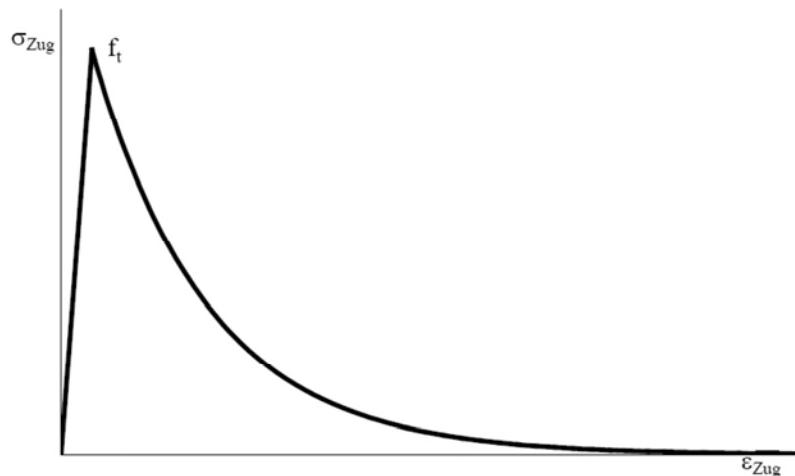


Fig. 3-19 stress-strain relation under tensile load perpendicular to the bed joints

### 3.3.7.3 Nonlinear stress-strain relation in case of shear load of bed joint

The shear failure of the bed joints, which could be observed in the test case, can be described by an exponential degradation of the cohesion  $C$  and linear reduction of the friction angle  $\phi_0$  to a residual friction angle  $\phi_r$ . The corresponding, assumed stress-strain line is shown in Fig. 3-20. The softening model for the cohesion  $C$  was chosen analogical to the approach described in chapter 3.3.6.2. Hereby it is assumed that for completely diminishing of the cohesion, a fracture energy  $G_{II,f,j}$  (mode II – adhesion-shear-strength) has to be dissipated. This has been experimentally established by van der Pluijm [6-27]. The tension and shear softening are synchronized.

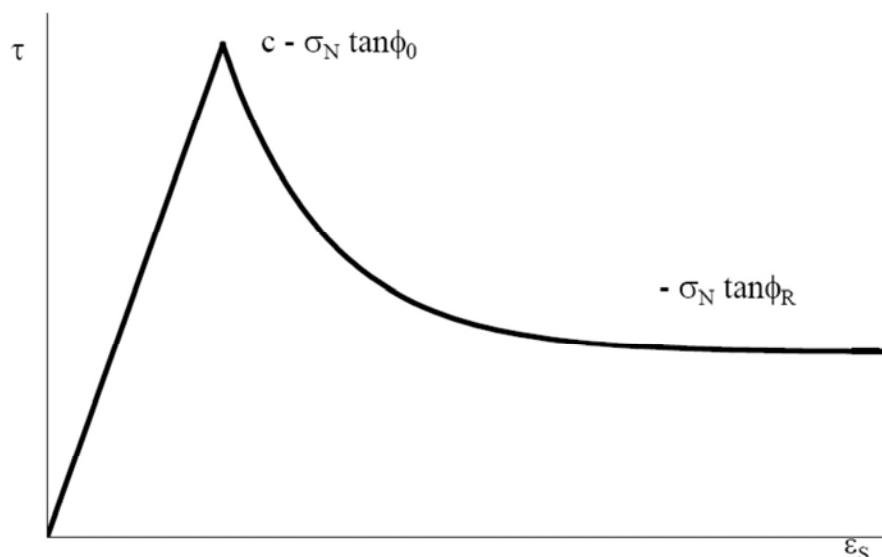


Fig. 3-20 Nonlinear stress-strain relation in case of shear of bed joint

### 3.3.8 Wood modelling using a boxed-value-model

The multi surface material model for wood is based on a boxed-value model from Grosse [6-26]. The orthotropic material model is implemented in multiPlas via LAW 33. It considers the interactions between the longitudinal, radial and tangential material behaviour of wood. The yield conditions are shown in Fig. 3-21 and Fig. 3-22. The stress and strain functions, implemented for describing the nonlinear deformation behaviour, are shown in chapter 3.3.8.1.

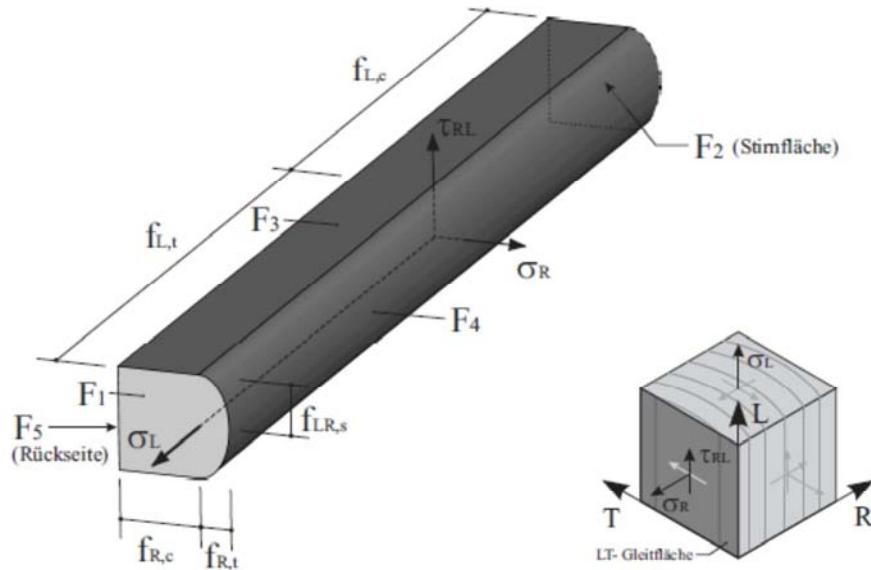


Fig. 3-21 yield condition – Interaction longitudinal vs. radial

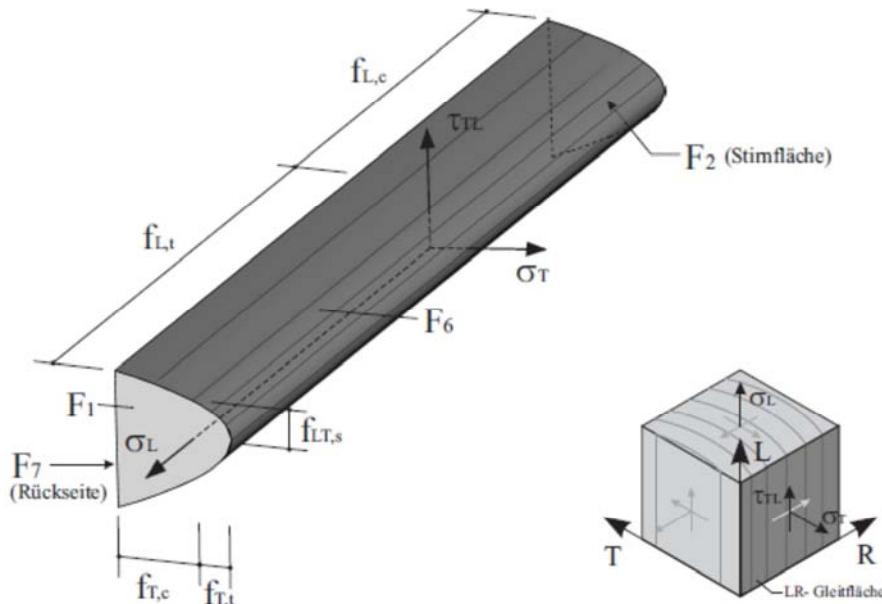


Fig. 3-22 yield condition – Interaction longitudinal vs. tangential

In multiPlas, the following conventions for the direction of wood fibre have been made:

|              |   |                                       |
|--------------|---|---------------------------------------|
| Radial       | = | X- Axis of element coordinate systems |
| Tangential   | = | Y- Axis of element coordinate systems |
| Longitudinal | = | Z- Axis of element coordinate systems |

This conventions hold for Cartesian and Cylindrical coordinate systems.

Following yield conditions are used:

Fiber rupture (tensile failure longitudinal)

$$F_1 = \sigma(3) - f_{Lt} \cdot \Omega_{Lt} = 0 \quad (3-25)$$

Fiber compressions (compression failure longitudinal)

$$F_2 = -\sigma(3) - f_{Lc} \cdot \Omega_{Lc} = 0 \quad (3-26)$$

Crack parallel to LT-Plane

$$F_3 = \left( \frac{\sigma(6)}{f_{RLs} \cdot \Omega_{RLs}} \right)^2 + \left( \frac{\sigma(4)}{f_{RTs} \cdot \Omega_{RTs}} \right)^2 - 1 = 0 \quad (3-27)$$

$$F_4 = \left( \frac{\sigma(1)}{f_{Rt} \cdot \Omega_{Rt}} \right)^2 + \left( \frac{\sigma(4)}{f_{RTs} \cdot \Omega_{RTs}} \right)^2 + \left( \frac{\sigma(6)}{f_{RLs} \cdot \Omega_{RLs}} \right)^2 - 1 = 0 \quad (3-28)$$

Radial Compression of fiber (compression failure radial)

$$F_5 = -\sigma(1) - f_{Rc} \cdot \Omega_{Rc} = 0 \quad (3-29)$$

Crack parallel to LR-Plane

$$F_6 = \left( \frac{\sigma(2)}{f_{Tt} \cdot \Omega_{Tt}} \right)^2 + \left( \frac{\sigma(4)}{f_{TRs} \cdot \Omega_{TRs}} \right)^2 + \left( \frac{\sigma(5)}{f_{TLs} \cdot \Omega_{TLs}} \right)^2 - 1 = 0 \quad (3-30)$$

Tangential Compression of fiber

$$F_7 = -\sigma(2) - f_{Tc} \cdot \Omega_{Tc} = 0 \quad (3-31)$$

### 3.3.8.1 Nonlinear deformation behaviour

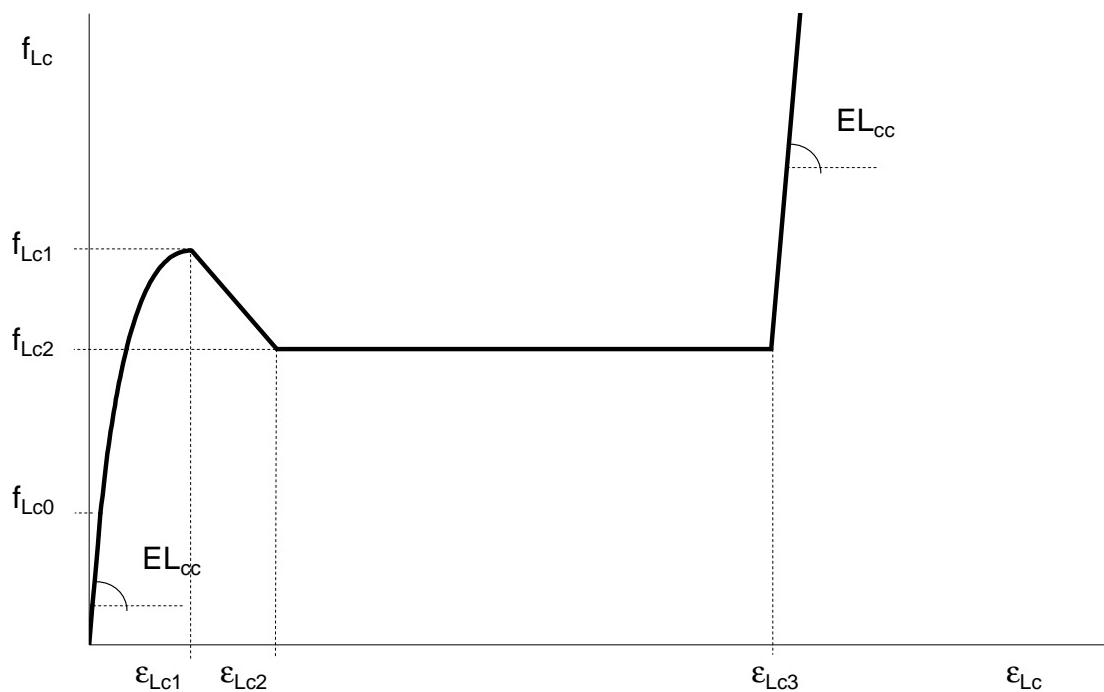
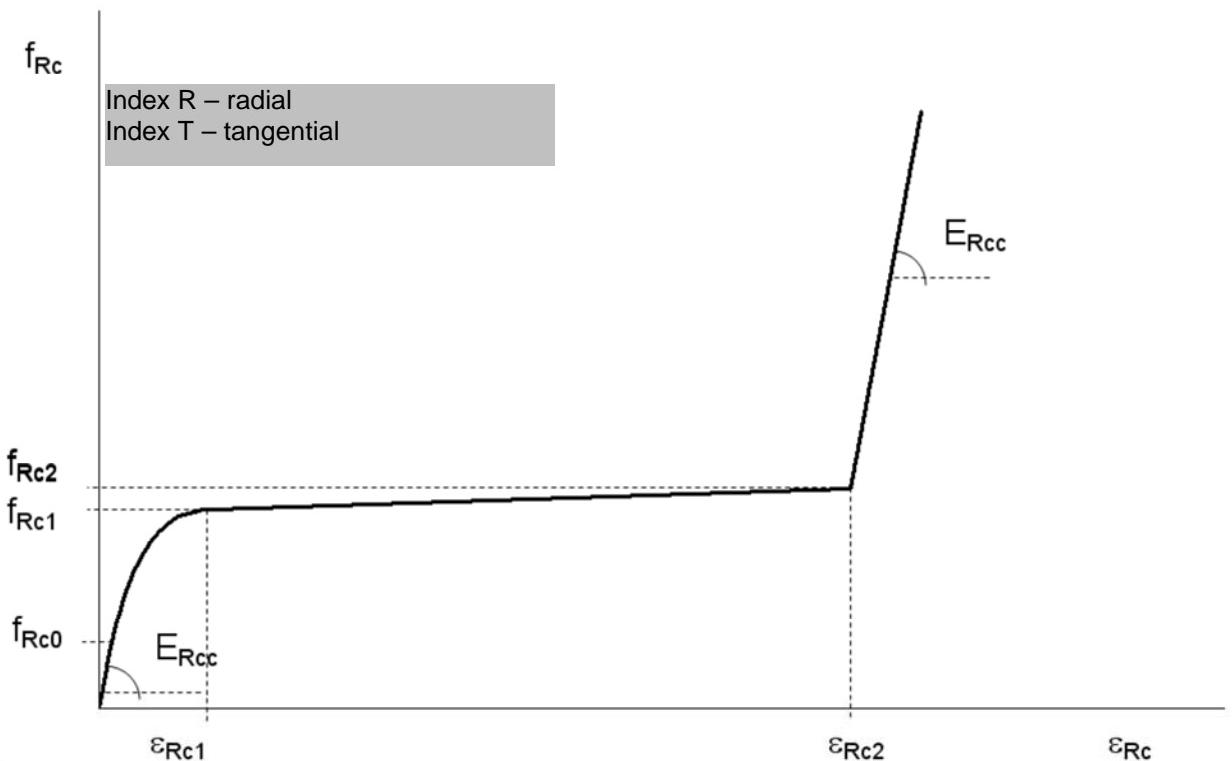
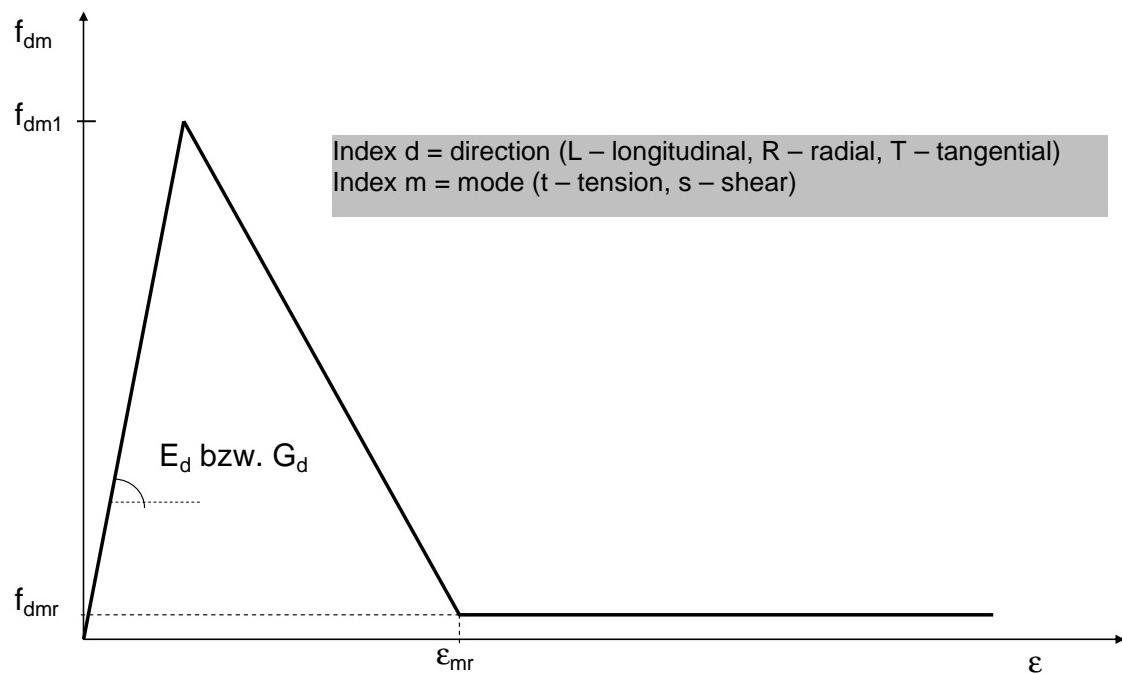


Fig. 3-23 Stress-strain relation - compression in fiber direction (longitudinal)



**Fig. 3-24 Stress-strain relation - compression perpendicular to fiber direction (radial or tangential)**



**Fig. 3-25 Stress-strain relation for shear and tension**

### 3.4 Dilatancy

The strict adherence of the stability postulations of Drucker usually requires an associated yield constitutive law (e.g. dilatancy angle = friction angle). But in reality, for some materials, the calculated volume strains are significantly larger than those, determined by experiments. In that cases, a deformation behaviour closer to reality can be described by using non-associated flow rules. The dilatancy angle describes the ratio of normal and shear translation in the Mohr-Coulomb shear criterion. It has two limits:

Dilatancy angle = friction angle => maximum plastic normal strain at shear strain, associated plasticity  
Dilatancy angle = 0.0 => no plastic normal strain at shear (not recommended limit case because of resulting numerical problems)

By replacing the friction angle  $\varphi$  by the dilatancy angle  $\psi$  within the yield condition (rsp. plastic potential function), a non-associated flow rule is obtained. In addition to that it has to be considered, that the dilatancy angle is only physically reasonable for

dilatancy angle  $\psi \leq$  friction angle  $\varphi$ .

A dilatancy angle larger than the friction angle leads to generation of energy within the system.

For the Drucker-Prager yield condition, the plastic deformation behaviour can be controlled via a non-associated flow rule by manipulating the dilatancy factor  $\delta$ . Then the plastic potential is modified according to the equations ( $Q = \sigma_s + \beta \delta \sigma_m$  (3-18) and (3-21)).

Thereby:

dilatancy factor  $\delta = 1 \Rightarrow$  associated plasticity

dilatancy factor  $\delta \leq 1 \Rightarrow$  non-associated plasticity

For the compressive domain  $0 \leq \delta_c \leq 1$  is true. In the tensile domain of the Drucker-Prager, a yield condition of  $\delta_t = 0,1 \dots 0,25$  is recommended.

In case of prevalent shear strain, the dilatancy factor  $\delta$  can be calculated via the ratio of the beta values from

Fig. 3-8 with the help of the friction angle  $\varphi$  and the dilatancy angle  $\psi$ . From equation (4.1), this could be calculated by:

$$\beta(\varphi) = \frac{6 \cdot \sin \varphi}{\sqrt{3}(3 + \sin \varphi)} \quad \beta(\psi) = \frac{6 \cdot \sin \psi}{\sqrt{3}(3 + \sin \psi)} \quad \delta = \frac{\beta(\varphi)}{\beta(\psi)} \quad (3-32)$$

Please note that a non-associated flow rule however lead to asymmetric deformation matrices and may result in pure convergence behaviour.

## 4 COMMANDS

### 4.1 Material Models

| LAW | Material Model   |
|-----|--|
| 1   | Mohr-Coulomb / Tresca (isotropic), tension cut off (isotropic)<br>Mohr-Coulomb (anisotropic), tension cut off (anisotropic) for up to 4 joint sets |
| 2   | Drucker-Prager / modified Drucker-Prager (ideal elastic-plastic)   |
| 5   | Drucker-Prager / modified Drucker-Prager, temperature dependent  |
| 8   | Mortar / Cement (modified Drucker-Prager, stress dependent, nonlinear hardening / softening)   |
| 9   | Concrete (nonlinear hardening / softening, Temperature Dependency)   |
| 10  | Mohr-Coulomb (anisotropic), tension cut off (anisotropic) for up to 4 joints   |
| 11  | fixed crack model (x-direction)  |
| 20  | Masonry_Ganz (linear hardening /softening, Temperature Dependency)   |
| 22  | Masonry_Ganz (nonlinear hardening / softening)   |
| 33  | boxed value (orthotropic)  |
| 40  | Drucker-Prager-Geo   |
| 41  | Coupling Mohr-Coulomb and Drucker-Prager   |
| 99  | usermpls   |

The material library multiPlas was implemented within the ANSYS-user-interface “userpl”. The activation is realized by using the tb-commands:

tb,user,mat,,80  
tbda,1,LAW, , ,

*mat* – material number  
allocation of the data field with the selected material model (LAW) and the material parameters (see the following sections 4.2)

## 4.2 TBDATA-Declaration

### 4.2.1 LAW = 1, 10 – Mohr Coulomb

|                   | 1    | 2     | 3            | 4    | 5            | 6       | 7            | 8      | 9            | 10                   |
|-------------------|------|-------|--------------|------|--------------|---------|--------------|--------|--------------|----------------------|
| 0-10<br>isotrop   | LAW  | phig  | Cg           | psig | phig*        | Cg*     | Tension      |        | Tension*     | number of joint sets |
| 11-20<br>1. joint | Phi  | C     | psi          | phi* | C*           | Tension | alpha        | beta   | Tension*     |                      |
| 21-30<br>2. joint | Phi  | C     | psi          | phi* | C*           | Tension | alpha        | beta   | Tension*     |                      |
| 31-40<br>3. joint | Phi  | C     | psi          | phi* | C*           | Tension | alpha        | beta   | Tension*     |                      |
| 41-50<br>4. joint | Phi  | C     | psi          | phi* | C*           | Tension | alpha        | beta   | Tension*     | tempd                |
| 51-60             | T1   | T2    | $\beta_{c2}$ | T3   | $\beta_{c3}$ | T4      | $\beta_{c4}$ | T5     | $\beta_{c5}$ | wr                   |
| 61-70             | Elem | Intpt | eps          | geps | maxit        | cutmax  | dtmin        | maxinc |              | ktuser               |
| 71-80             |      |       |              |      |              |         |              |        |              |                      |

#### Base material parameter Isotropic Mohr-Coulomb

|          |  |
|----------|--|
| phig     | friction angle   |
| Cg       | cohesion   |
| psig     | dilatancy angle  |
| phig*    | residual friction angle  |
| Cg*      | residual cohesion  |
| Tension  | tensile strength -Tension cut off- ( $\leq Cg/\tan(\text{phig})$ ) |
| Tension* | residual tensile strength ( $\leq Cg^*/\tan(\text{phig}^*)$ )      |

#### Temperature dependency rsp. moisture dependency<sup>1</sup>

The temperature-dependent strength is realised over the temperature dependence of the cohesion switch for temperature dependency

tempd  
=0: no temperature dependency

=1: temperature dependence of the cohesion

|              |  |
|--------------|--|
| T1           | reference temperature with 100% strength, see Cg (field 3) |
| T2-5         | temperatures at °C (in ascending order)                    |
| $\beta_{ci}$ | relative cohesion $Cg(T_i)/Cg$                             |

#### Anisotropic Mohr-Coulomb (up to 4 joint sets)

|          |  |
|----------|--|
| phi      | joint friction angle   |
| C        | joint cohesion   |
| psi      | joint dilatancy angle  |
| phi*     | joint residual friction angle                                      |
| C*       | joint residual cohesion  |
| Tension  | joint tensile strength - Tension cut off- ( $\leq Cg/\tan(\phi)$ ) |
| Tension* | joint residual tensile strength ( $\leq Cg^*/\tan(\phi^*)$ )       |

#### direction of anisotropic joint system

The transformation into the element coordinate system is defined by two angles (alpha, beta) see Fig. 3-4 and Fig. 3-6.

|       |                                |
|-------|--------------------------------|
| alpha | negative rotation about Z-axis |
| beta  | positive rotation about Y-axis |

<sup>1</sup> Volume-referred moisture as temperature equivalent interpreted

## 4.2.2 LAW = 2 – Modified Drucker-Prager

|                   | 1    | 2     | 3   | 4    | 5     | 6       | 7     | 8      | 9        | 10                   |
|-------------------|------|-------|-----|------|-------|---------|-------|--------|----------|----------------------|
| 0-10<br>isotrop   | LAW  | Rd    | Rz  | Ru   |       |         |       |        |          | number of joint sets |
| 11-20<br>1. joint | Phi  | C     | psi | phi* | C*    | Tension | alpha | beta   | Tension* |                      |
| 21-30<br>2. joint | Phi  | C     | psi | phi* | C*    | Tension | alpha | beta   | Tension* |                      |
| 31-40<br>3. joint | Phi  | C     | psi | phi* | C*    | Tension | alpha | beta   | Tension* |                      |
| 41-50<br>4. joint | Phi  | C     | psi | phi* | C*    | Tension | alpha | beta   | Tension* |                      |
| 51-60             |      |       |     |      |       |         |       |        |          | wr                   |
| 61-70             | Elem | Intpt | eps | geps | maxit | cutmax  | dtmin | maxinc |          | ktuser               |
| 71-80             |      |       |     |      |       |         |       |        |          |                      |

### Base material parameter:

Rd uniaxial compression strength  
 Rz uniaxial tensile strength  
 Ru biaxial compression strength

(Remark: ideal elastic-plastic behaviour with associated flow rule)

### Combination with joints / anisotropic Mohr-Coulomb (up to 4 joint sets)

phi joint friction angle  
 C joint cohesion  
 psi joint dilatancy angle  
 phi\* joint residual friction angle  
 C\* joint residual cohesion  
 Tension joint tensile strength -Tension cut off- ( $\leq C_g/\tan(\phi)$ )  
 Tension\* joint residual tensile strength ( $\leq C_g^*/\tan(\phi^*)$ )

### direction of anisotropic joint system

The transformation into the element coordinate system is defined by two angles (alpha, beta) see Fig. 3-4 and Fig. 3-6.

alpha negative rotation about Z-axis  
 beta positive rotation about Y-axis

### 4.2.3 LAW = 5 – Modified Drucker-Prager, temperature dependent

|                 | 1            | 2            | 3            | 4            | 5            | 6            | 7               | 8               | 9             | 10            |
|-----------------|--------------|--------------|--------------|--------------|--------------|--------------|-----------------|-----------------|---------------|---------------|
| 0-10<br>isotrop | LAW          | Rd           | Rz           | Ru           |              |              |                 |                 |               |               |
| 11-20           |              |              |              |              |              | T1           |                 |                 |               |               |
| 21-30           | T2           | T3           | T4           | T5           | T6           | T7           | T8              | T9              | T10           | T11           |
| 31-40           | $\beta_{c2}$ | $\beta_{c3}$ | $\beta_{c4}$ | $\beta_{c5}$ | $\beta_{c6}$ | $\beta_{c7}$ | $\beta_{c8}$    | $\beta_{c9}$    | $\beta_{c10}$ | $\beta_{c11}$ |
| 41-50           |              |              |              |              |              |              |                 |                 |               |               |
| 51-60           |              |              |              | utz          |              |              | T <sub>ts</sub> | T <sub>tE</sub> | $\beta_{tE}$  | wr            |
| 61-70           | Elem         | Intpt        | eps          | geps         | maxit        | cutmax       | dtmin           | maxinc          |               | ktuser        |
| 71-80           |              |              |              |              |              |              |                 |                 |               |               |

**Base material parameter:**

**for reference temperatur T1 (e.g. room-temperatur):**

Rd uniaxial compression strength

Rz uniaxial tensile strength

Ru biaxial compression strength

(Remark: ideal elastic-plastic behaviour with associated flow rule)

**Temperature dependency**

utz switch for temperature dependency of tensile strength (=0 – off; =1 – on)

T<sub>ts</sub> temperature, at which a linear, temperature-dependent reduction of the tensile strength begins (see Fig. 3-16)

T<sub>tE</sub> temperature, up to which the linear, temperature-dependent reduction of the tensile strength takes place (see Fig. 3-16)

$\beta_{tE}$  residual plateau for tensile strength Rz(T<sub>tE</sub>)/Rz

T2-11 temperatures in °C (please enter in ascending order !!!)

$\beta_{ci}$  temperature-dependent, normalized compressive strength Rd(T<sub>i</sub>)/Rd

#### 4.2.4 LAW = 8 – Modified Drucker-Prager, calibrated stress dependent nonlinear hardening (Mortar / Cement)

|       | 1                  | 2          | 3                   | 4                  | 5                 | 6                 | 7                  | 8                   | 9                  | 10                  |
|-------|--------------------|------------|---------------------|--------------------|-------------------|-------------------|--------------------|---------------------|--------------------|---------------------|
| 0-10  | LAW                | Rd         | Rz                  | Ru                 | $\delta_{\psi t}$ | $\delta_{\psi c}$ | $\delta_{\psi c2}$ | $\varepsilon_{ml1}$ | $\varepsilon_{u1}$ | $O_{i1}$            |
| 11-20 | $O_{u1}$           | $O_{r1}$   | $\varepsilon_{ml2}$ | $\varepsilon_{u2}$ | $O_{i2}$          | $O_{u2}$          | $O_{r2}$           | fst2                | $\varepsilon_{i3}$ | $\varepsilon_{ml3}$ |
| 21-30 | $\varepsilon_{u3}$ | $O_{o3}$   | $O_{i3}$            | $O_{u3}$           | $O_{r3}$          | fst3              | $\varepsilon_{i4}$ | $\varepsilon_{ml4}$ | $\varepsilon_{u4}$ | $O_{o4}$            |
| 31-40 | $O_{i4}$           | $O_{u4}$   | $O_{r4}$            | fst4               | Ev                |                   |                    |                     |                    |                     |
| 41-50 |                    |            |                     |                    |                   |                   |                    |                     |                    |                     |
| 51-60 | $G_f$              | $G_{fJ}^I$ | $G_{fJ}^{II}$       |                    |                   |                   |                    |                     |                    | wr                  |
| 61-70 | Elem               | Intpt      | eps                 | geps               | maxit             | cutmax            | dtmin              | maxinc              |                    | ktuser              |
| 71-80 |                    |            |                     |                    |                   |                   |                    |                     |                    |                     |

##### Base material parameter:

- Rd uniaxial compression strength  
 Rz uniaxial tensile strength  
 Ru biaxial compression strength  
 $\delta_{\psi t}$  dilatancy factor in tensile stress domain  $0 \leq \delta_{\psi} \geq 1$   
 $\delta_{\psi c}$  dilatancy factor in compression stress domain  $0 \leq \delta_{\psi} \geq 1$  (recommendation  $\delta_{\psi} = 1,00$ )  
 Ev elastic modulus  
 $G_f$  fracture energy (Mode 1 - tensile failure)

##### Nonlinear deformation behaviour under multiaxial compression ( $\sigma_m < 0$ )

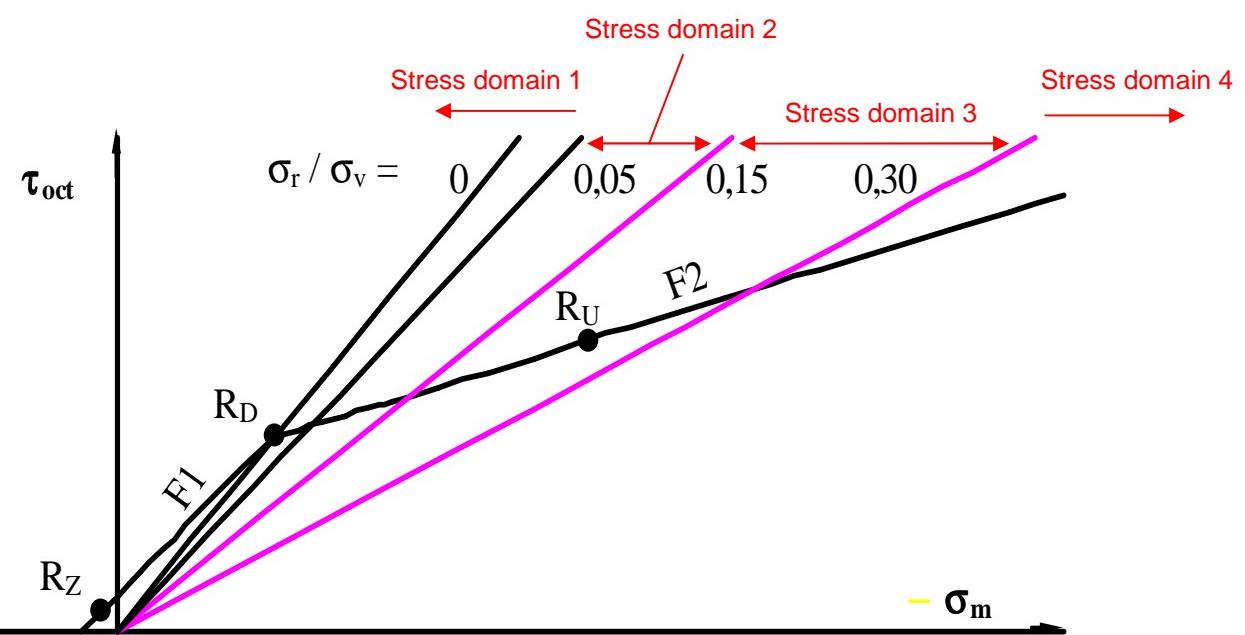


Fig. 4-1 Compression stress domains

##### Parameter for stress-strain-relations

###### Stress domain 1: ( $\sigma_r/\sigma_v < 0,05$ ) – uniaxial compression test

- $\varepsilon_{ml1}$  strain at compression strength Rd  
 $\Omega_i$  start of nonlinear hardening  
 $\Omega_{u1}$  compression stress level (see Fig. 4-2)  
 $\varepsilon_{u1}$  strain at softening up to  $\Omega_{u1}$   
 $\Omega_{r1}$  residual stress plateau (see Fig. 4-2)

**Stress domain 2: ( $0,05 \geq \sigma_r/\sigma_v < 0,15$ )**

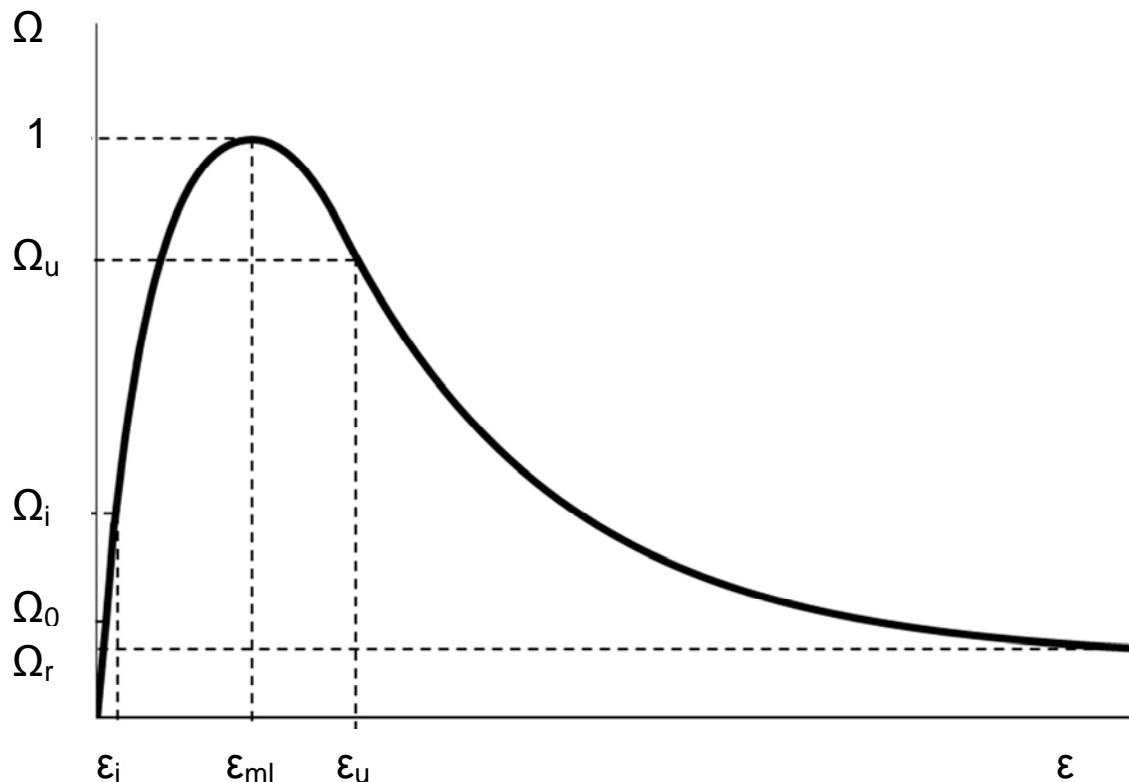
|                     |   |
|---------------------|---|
| $\Omega_{i2}$       | start of nonlinear hardening            |
| $\varepsilon_{ml2}$ | strain at compression strength          |
| $\Omega_{u2}$       | compression stress level (see Fig. 4-2) |
| $\varepsilon_{u2}$  | strain at softening up to $\Omega_{u2}$ |
| $\Omega_{r2}$       | residual stress plateau (see Fig. 4-2)  |
| fst2                | factor increase in compressive strength |

**Stress domain 3: ( $0,15 \geq \sigma_r/\sigma_v < 0,30$ )**

|                     |   |
|---------------------|---|
| $\Omega_{03}$       | start of nonlinear hardening                                      |
| $\Omega_{i3}$       | compression stress level (see Fig. 4-2)                           |
| $\varepsilon_{i3}$  | strain at stress level $\Omega_{i3}$                              |
| $\varepsilon_{ml3}$ | strain at compression strength                                    |
| $\Omega_{u3}$       | compression stress level (see Fig. 4-2)                           |
| $\varepsilon_{u3}$  | strain at stress level $\Omega_{u3}$                              |
| $\Omega_{r3}$       | residual stress plateau (see Fig. 4-2)                            |
| fst3                | factor increase in compressive strength (at $\varepsilon_{ml3}$ ) |

**Stress domain 4: ( $0,30 \geq \sigma_r/\sigma_v$ )**

|                     |   |
|---------------------|---|
| $\Omega_{04}$       | start of nonlinear hardening                                      |
| $\Omega_{i4}$       | compression stress level (see Fig. 4-2)                           |
| $\varepsilon_{i4}$  | strain at stress level $\Omega_{i4}$                              |
| $\varepsilon_{ml4}$ | strain at compression strength                                    |
| $\Omega_{u4}$       | compression stress level (see Fig. 4-2)                           |
| $\varepsilon_{u4}$  | strain at stress level $\Omega_{u4}$                              |
| $\Omega_{r4}$       | residual stress plateau (see Fig. 4-2)                            |
| fst4                | factor increase in compressive strength (at $\varepsilon_{ml4}$ ) |

**Fig. 4-2 Input parameter in compression stress domain**

## 4.2.5 LAW = 9 – Concrete

|       | 1             | 2             | 3             | 4             | 5                 | 6                 | 7             | 8             | 9              | 10             |
|-------|---------------|---------------|---------------|---------------|-------------------|-------------------|---------------|---------------|----------------|----------------|
| 0-10  | LAW           | Rd            | Rz            | Ru            | $\delta_{\psi t}$ | $\delta_{\psi c}$ |               |               |                |                |
| 11-20 | $\kappa_{m1}$ | $\kappa_u$    | $\Omega_i$    | $\Omega_u$    | $\Omega_r$        | T1                |               |               |                |                |
| 21-30 | T2            | T3            | T4            | T5            | T6                | T7                | T8            | T9            | T10            | T11            |
| 31-40 | $\beta_{c2}$  | $\beta_{c3}$  | $\beta_{c4}$  | $\beta_{c5}$  | $\beta_{c6}$      | $\beta_{c7}$      | $\beta_{c8}$  | $\beta_{c9}$  | $\beta_{c10}$  | $\beta_{c11}$  |
| 41-50 | $\kappa_{m2}$ | $\kappa_{m3}$ | $\kappa_{m4}$ | $\kappa_{m5}$ | $\kappa_{m6}$     | $\kappa_{m7}$     | $\kappa_{m8}$ | $\kappa_{m9}$ | $\kappa_{m10}$ | $\kappa_{m11}$ |
| 51-60 | $G_f$         | $\Omega_{tr}$ | $\kappa_{tr}$ | utz           |                   | mlaw              | $T_{ts}$      | $T_{te}$      | $\beta_{te}$   | wr             |
| 61-70 | Elem          | Intpt         | eps           | geps          | maxit             | cutmax            | dtmin         | maxinc        | EInt           | ktuser         |
| 71-80 |               |               |               |               |                   |                   |               |               |                |                |

### Base material parameter:

for reference temperatur T1 (e.g. room-temperatur):

Rd uniaxial compression strength

Rz uniaxial tensile strength (recommendation Rz = 0,1 Rd for normal concrete)

Ru biaxial compression strength (recommendation Ru = 1,2 Rd for normal concrete)

$\delta_{\psi t}$  dilatancy factor in tensile stress domain  $0 \leq \delta_{\psi} \geq 1$  (recommendation  $\delta_{\psi t} = 0,25$ )

$\delta_{\psi c}$  dilatancy factor in compression stress domain  $0 \leq \delta_{\psi} \geq 1$  (recommendation  $\delta_{\psi c} = 1,00$ )

### Hardening- / softening function

mlaw switch for softening function

= 0 – linear softening up to a predefined limit strain  $\kappa_{cr}$  after DIN EN 1992-1-2

= 1 – exponential softening with fracture energy

= 2 – like 0, but with mixed softening model (hydrostatic and deviatoric part)

### Hardening and softening function (stress-strain-function) in compression stress domain

$\kappa_{m1}$  plastic strain at compression strength Rd ( $\kappa_{m1} = \varepsilon_{ml} - Rd/E$ )

$\Omega_i$  start of nonlinear hardening (recommendation  $\Omega_i = 0,33$ )

$\Omega_r$  residual stress plateau (recommendation  $\Omega_r = 0,2$ )

mlaw = 1:

$\kappa_u$  plastic strain at softening up to  $\Omega_u$  ( $\kappa_u = \varepsilon_u - \Omega_u * Rd/E$ )

$\Omega_u$  stress level see Fig. 4-3

### Softening function (stress-strain-function) in tensile stress domain

mlaw = 0 bzw. 2:

$\Omega_{tr}$  residual plateau

$\kappa_{tr}$  plastic limit strain

mlaw = 1:

$G_f$  fracture energy (Mode 1 - tensile failure)

### Temperature dependency

Temperature dependency is available for mlaw = 0/2

utz switch for temperature dependency of tensile strength (=0 – off; =1 – on)

$T_{ts}$  temperature, at which a linear, temperature-dependent reduction of the tensile strength begins (see Fig. 3-16)

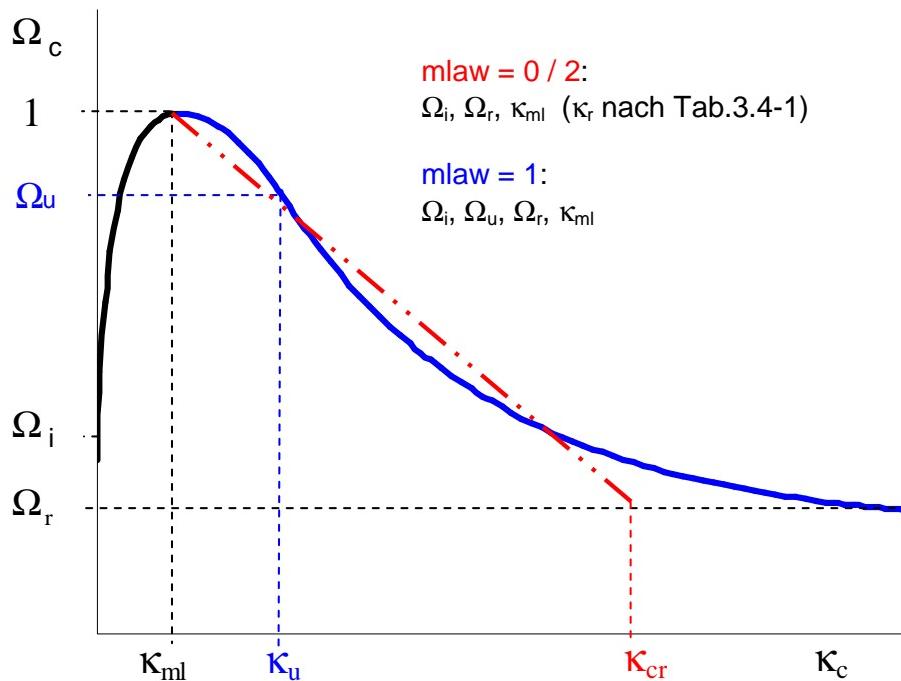
$T_{te}$  temperature, up to which the linear, temperature-dependent reduction of the tensile strength takes place (see Fig. 3-16)

$\beta_{te}$  residual plateau for tensile strength  $Rz(T_{te})/Rz$

T2-11 temperatures in °C (please enter in ascending order !!!)

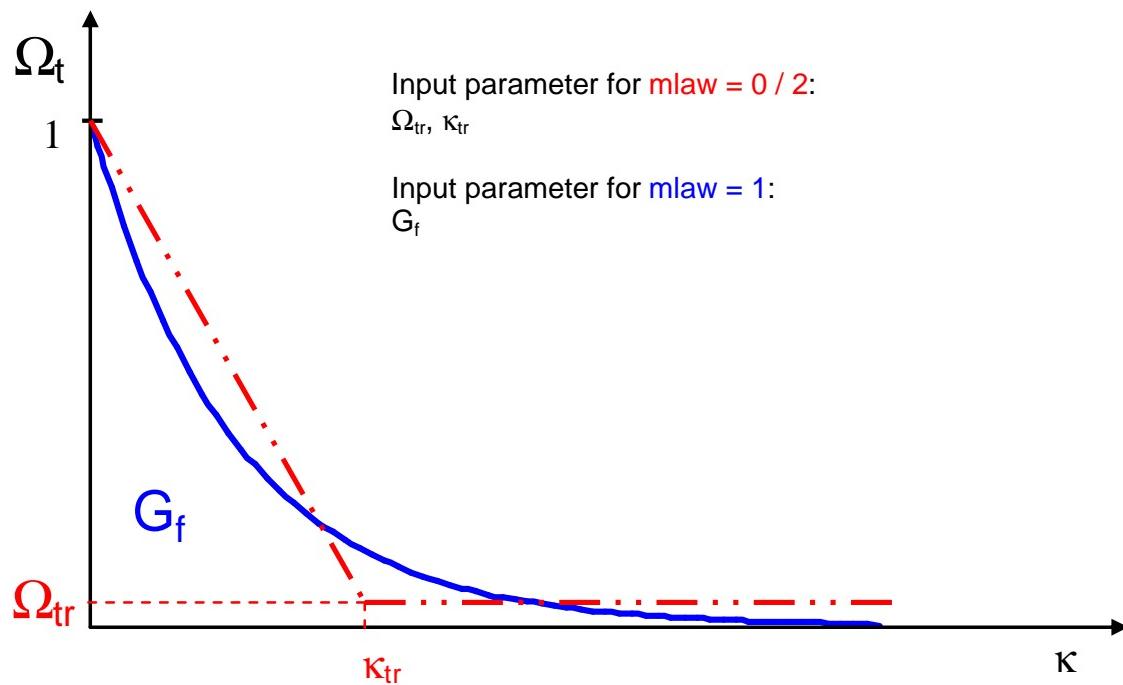
$\beta_{ci}$  temperature-dependent, normalized compressive strength  $Rd(T_i)/Rd$

$\kappa_{mi}$  plastic strain with reaching the compressive strength (for  $T_i$ )



**Fig. 4-3 Input parameter in compression stress domain**

Overview input parameter of softening function in tensile stress domain



**Fig. 4-4 Input parameter in tensile stress domain**

**Remark:** switch to LAW = 5 (with same input like LAW=9) – for temperature dependency without mechanical softening

#### 4.2.6 LAW = 11 – Fixed Crack Model

|       | 1       | 2     | 3   | 4    | 5     | 6      | 7     | 8      | 9    | 10           |
|-------|---------|-------|-----|------|-------|--------|-------|--------|------|--------------|
| 0-10  | LAW     | ftx   |     |      |       |        |       |        |      |              |
| 11-20 |         |       |     |      |       |        |       |        |      |              |
| 21-30 |         |       |     |      |       |        |       |        |      |              |
| 31-40 |         |       |     |      |       |        |       |        |      |              |
| 41-50 |         |       |     |      |       |        |       |        |      |              |
| 51-60 | $G_F^I$ |       |     |      |       |        | ftr   |        |      | wr<br>(Ausg) |
| 61-70 | Elem    | Intpt | eps | geps | maxit | cutmax | dtmin | maxinc | EInt | ktuser       |
| 71-80 |         |       |     |      |       |        |       |        |      |              |

##### Material parameter

- ftx                    tensile strength in x-direction  
 $G_F^I$                 fracture energy (Mode 1 - tensile failure)  
 ftr                    residual tensile strength (for numerical stabilization)

##### Notes:

fixed and smeared crack model in x-direction with exponential softening

used equivalent length:

$$\text{for volume elements: } h = \sqrt[3]{\frac{V_{El}}{n_{INT}}} \quad \text{for shell / plane elements: } h = \sqrt{\frac{A_{El}}{n_{INT}}}$$

with

$n_{INT}$  – number of integration points,  $V_{El}$  – element volume,  $A_{El}$  – element area

#### 4.2.7 LAW = 20 – Masonry Linear Softening

|       | 1                            | 2                            | 3                             | 4                | 5     | 6      | 7                | 8                | 9     | 10               |
|-------|------------------------------|------------------------------|-------------------------------|------------------|-------|--------|------------------|------------------|-------|------------------|
| 0-10  | LAW                          | fmx                          | fmy                           | ftx              | ftxx  | fty    | nue_y            | ka_u             | eta_r | as_y             |
| 11-20 | al                           | ü_y                          | phi                           | c                | phir  | psi    | direc            | dreid            | fmz   | ftz              |
| 21-30 | ftzz                         | nue_z                        | as_z                          | ü_z              | tempd | T1     | T2               | β <sub>fm2</sub> | ka_u2 | T3               |
| 31-40 | β <sub>fm3</sub>             | ka_u3                        | T4                            | β <sub>fm4</sub> | ka_u4 | T5     | β <sub>fm5</sub> | ka_u5            | T6    | β <sub>fm6</sub> |
| 41-50 | ka_u6                        | T7                           | β <sub>fm7</sub>              | ka_u7            | Tza   | Tze    | bte              |                  |       |                  |
| 51-60 | G <sup>I</sup> <sub>FJ</sub> | G <sup>I</sup> <sub>FB</sub> | G <sup>II</sup> <sub>FJ</sub> | G <sub>m</sub>   |       | cr     | ftr              | psir             |       | wr<br>(Ausg)     |
| 61-70 | Elem                         | Intpt                        | eps                           | geps             | maxit | cutmax | dtmin            | maxinc           | EInt  | ktuser           |
| 71-80 |                              |                              |                               |                  |       |        |                  |                  |       |                  |

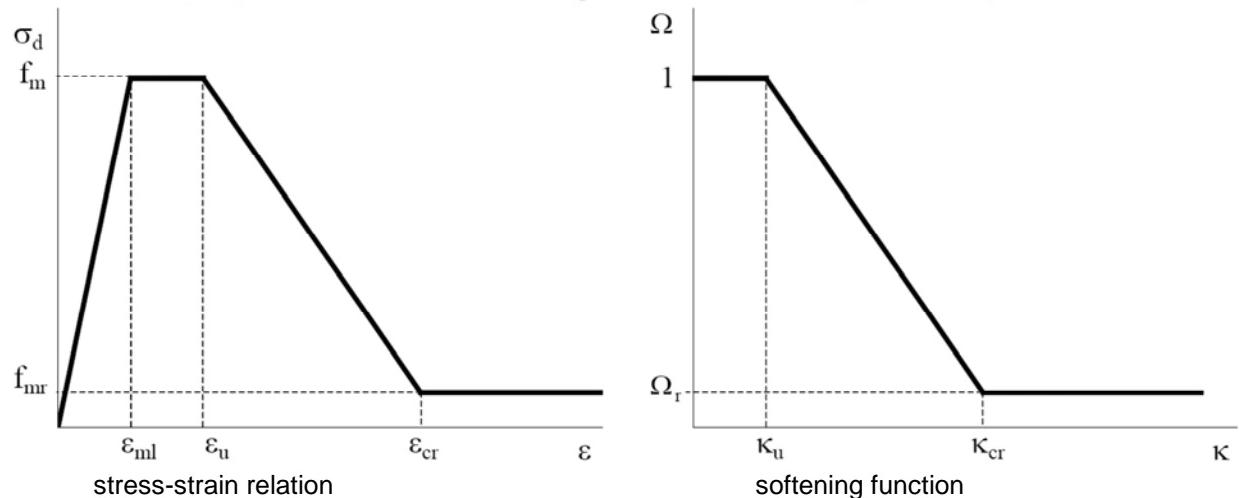
##### Material parameter

|                               |   |
|-------------------------------|---|
| fmx                           | uniaxial compression strength of masonry normal to the bed joints   |
| fmy                           | uniaxial compression strength of masonry normal to the head joints ( fmy ≤ fmx ! )  |
| ftx                           | tensile strength normal to the bed joints ( ≤ C / tan(phi) )  |
| ftxx                          | ftxx=10*ftx (geometrical parameter for F <sub>8</sub> )   |
| fty                           | tensile strength normal to the head joints (= 50% of tensile strength of units)   |
| nue_y                         | =0,9 (geometrical parameter for F <sub>8</sub> )  |
| as_y                          | distance of the head joints (mean value)  |
| al                            | distance of the bed joints (mean value)   |
| ü_y                           | lap length  |
| phi                           | friction angle (bed joints)   |
| c                             | cohesion (bed joints)   |
| phir                          | residual friction angle (bed joints)  |
| psi                           | dilatancy angle (usually 20°)   |
| ka_u                          | plastic strain hence softening begins   |
| eta_r                         | ratio of residual compressive strength / initial compressive strength   |
| G <sup>I</sup> <sub>FJ</sub>  | fracture energy MODE I tensile failure normal to bed joint(s)   |
| G <sup>I</sup> <sub>FB</sub>  | fracture energy MODE I tensile failure of stones (horizontal)   |
| G <sup>II</sup> <sub>FJ</sub> | fracture energy MODE II shear failure of bed joint(s)   |
| G <sub>m</sub>                | „strain energy“ (compressive failure)   |
| direc                         | orientation of the joints in relation to the element coordinate system<br>(0 = x – normal to bed joint; y – normal to head joint; z – normal to longitudinal joint<br>1 = z – normal to bed joint; y – normal to head joint; x – normal to longitudinal joint<br>2 = y – normal to bed joint; x – normal to head joint; z – normal to longitudinal joint) |
| dreid                         | switch for the three dimensional strength monitoring<br>=0 for 2D      F1 to F10<br>=1 for 2,5D      F1 to F10, F6 with Tau_res<br>=2 for 3D      F1 to F18   |
| if dreid = 2:                 |   |
| fmz                           | compressive strength of the masonry normal to longitudinal joint  |
| ftz                           | tensile strength normal to longitudinal joint (= ½ * stone tensile strength)  |
| ftzz                          | geometric parameter of F <sub>16</sub> (e.g. ftzz=10*ftx)   |
| nue_z                         | value of decrease of the uniaxial horizontal MW-compressive strength fmz (s. F <sub>16</sub> )  |
| as_z                          | distance of the longitudinal joints (stone breadth)   |
| ü_z                           | amount of offset between longitudinal joints  |
| cr                            | residual cohesion (for numerical stabilization)   |
| ftr                           | residual tensile strength (for numerical stabilization)   |
| psir                          | residual dilatancy (for numerical stabilization)  |

---

tempd      switch for temperature dependency  
           =0 or no entry:        no temperature dependency  
           =1:                    temperature dependency for compression and tension

Overview of input parameters of the softening function for the compressive space



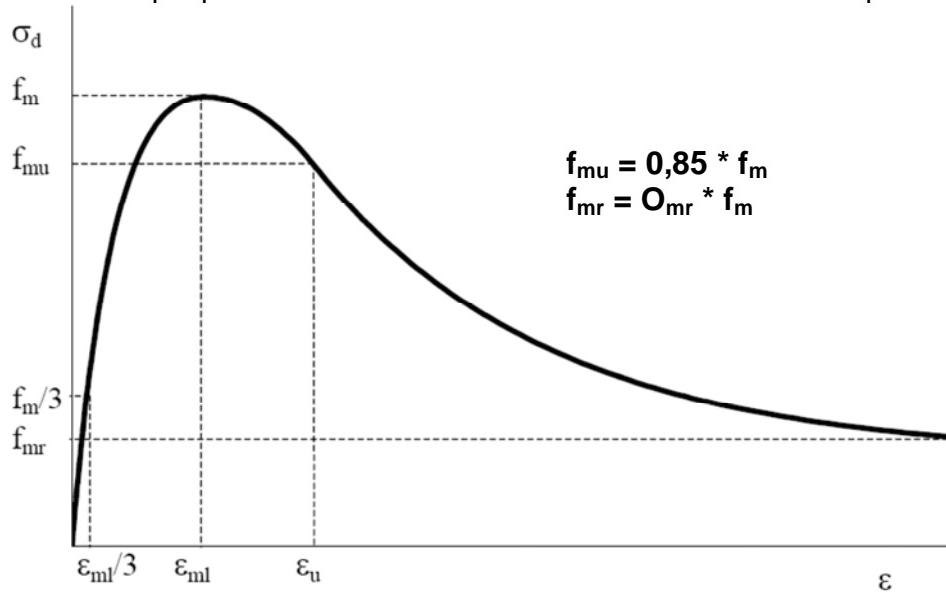
#### 4.2.8 LAW = 22 – Masonry Nonlinear Hardening/Softening

|       | 1                            | 2                            | 3                             | 4    | 5     | 6      | 7     | 8      | 9    | 10           |
|-------|------------------------------|------------------------------|-------------------------------|------|-------|--------|-------|--------|------|--------------|
| 0-10  | LAW                          | fmx                          | fmy                           | ftx  | ftxx  | fty    | nue_y | ep_ml  | Om_r | as_y         |
| 11-20 | al                           | ü_y                          | phi                           | c    | phir  | psi    | direc | dreid  | fmz  | ftz          |
| 21-30 | ftzz                         | nue_z                        | as_z                          | ü_z  |       | ep_u   |       | Ev     |      |              |
| 31-40 |                              |                              |                               |      |       |        |       |        |      |              |
| 41-50 |                              |                              |                               |      |       |        |       |        |      |              |
| 51-60 | G <sup>I</sup> <sub>FJ</sub> | G <sup>I</sup> <sub>FB</sub> | G <sup>II</sup> <sub>FJ</sub> |      |       | cr     | ftr   | psir   |      | wr<br>(Ausg) |
| 61-70 | Elem                         | Intpt                        | eps                           | geps | maxit | cutmax | dtmin | maxinc | EInt | ktuser       |
| 71-80 |                              |                              |                               |      |       |        |       |        |      |              |

##### Material parameter

|                               |   |
|-------------------------------|---|
| fmx                           | compressive strength of the masonry normal to the bed joint   |
| fmy                           | compressive strength of the masonry normal to the head joint <b>fmy ≤ fmx !</b>   |
| ftx                           | tensile strength normal to the bed joint (limit to C / tan(phi))  |
| ftxx                          | geometric parameter for F <sub>8</sub> (e.g. ftxx=10*ftx)   |
| fty                           | tensile strength normal to the head joint (= ½ * stone tensile strength)  |
| nue_y                         | value of decrease of the uniaxial horizontal MW-tensile strength fmy (s. F <sub>8</sub> )   |
| as_y                          | distance of head joints (stone length)  |
| al                            | distance of bed joints (stone height)   |
| ü_y                           | amount of offset between head joints  |
| phi                           | friction angle at the bed joint   |
| c                             | cohesion at the bed joint   |
| phir                          | residual strength - friction angle at the bed joint   |
| psi                           | initial angle of dilatancy (usually = friction angle)   |
| ep_ml                         | strain at reaching the uniaxial compressive strength of the masonry fmx   |
| Om_r                          | ration residual compressive strength / initial compressive strength   |
| ep_u                          | strain at softening in the pressure range at 0,85 fmx   |
| Ev                            | Youngs' modulus normal to the bed joint   |
| G <sup>I</sup> <sub>FJ</sub>  | fracture energy MODE I tensile failure normal to the bed joint(s)   |
| G <sup>I</sup> <sub>FB</sub>  | fracture energy MODE I tensile failure of the stones (horizontal)   |
| G <sup>II</sup> <sub>FJ</sub> | fracture energy MODE II shear failure of the bed joint(s)   |
| direc                         | orientation of the joints in relation to the element coordinate system<br>0 = x – normal to bed joint; y – normal to head joint; z – normal to longitudinal joint<br>1 = z – normal to bed joint; y – normal to head joint; x – normal to longitudinal joint<br>2 = y – normal to bed joint; x – normal to head joint; z – normal to longitudinal joint |
| dreid                         | switch for the three dimensional strength monitoring<br>= 0 for 2D      F1 to F10<br>= 1 for 2,5D    F1 to F10, F6 with Tau_res<br>= 2 for 3D      F1 to F18  |
| if dreid = 2:                 |   |
| fmz                           | compressive strength of the masonry normal to longitudinal joint  |
| ftz                           | tensile strength normal to longitudinal joint (= ½ * stone tensile strength)  |
| ftzz                          | geometric parameter of F <sub>16</sub> (e.g. ftzz=10*ftx)   |
| nue_z                         | value of decrease of the uniaxial horizontal MW-compressive strength fmz (s. F <sub>16</sub> )  |
| as_z                          | distance of the longitudinal joints (stone breadth)   |
| ü_z                           | amount of offset between longitudinal joints  |
| cr                            | residual cohesion (for numerical stabilization)   |
| ftr                           | residual tensile strength (for numerical stabilization)   |
| psir                          | residual dilatancy (for numerical stabilization)  |

Overview input parameter of the relation of stress-strain in the compressive space



#### 4.2.9 LAW = 33 – Orthotropic Boxed Value Model

|       | 1               | 2               | 3               | 4               | 5              | 6              | 7               | 8               | 9               | 10              |
|-------|-----------------|-----------------|-----------------|-----------------|----------------|----------------|-----------------|-----------------|-----------------|-----------------|
| 0-10  | LAW             | fLt             | fLc             | fRt             | fRc            | fTt            | fTc             | fRLs            | fRTs            | ntf             |
| 11-20 | Phi             | C               | psi             | phi*            | C*             | Tension        | alpha           | beta            | Tension*        |                 |
| 21-30 | $\Omega_{Lc0}$  | $\kappa_{Lc1}$  | $\Omega_{Lc2}$  | $\kappa_{Lc2}$  | $\kappa_{Lc3}$ |                |                 |                 | fTLs            | fTRs            |
| 31-40 | $\Omega_{Rc0}$  | $\kappa_{Rc1}$  | $\Omega_{Rc2}$  | $\kappa_{Rc2}$  |                | $\Omega_{Tc0}$ | $\kappa_{Tc1}$  | $\Omega_{Tc2}$  | $\kappa_{Tc2}$  |                 |
| 41-50 | $\Omega_{Ltr}$  | $\kappa_{Ltr}$  | $\Omega_{Rtr}$  | $\kappa_{Rtr}$  | $\Omega_{Ttr}$ | $\kappa_{Ttr}$ | $\Omega_{RLsr}$ | $\kappa_{RLsr}$ | $\Omega_{RTsr}$ | $\kappa_{RTsr}$ |
| 51-60 | $\Omega_{TLsr}$ | $\kappa_{TLsr}$ | $\Omega_{TRsr}$ | $\kappa_{TRsr}$ |                |                |                 |                 |                 | wr<br>(Ausg)    |
| 61-70 | Elem            | Intpt           | eps             | geps            | maxit          | cutmax         | dtmin           | maxinc          |                 | ktuser          |
| 71-80 |                 |                 |                 |                 |                |                |                 |                 |                 |                 |

##### Material parameter

- fLt uniaxial tensile strength longitudinal resp. parallel to the fiber direction  
 fLc uniaxial compressive strength longitudinal resp. parallel to the fiber direction  
 fRt uniaxial tensile strength radial  
 fRc uniaxial compressive strength radial  
 fTt uniaxial tensile strength tangential  
 fTc uniaxial compressive strength tangential  
 fRLs shear strength radial/longitudinal  
 fRTs shear strength radial/tangential  
 fTLs shear strength tangential/longitudinal  
 fTRS shear strength tangential/radial

##### relation of stress and strain, longitudinal, pressure domain

- $\Omega_{Lc0}$  starting point of the parabolic hardening, longitudinal (stress ratio to fLc)  
 $\kappa_{Lc1}$  plastic strain at reaching fLc  
 $\Omega_{Lc2}$  level of softening due to generation of knik bands  
 $\kappa_{Lc2}$  plastic strain at reaching  $\Omega_{Lc2}$   
 $\kappa_{Lc3}$  plastic strain at reaching the hardening due to compaction  
 $E_{Lcc}$  Youngs' modulus in the hardening area due to compaction =  $E_L$

##### relation of stress and strain, radial / tangential, pressure domain

- $\Omega_{Rc0}$  starting point of the parabolic hardening, longitudinal (stress ratio to fLc)  
 $\kappa_{Rc1}$  plastic strain at reaching fLc  
 $\Omega_{Rc2}$  level of softening due to generation of knik bands  
 $\kappa_{Rc2}$  plastic strain at reaching  $\Omega_{Rc2}$   
 $E_{Rcc}$  Youngs' modulus in the hardening area due to compaction =  $E_R$

Werte für tangentiale Richtung Index R → T

##### relation of stress and strain tensile area and shear domain

- $\Omega_{dmr}$  ratio residual strength / initial strength  
 $\kappa_{dmr}$  plastic strain at reaching the residual strength

For both dimensions applies:

Index d = direction (L – longitudinal, R – radial, T – tangential)

Index m = mode (t – tension, s – shear)

For graphical explanation of the material values see Fig. 3-23, Fig. 3-24 and Fig. 3-25.

#### 4.2.10 LAW = 40 – Geological Drucker-Prager

|       | 1    | 2      | 3    | 4    | 5     | 6      | 7     | 8      | 9 | 10     |
|-------|------|--------|------|------|-------|--------|-------|--------|---|--------|
| 0-10  | LAW  |        |      |      |       |        |       |        |   |        |
| 11-20 |      |        |      |      |       |        |       |        |   |        |
| 21-30 |      |        |      |      |       |        |       |        |   |        |
| 31-40 |      |        |      |      |       |        |       |        |   |        |
| 41-50 |      |        |      |      |       |        |       |        |   |        |
| 51-60 | beta | Sig_yt | delt |      |       |        |       |        |   | wr     |
| 61-70 | Elem | Intpt  | eps  | geps | maxit | cutmax | dtmin | maxinc |   | ktuser |
| 71-80 |      |        |      |      |       |        |       |        |   |        |

#### DRUCKER-PRAGER

beta material parameter, that determines the ascent of the Drucker-Prager cone  
 Sig\_yt strength value (analogue cohesion)  
 delt dilatancy factor

(note: ideal elasto-plastic material model with associated or non-associated flow rule)

#### 4.2.11 LAW = 41 – Combination Mohr-Coulomb and Drucker-Prager resp. TRESCA vs. MISES

|       | 1    | 2      | 3    | 4    | 5      | 6      | 7       | 8      | 9        | 10     |
|-------|------|--------|------|------|--------|--------|---------|--------|----------|--------|
| 0-10  | LAW  | phig   | Cg   | psig | phig*  | Cg*    | Tension |        | Tension* |        |
| 11-20 |      |        |      |      |        |        |         |        |          |        |
| 21-30 |      |        |      |      |        |        |         |        |          |        |
| 31-40 |      |        |      |      |        |        |         |        |          |        |
| 41-50 |      |        |      |      |        |        |         |        |          |        |
| 51-60 | beta | Sig_yt | delt |      |        |        |         |        |          | wr     |
| 61-70 | Elem | Intpt  | eps  | geps | max-it | cutmax | dtmin   | maxinc |          | ktuser |
| 71-80 |      |        |      |      |        |        |         |        |          |        |

##### Isotropic MOHR-COULOMB + DRUCKER-PRAGER

|          |   |
|----------|---|
| phig     | frictional angle  |
| Cg       | cohesion  |
| psig     | dilatancy angle   |
| phig*    | residual strength – frictional angle                                      |
| Cg*      | residual strength - cohesion  |
| Tension  | tension cut off ( $\leq C_g / \tan(\text{phig})$ )                        |
| Tension* | residual strength ( $\leq C_g^* / \tan(\text{phig}^*)$ )                  |
| beta     | material parameter, that determines the ascent of the Drucker-Prager cone |
| Sig_yt   | strength value (analog cohesion)  |
| delt     | dilatancy factor  |

Remark:

Mohr Coulomb = Tresca if friction angle = 0

Drucker Prager = v Mises if beta = 0

## 4.3 Numerical control variables

|           |  |
|-----------|--|
| eps       | local convergence criteria Return Mapping  |
| geps      | criteria for singular systems of equations for multi-area activity   |
| maxit     | Maximum amount of local iterations of the return mapping process   |
| cutmax    | amount of local bisections prior the activation of a global bisection                                      |
| maxinc    | maximum incrementation of a load step (global + local)   |
| dtmin     | minimum time increment of the ANSYS-command ( <i>deltim,,dtmin</i> )                                       |
| ktuser =1 | given setting to build the elasto-plastic tangent matrix at the local plane of the integration point (= 1) |
| EInt      | switch for Element-Integration<br>= 0: full integration<br>= 1: reduced integration                        |
|           | activation of the output control (debug- resp. control-modus for developers or users when necessary)       |
| wr        | output key   |
| Elem      | element number   |
| Intp      | number of the integration point  |

### 4.3.1 Choice of the numerical control variables

|                |   |
|----------------|---|
| eps:           | $10^{-6}$ , shall not be chosen to small ( $10^{-4}$ at KN and m);  |
| maxit:         | 10 local iteration steps shall be enough (at least as many as active yield surfaces);<br>but not to be chosen too small   |
| geps:          | $10^{-20}$ for double precision;  |
| maxinc:        | must be larger than global and local load increments separately and also than the product<br>e.g. at dtmin 0.05: maxinc > 1/0.05 > 20 and cutmax 5: maxinc > $2^5$ > 32<br>maxinc > $20 \cdot 32 > 640$ , |
| cutmax         | 4   |
| output control |   |
| wr = 1         | output of the violated yield criterias  |

```
***** START mpls5 *****
Elem: 436 intpt= 1 KTFORM= 0TIMINC=0.5000 KFSTEQ= 0 KFIRST= 0 LAW= 1
***** START LOCAL STRAIN INCREMENT *****
***** START LOCAL ITERATION *****
*** Kontrollausgabe Fliesskriterien ***
1060 F-value 1-6:    70.165    0.000    0.000    0.000    0.000    96.647
1070 F-value 7-12:   0.000    0.000    0.000    0.000    0.000    0.000
1080 F-value 13-18:  0.000    0.000    0.000    0.000    0.000    0.000
1090 nfail= 2
```

wr =2        output of the local iteration sequence with trialstresses, violated yield criterias,  
plastic multiplicators, plastic and elastic increments of strain

Means:  
for LAW 1, 2, 10:

|     |                                       |
|-----|---------------------------------------|
| F1  | shear failure MOHR-COULOMB, isotropic |
| F2  | shear failure 1. joint                |
| F3  | shear failure 2. joint                |
| F4  | shear failure 3. joint                |
| F5  | shear failure 4. joint                |
| F6  | tensile failure isotropic             |
| F7  | tensile failure 1. joint              |
| F8  | tensile failure 2. joint              |
| F9  | tensile failure 3. joint              |
| F10 | tensile failure 4. joint              |

for LAW 9:

|    |   |
|----|---|
| F1 | DRUCKER-PRAGER, F1 (tensile domain, tensile-compressive domain)     |
| F2 | DRUCKER-PRAGER, F2 (compressive-tensile domain, compressive domain) |

for LAW 20, 22:

|           |   |
|-----------|---|
| F1 (F11)  | stone tensile failure   |
| F2 (F12)  | compression failure of the masonry                                      |
| F3 (F13)  | shear failure of the masonry, stone failure                             |
| F4 (F14)  | tensile failure of the masonry, parallel to bed joint, stone failure    |
| F5 (F15)  | transition section between F1, F3, F4 resp. F11, F13, F14               |
| F6        | shear failure of bed joints   |
| F7        | tensile failure of bed joints   |
| F8 (F16)  | tensile failure of bed joints on horizontal compressive stress          |
| F9 (F17)  | staircase-shaped shear failure of bed- and head joints                  |
| F10 (F18) | tensile failure of the masonry parallel to the bed joint, joint failure |

for LAW 40:

|    |                |
|----|----------------|
| F2 | DRUCKER-PRAGER |
|----|----------------|

for LAW 41:

|    |                                       |
|----|---------------------------------------|
| F1 | shear failure MOHR-COULOMB, isotropic |
| F2 | DRUCKER-PRAGER                        |
| F6 | tensile failure isotropic             |

### 4.3.2 Remarks for choosing the material parameters

No material parameter should be ever set to 0.0. Even for residual strengths values above  $\text{eps}^*100$  should be chosen. Dilatancy angles close to zero imply ideally smooth friction surfaces in a physical sense and can lead to extreme convergence difficulties. This results from tension component which can not be removed in case of shear failure. The dilatancy angle therefore should always be set at least to  $1^\circ$ . The tension strength is limited to the intersection point of the Mohr-Coulomb-line (-plane) and the normal friction axis ( $C / \tan(\phi)$ ).

### 4.3.3 Remarks and tips for using multiPlas in nonlinear structural analysis

If an oscillation can be seen for a certain imbalance value, the convergence for the load step can be achieved by increasing the convergence criteria in ANSYS slightly above the oscillation value. In the following load case the convergence criteria can be set to the smaller value again.

In case of frequent error messages (\*\*local return mapping failed\*\*) the local number of iterations should be increased and the yield areas should be checked. This output only occurs if  $wr \geq 1$ .

In case where problems occur from processing the polyhedral yield figure (in case of unfortunate physically problematic choice of parameters) the calculations should be performed by using isotropic yield criteria with the whole load at first. Then a following calculation with activation of anisotropic yield criteria (this is especially the case for primary stress conditions) can be done.

Do never chose dilatancy or friction angle as 0.0 because this can lead to unbalanced forces which can not be relocated!

A cohesion  $c = 0$  (e.g. sand) implies that the material does not have any uniaxial compressive or tensile strength. First, the material therefore has to be iterated into a stable position. This leads very often to convergence difficulties, so it is advised to use an adequately small value instead of zero for the cohesion while using the MOHR-COULOMB (LAW = 1) yield conditions.

The automatic time stepping is called directly from the routine (it can be switched on via: autots,on).

---

The global load step bisection can be disabled by choosing a large value for cutmax. In the case of a local bisection, no hints are written out.

Be careful not to use too large values for maxinc and simultaneous suppression of the global bisection. This may lead to a large computational effort in a Newton-Raphson-Equilibrium iteration! In this case, request the cause by use the global bisection!

Multi surface plasticity fundamentally is a physical path dependent phenomenon. Therefore a global incrementation in order to represent the relocation of force correctly is of utmost importance.

In the multi surface routines, softening (residual strength) is only introduced in at the equilibrium states (so only after reaching the global Newton-Raphson equilibrium). Therefore, a global incrementing is important in the case of softening.

The value dtmin in the tb-data-fiel has to be identical to the value of dtmin that is used by ANSYS in the solution-phase (deltim,dtanfang,dtmin,dtmax,...).

If no convergent solution could be found:

- decrease incrementation (dtmin,...)
- increase the global convergence criteria (cnvtol,f,...)

Newton-Raphson, full (usage of consistent elasto-plastic tangent) or Newton-Raphson, init (starting stiffness) is supported. For the practical problems Newton-Raphson, init is recommended. Especially when considering geometric nonlinearities or when working with EKILL / EALIVE the full Newton-Raphson method is necessary.

## 4.4 Remarks for Postprocessing

### Plastic effective strain

EPPELQV: The plastic effective strain shows the quantitative activity and is used for pointing out the areas in which local load shifting or material failure / crack forming take place.

$$\varepsilon_{\text{pl,eqv}} = \sqrt{\frac{2}{3} [\varepsilon_{\text{pl},x}^2 + \varepsilon_{\text{pl},y}^2 + \varepsilon_{\text{pl},z}^2 + \frac{1}{2} (\varepsilon_{\text{pl},xy}^2 + \varepsilon_{\text{pl},yz}^2 + \varepsilon_{\text{pl},zx}^2)]}$$

### Plastic activity activity (NSLRAT)

The plastic activity shows which qualitative plastic activities are taking place in the current equilibrium state. They are used for illustration which of the flow criteria is active, that means not satisfied, within the respective area of the structure. This enables deducting the type and cause of the load shifting.

The pointer of the plastic activity is path depended. A plastic activity can be activated and deactivated more than once during a load case. The plastic activity is identified by a characteristic (nl,srat):

Output for LAW 1, 10:

|               |                                       |
|---------------|---------------------------------------|
| scale         | active yield criterion                |
| 1             | shear failure MOHR-COULOMB, isotropic |
| 10            | shear failure 1. separation plane     |
| 100           | shear failure 2. separation plane     |
| 1000          | shear failure 3. separation plane     |
| 10 000        | shear failure 4. separation plane     |
| 100 000       | tensile failure isotropic             |
| 1 000 000     | tensile failure 1. separation plane   |
| 10 000 000    | tensile failure 2. separation plane   |
| 100 000 000   | tensile failure 3. separation plane   |
| 1 000 000 000 | tensile failure 4. separation plane   |

Output for LAW 2, 9:

|       |  |
|-------|--|
| scale | active yield criterion   |
| 1     | DRUCKER-PRAGER, joint 1 (tensile space, tensile-compressive space)     |
| 10    | DRUCKER-PRAGER, joint 2 (compressive-tensile space, compressive space) |

Output for LAW 20, 22:

|               |   |
|---------------|---|
| scale         | active yield criterion  |
| 1             | stone tensile failure   |
| 10            | compressive failure of the masonry  |
| 100           | shear failure of the masonry, stone failure                               |
| 1000          | tensile failure of the masonry parallel to bed joint, stone failure       |
| 10 000        | transition section between F1, F3, F4 resp. F11, F13, F14                 |
| 100 000       | shear failure of bed joints   |
| 1 000 000     | tensile failure of bed joints   |
| 10 000 000    | tensile failure of bed joints on horizontal horizontal compressive stress |
| 100 000 000   | staircase-shaped shear failure of bed- and head joints                    |
| 1 000 000 000 | tensile failure of the masonry parallel to the bed joint, joint failure   |

## Output for LAW 33:

|             |   |
|-------------|---|
| scale       | active yield criterion                              |
| 1           | F1 tensile failure longitudinal                     |
| 10          | F2 compressive failure longitudinal                 |
| 100         | F3 shear failure parallel to the LT plane           |
| 1000        | F4 tensile / shear failure parallel to the LT plane |
| 10 000      | F5 compressive failure radial                       |
| 100 000     | F6 tensile- / shear fail parallel to the LR plane   |
| 1 000 000   | F7 compressive failure tangential                   |
| 10 000 000  | shear failure separation plane                      |
| 100 000 000 | tensile failure separation plane                    |

## Output for LAW 40:

|       |                        |
|-------|------------------------|
| scale | active yield criterion |
| 1     | -                      |
| 10    | DRUCKER-PRAGER         |

## Output for LAW 41:

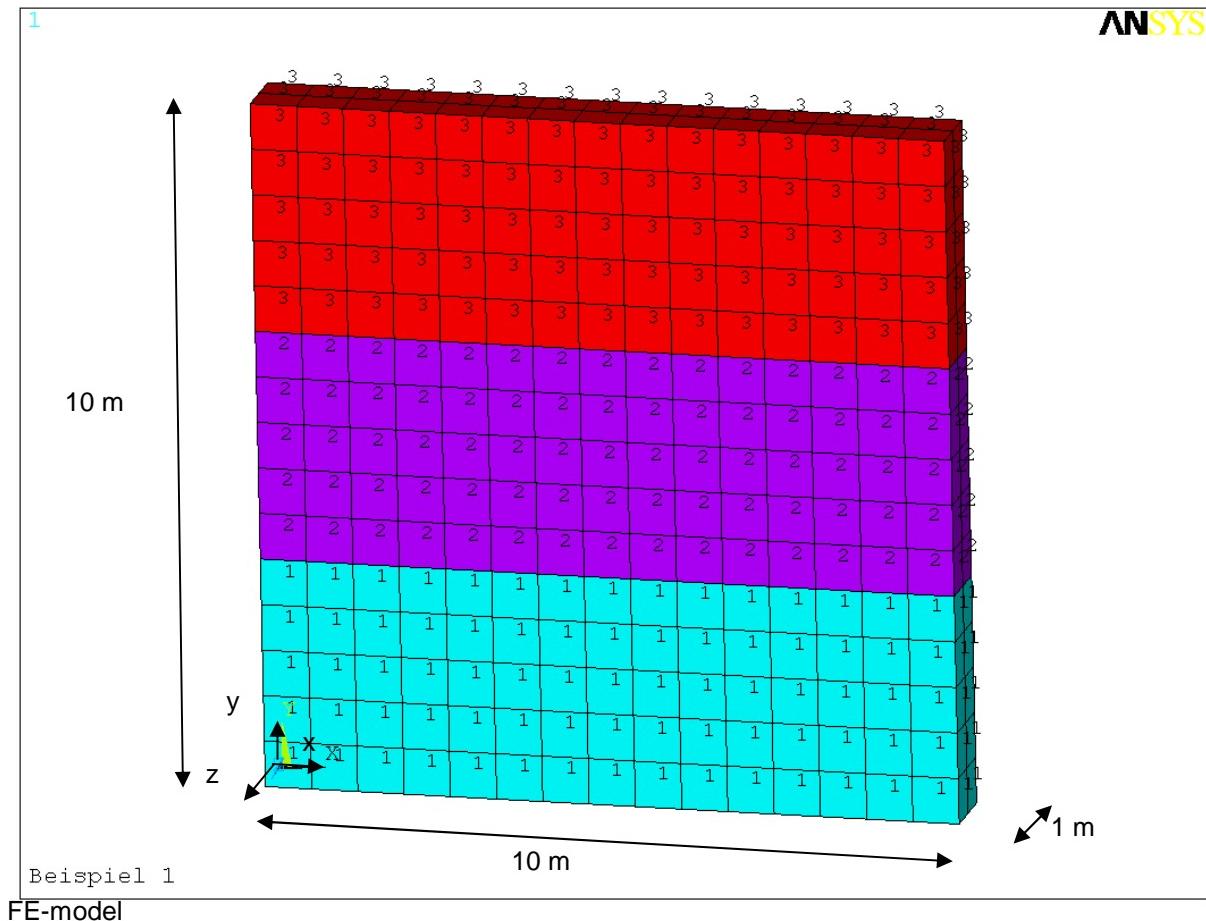
|         |   |
|---------|---|
| scale   | active yield criterion                  |
| 1       | tensile failure MOHR-COULOMB, isotropic |
| 10      | DRUCKER-PRAGER                          |
| 100     | -                                       |
| 1000    | -                                       |
| 10 000  | -                                       |
| 100 000 | tensile failure isotropic               |

If several flow conditions are active at once then the activity pointer are added up. For example SRAT = 101 for LAW 1 with separation planes stands for shear failure MOHR-COULOMB isotropic and shear failure on the second separation plane.

The scaling settings for the output are done using the cval-command in ANSYS  
 (e.g.: /CVAL,all,0.5,1,10,100000  
 ples,nl,srat  
 for LAW 41)

## 5 VERIFICATION EXAMPLES

### 5.1 Example 1 – Earth pressure at rest



Material assumptions (material 1 to 3), sand:

|                                       |                              |
|---------------------------------------|------------------------------|
| Angle of inner friction               | $\phi = 30^\circ$            |
| Cohesion                              | $c = 0$                      |
| Constrained modulus                   | $E_s = 40000 \text{ kN/m}^2$ |
| Coefficient of earth pressure at rest | $k_0 = 0,5$                  |
| Density                               | $\rho = 1,8 \text{ t/m}^3$   |

Therefore:

$$\text{Poisson's ratio: } v = \frac{k_0}{1+k_0} = 0,333$$

$$\text{Shear modulus: } G = \frac{1-2v}{2(1-v)} E_s = 10000 \text{ kN/m}^2$$

theory see [6-19]

$$\text{Young's modulus: } E = 2(1+v)G = 26670 \text{ kN/m}^2$$

Boundary conditions:

|                                   |                    |
|-----------------------------------|--------------------|
| lower boundary $y = 0$ :          | $ux = uy = uz = 0$ |
| side boundary $x = 0$ bzw. $10$ : | $ux = 0$           |
| side boundary $z = 0$ bzw. $1$ :  | $uz = 0$           |

Elements: Solid45

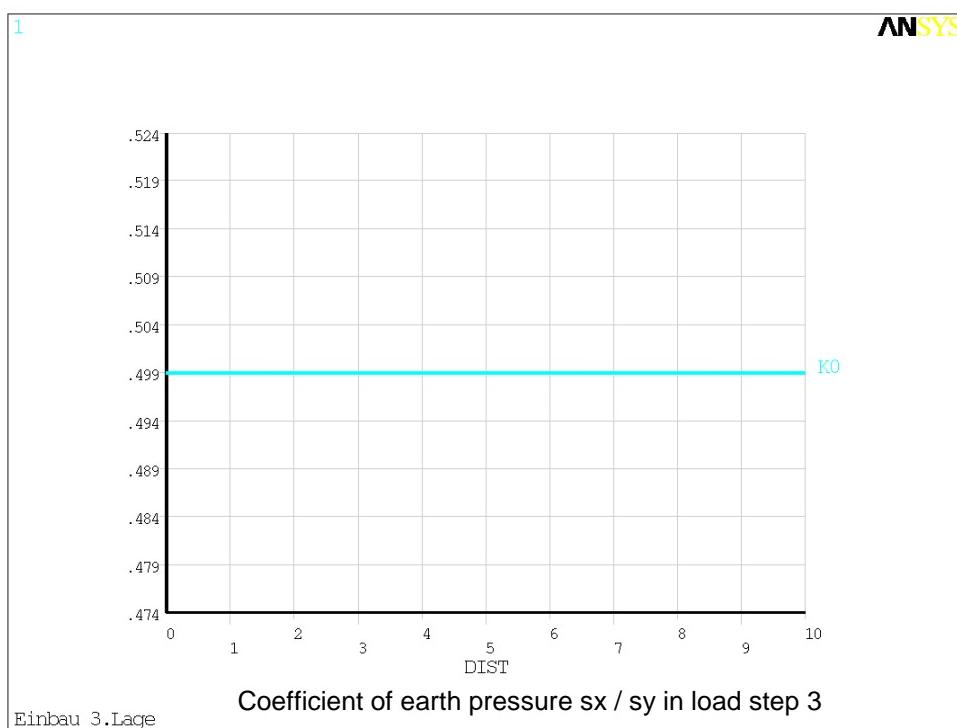
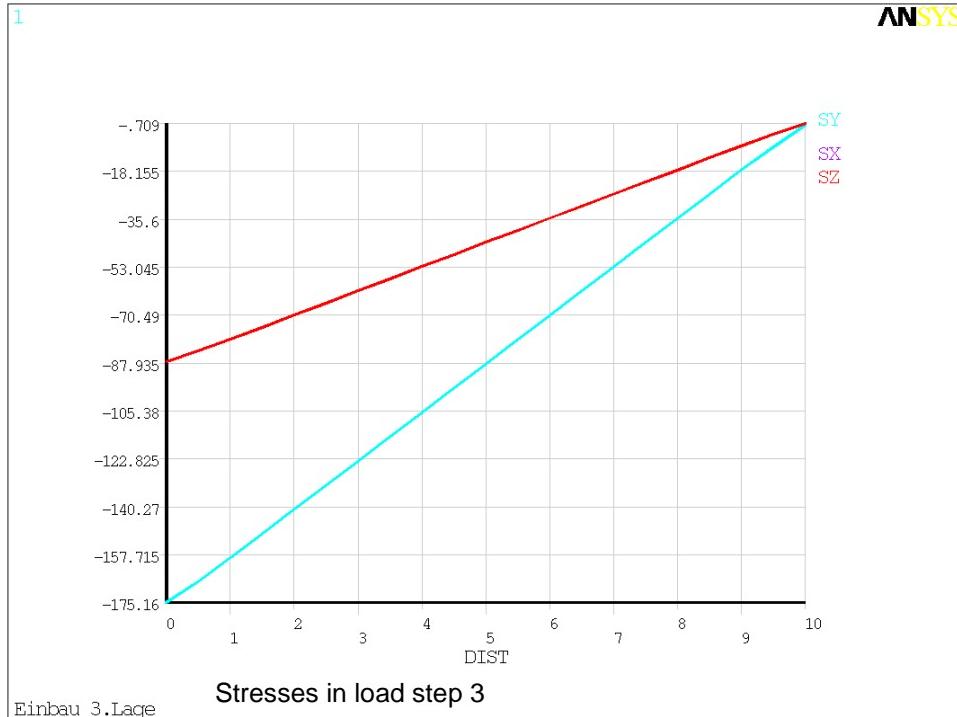
Load history:

1st Load step: installation 1st layer (material 1)

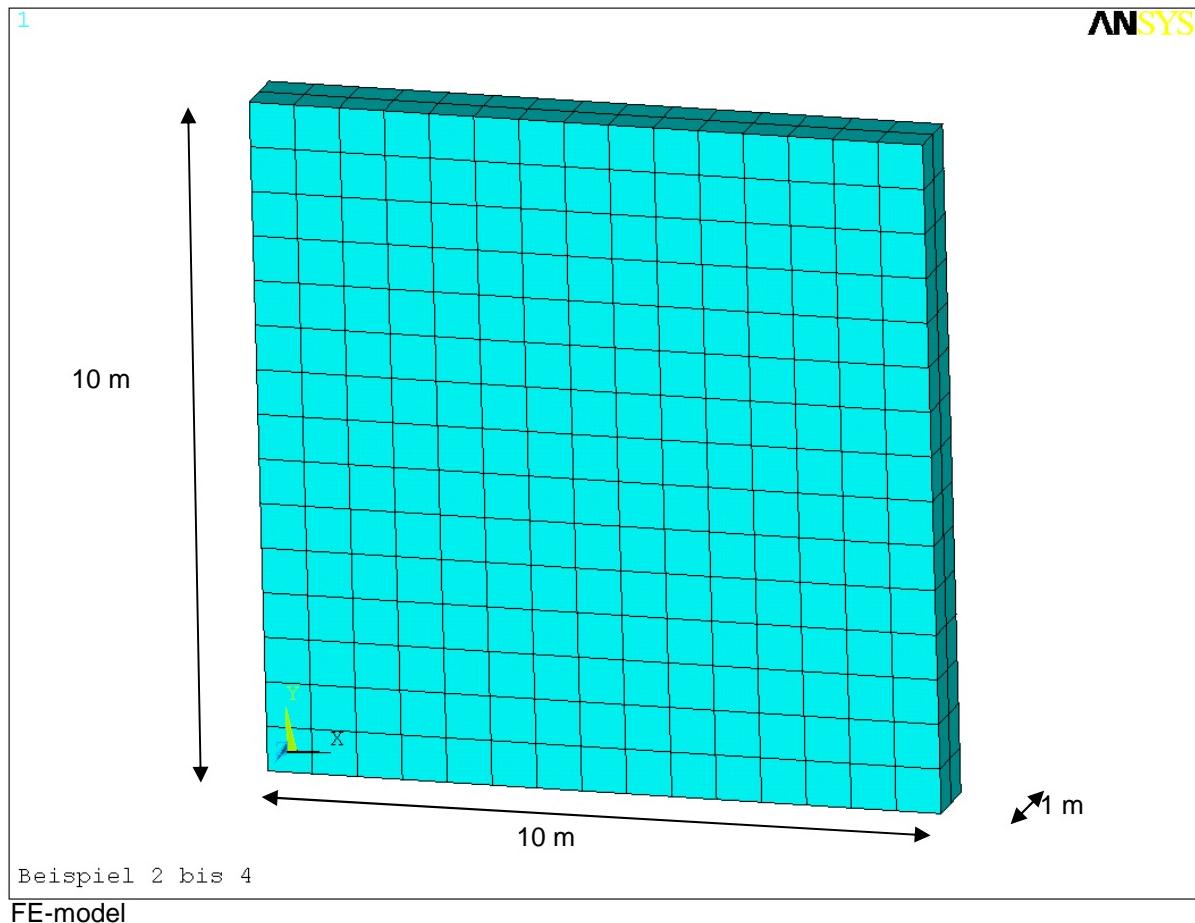
2nd Load step: installation 2nd layer (material 2)

3rd Load step: installation 3rd layer (material 3)

Reference solution: (bsp1.dat) path plots along the boundary at  $x = 0$



## 5.2 Examples 2 to 4 - Earth pressure at rest and active earth pressure



### Material assumption (material 1):

|                                       |   |
|---------------------------------------|---|
| Angle of inner friction               | $\phi = 30^\circ$ ; residual strength $\phi_r = 30^\circ$ |
| Angle of dilatancy                    | $\psi = 30^\circ$   |
| Cohesion                              | $c = 0$   |
| Elastic modulus                       | $E_s = 40000 \text{ kN/m}^2$                              |
| Coefficient of earth pressure at rest | $k_0 = 0,5$   |
| Density                               | $\rho = 1,8 \text{ t/m}^3$                                |

Therefore:

|                   |                            |
|-------------------|----------------------------|
| Poisson's ration: | $\nu = 0,333$              |
| Shear modulus:    | $G = 10000 \text{ kN/m}^2$ |
| Young's modulus:  | $E = 26670 \text{ kN/m}^2$ |

Elements: Solid45

Load history:

1st Load step: Earth pressure in a result of the gravity

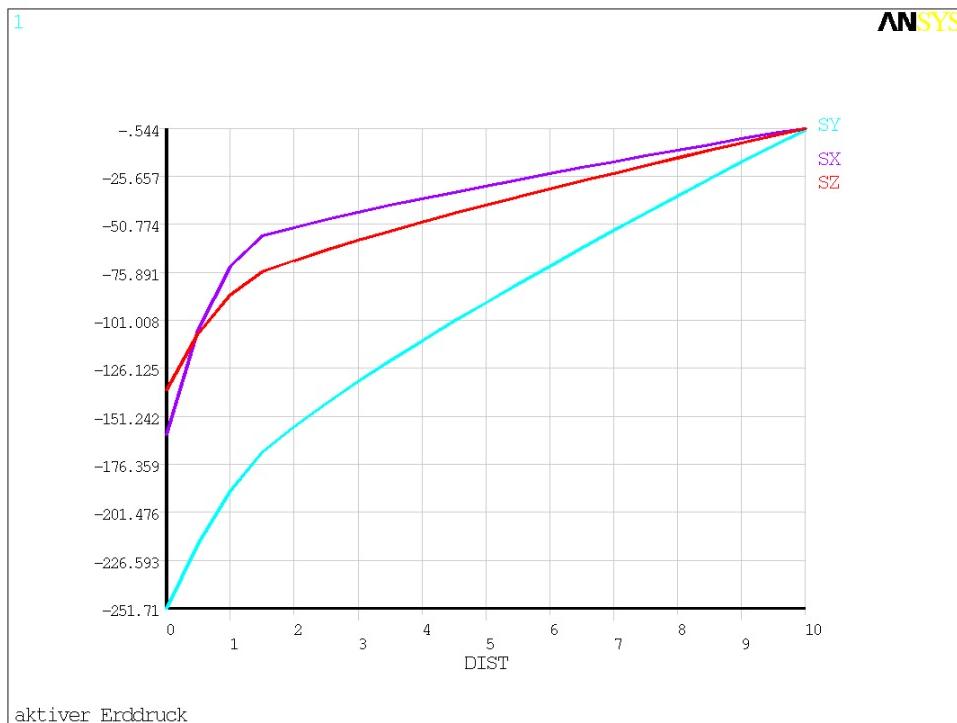
Boundary conditions:

|                                |                       |
|--------------------------------|-----------------------|
| lower boundary $y = 0$ :       | $u_x = u_y = u_z = 0$ |
| side boundary $x = 0$ bzw. 10: | $u_x = 0$             |
| side boundary $z = 0$ bzw. 1:  | $u_z = 0$             |

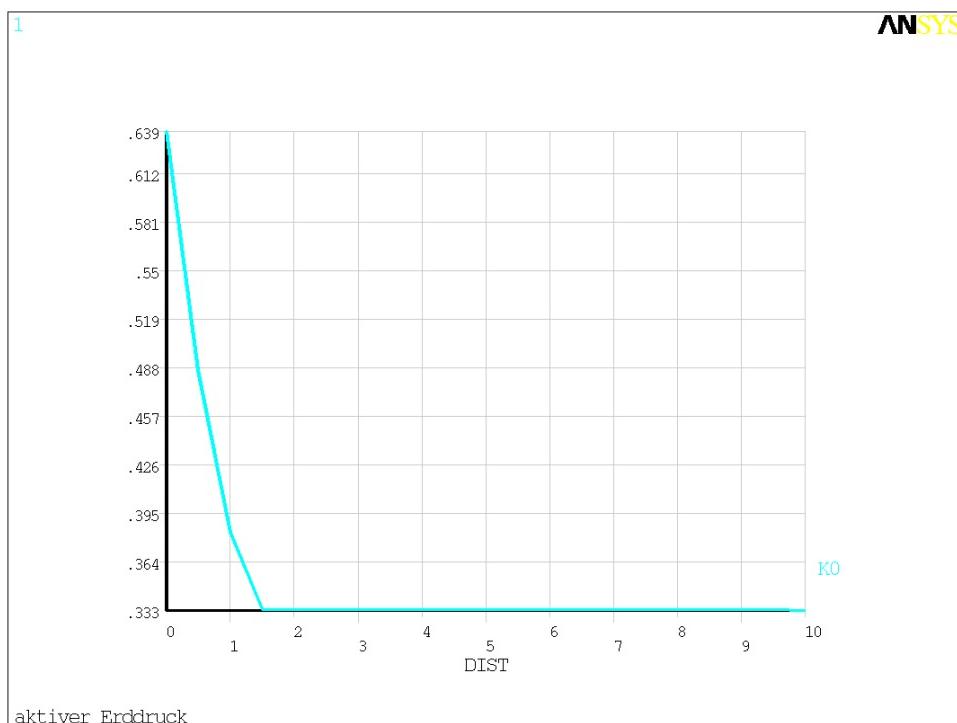
2nd load step: Activation of the active earth pressure by rotation of the side boundary  $x = 0$  about the base point, horizontal top point displacement: 3cm

Reference solution: Example 2 - Calculation with LAW = 1 MOHR-COULOMB (bsp2.dat)

Number of substeps / iterations: 4 / 18  
 cpu-time: (1x 4-M CPU 1,70 GHz) 21,9 sec



Stresses in load step 2 as path plots along the boundary  $x = 0$

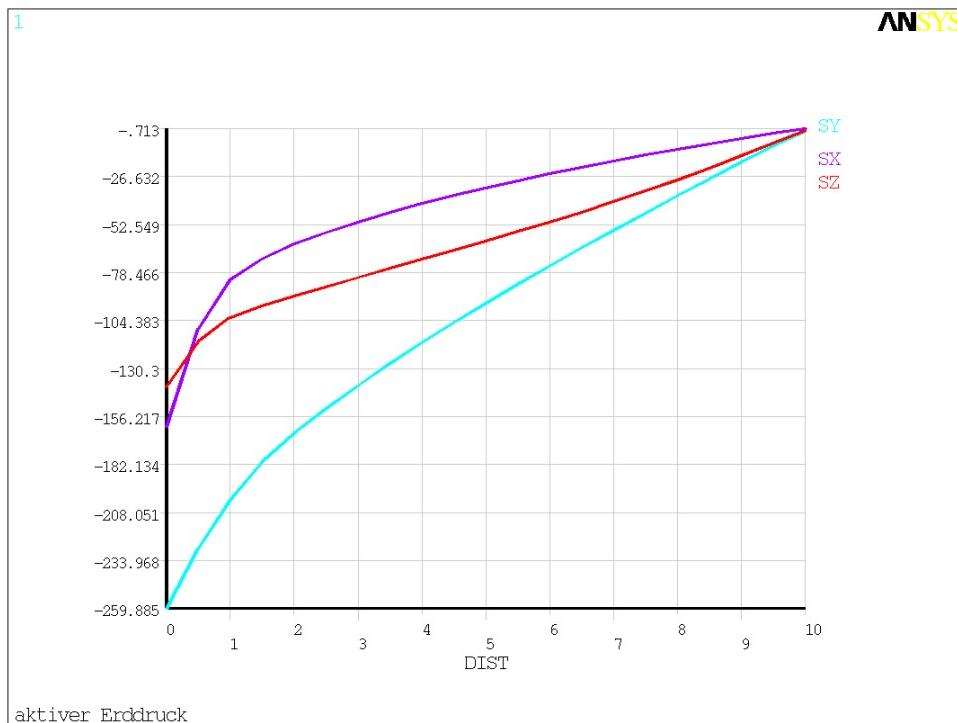


Coefficient of earth pressure  $s_x / s_y$  in load step 2 as a path plot along the border  $x = 0$

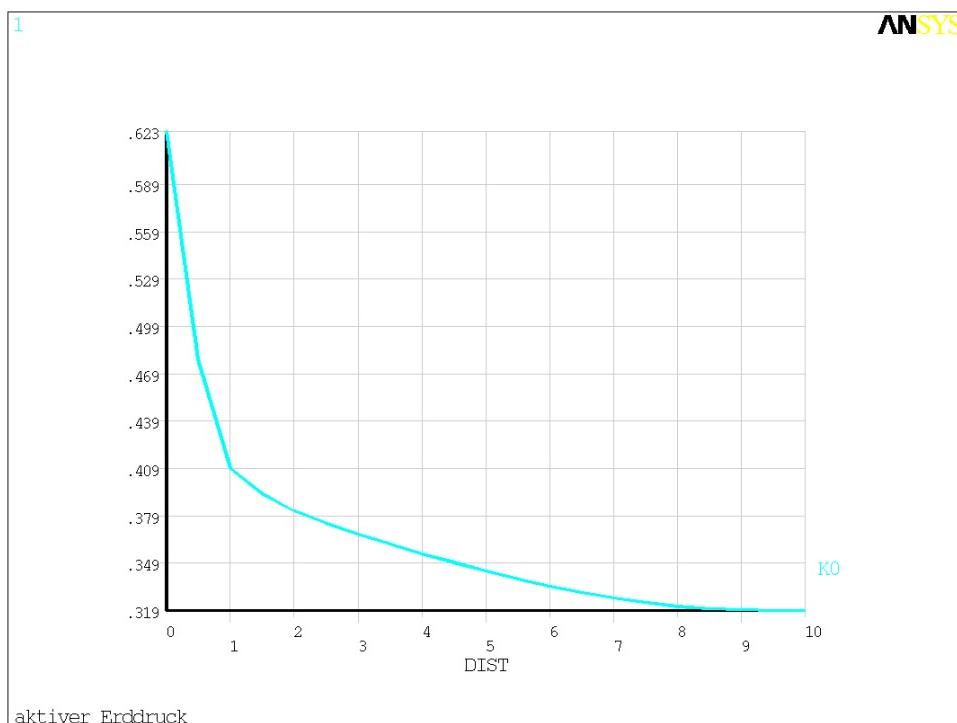
$U_{sum} = 0,047487 \text{ m}$   
 $EPPL, EQV = 0,003927$

Reference solution: Example 3 - Calculation with LAW = 40 DRUCKER-PRAGER (bsp3.dat)

Number of substeps / iterations: 4 / 8  
 cpu-time: (1x 4-M CPU 1,70 GHz) 13,4 sec



Stresses in load step 2 as path plots along the boundary  $x = 0$

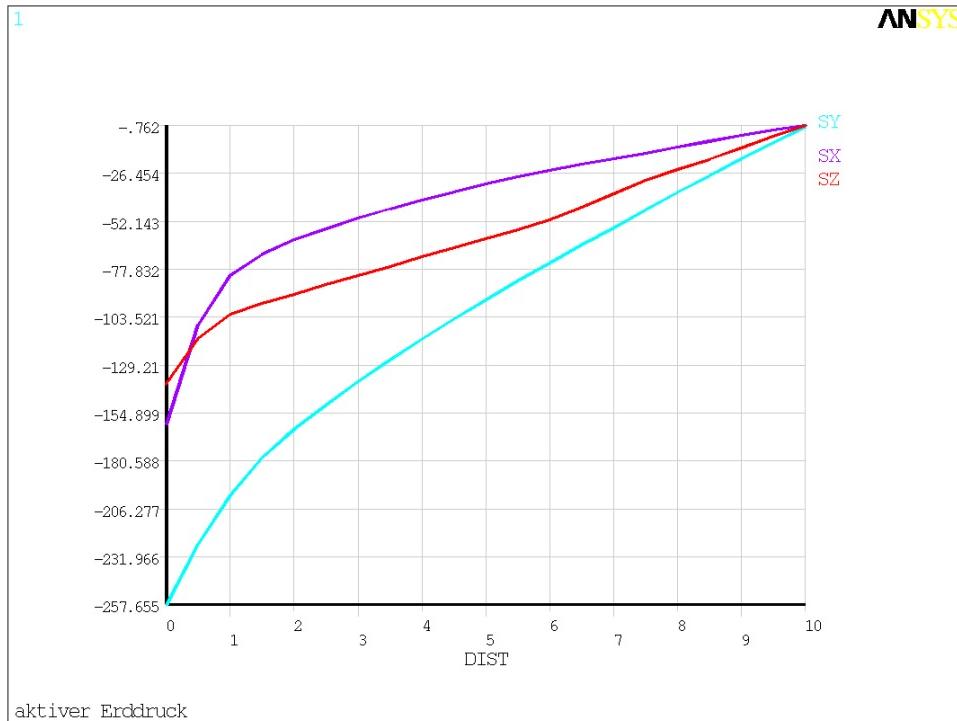


Coefficient of earth pressure  $s_x / s_y$  in load step 2 as a path plot along the border  $x = 0$

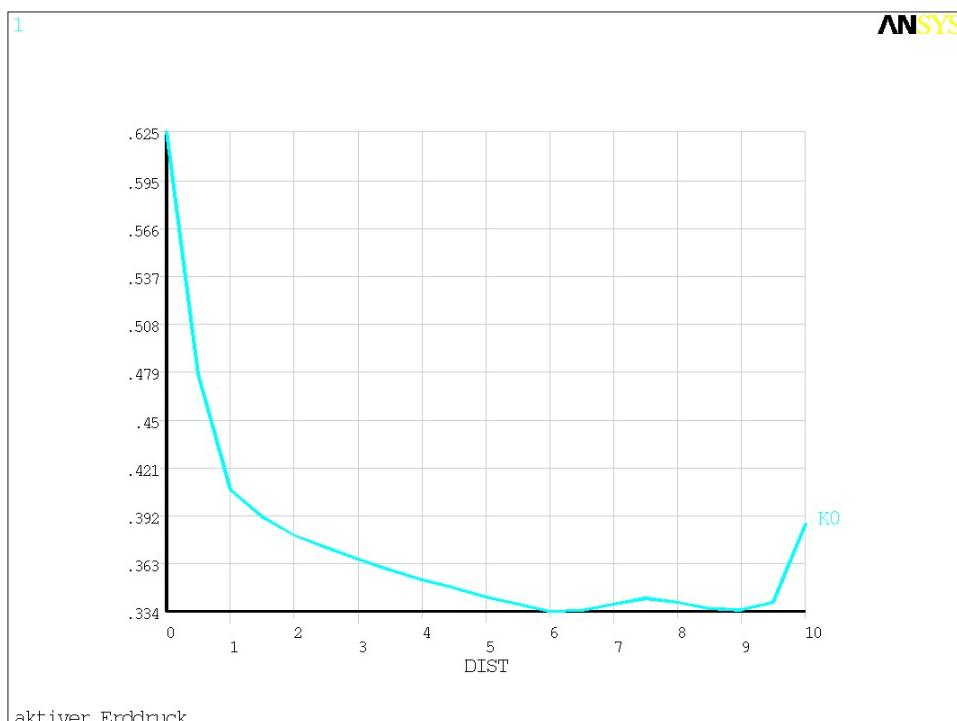
$U_{sum} = 0,046891 \text{ m}$   
 $EPPL, EQV = 0,003238$

Reference solution: Example 4 - Calculation with LAW = 41 MOHR-COULOMB+DRUCKER-PRAGER (bsp4.dat)

Number of substeps / iterations: 4 / 9  
cpu-time: (1x 4-M CPU 1,70 GHz) 14,41 sec



Stresses in load step 2 as path plots along the boundary  $x = 0$



Coefficient of earth pressure  $s_x / s_y$  in load step 2 as a path plot along the border  $x = 0$

maximale Gesamtverschiebung:  $U_{sum} = 0,047003$  m  
maximale plastische Vergleichsdehnung:  $EPPL, EQV = 0,003361$

### 5.3 Examples 5 to 8 - Kienberger Experiment G6 [6-13]

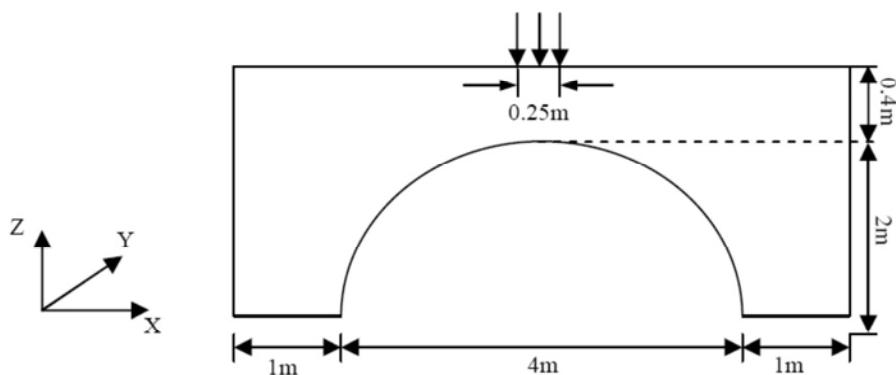


Figure 6. Geometry of laboratory testing.

Table 4. Soil characteristics.

| Soil | E [MPa] | $\nu$ | Density<br>[kg/m <sup>3</sup> ] | c [MPa] | $\phi$ [°] | $\psi$ [°] |
|------|---------|-------|---------------------------------|---------|------------|------------|
| Sand | 15      | 0.2   | 1800                            | 0       | 45         | 15         |

Table 5. Steel profile characteristics.

| Steel profile | E [GPa] | $\nu$ | Density<br>[kg/m <sup>3</sup> ] | I [cm <sup>4</sup> /m] | t [mm] | A [cm <sup>2</sup> /m] |
|---------------|---------|-------|---------------------------------|------------------------|--------|------------------------|
| S235 W 152/50 | 210     | 0.3   | 7850                            | 95.94                  | 2.7    | 33.29                  |

\*\*Calculation:

- material and geometric nonlinear
- Convergence bound at 1% to 2% of the L2-norm of the residual forces.  
In ANSYS, the convergence criterion is defined as default value of 0.1 % of the L2-norm of the residual forces. That means that all residual forces have to be transferred to the load vector except 0.1 % of the Root Mean Square. In the following calculations, a convergence criterion between 1% and 2% has been used. According to experience, convergence criteria between 1% and 2% are precisely enough, to verify equilibrium conditions.  
(Cohesion = 0 means no tensile- resp. compressive strength of the material. Hence result convergence problems, so that the convergence bound has to be increased compared with the default value to achieve a solution.)

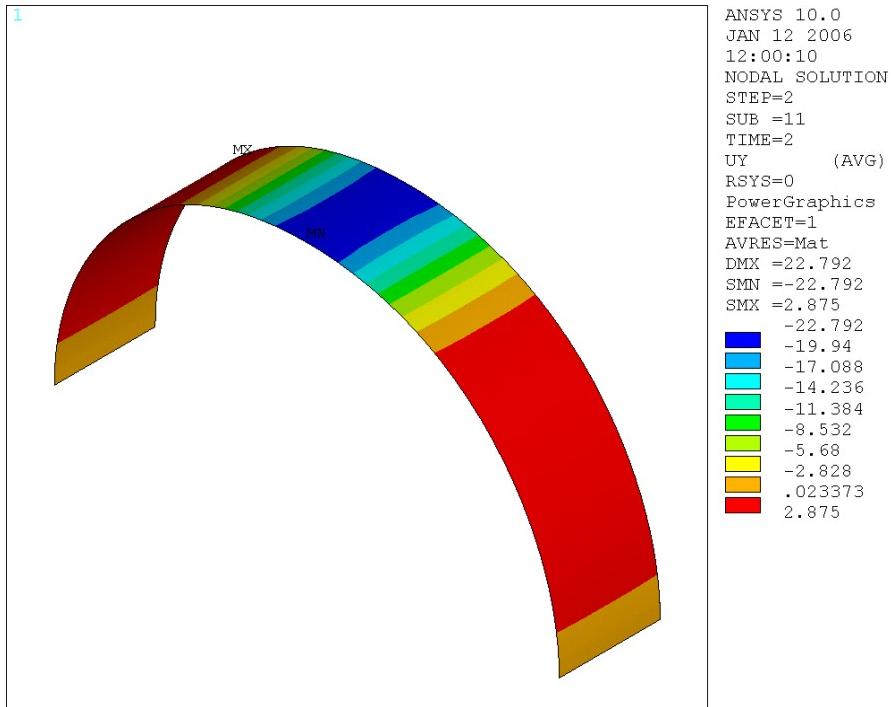
\*\*Element types:

Solid45 und Shell63

\*\*Load history

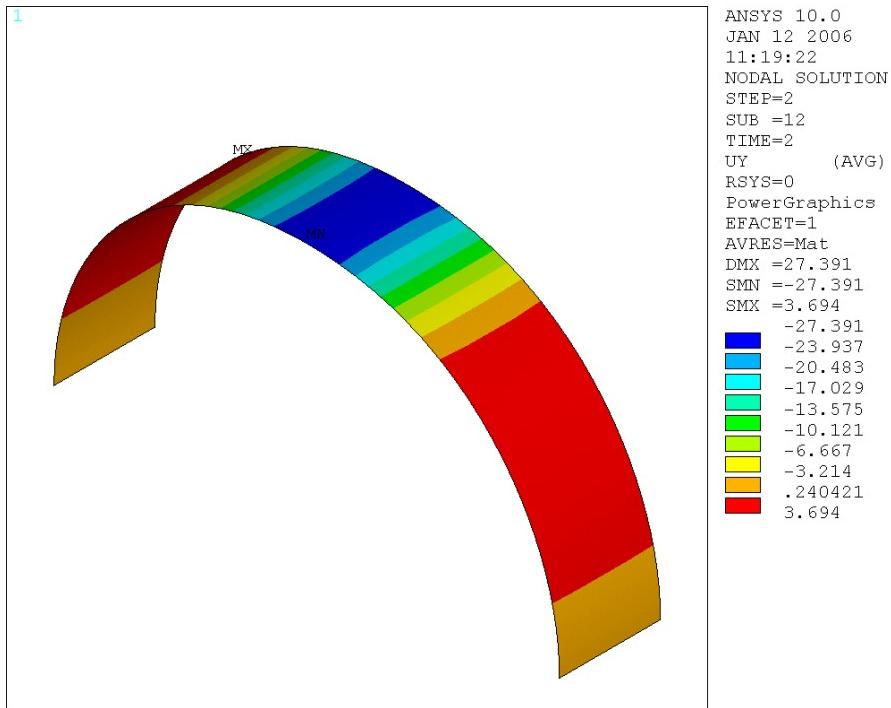
- Load step 1: self-weight Sand
- Load step 2: load

Reference solution: Example 5 - Calculation with LAW = 1 MOHR-COULOMB (bsp5.dat)



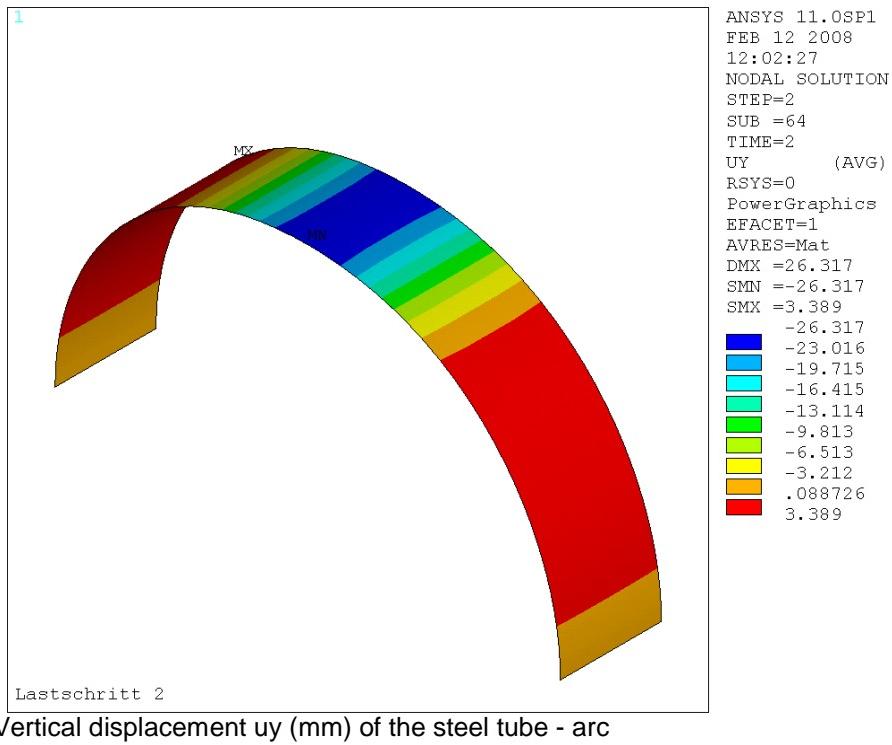
Vertical displacement  $uy$  (mm) of the steel tube - arc

Reference solution: Example 6 - Calculation with LAW = 40 DRUCKER\_PRAGER (bsp6.dat)

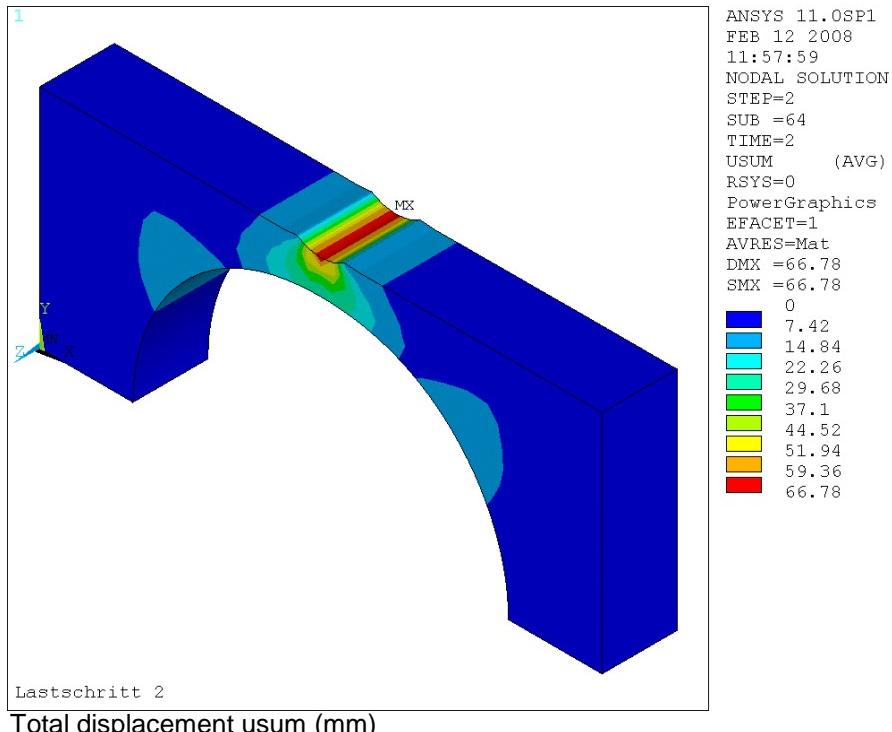


Vertical displacement  $uy$  (mm) of the steel tube - arc

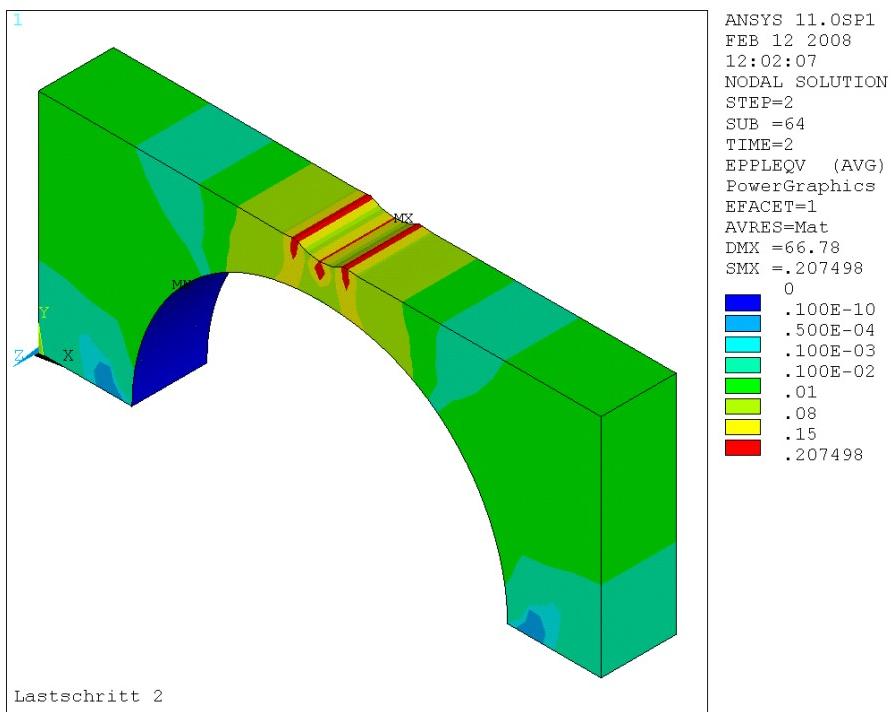
Reference solution: Example 7 - Calculation with LAW = 41 MOHR-COULOMB+DRUCKER-PRAGER  
(bsp7.dat)



Vertical displacement  $u_y$  (mm) of the steel tube - arc

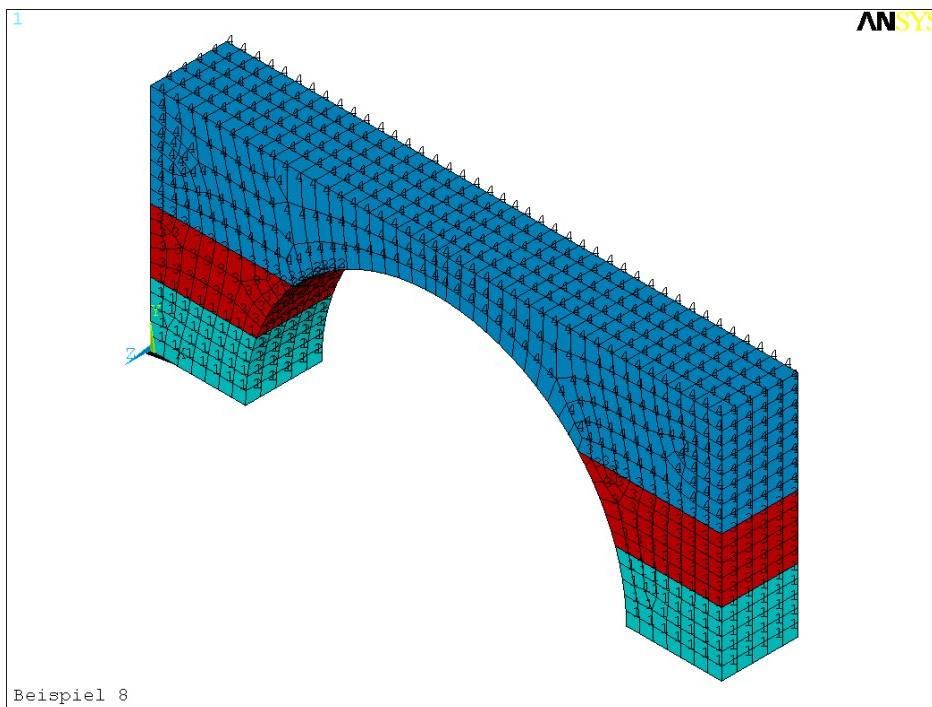


Total displacement  $u_{sum}$  (mm)



Equivalent plastic strain

Reference solution: Example 8 - Calculation with LAW = 40 DRUCKER-PRAGER (bsp8.dat)



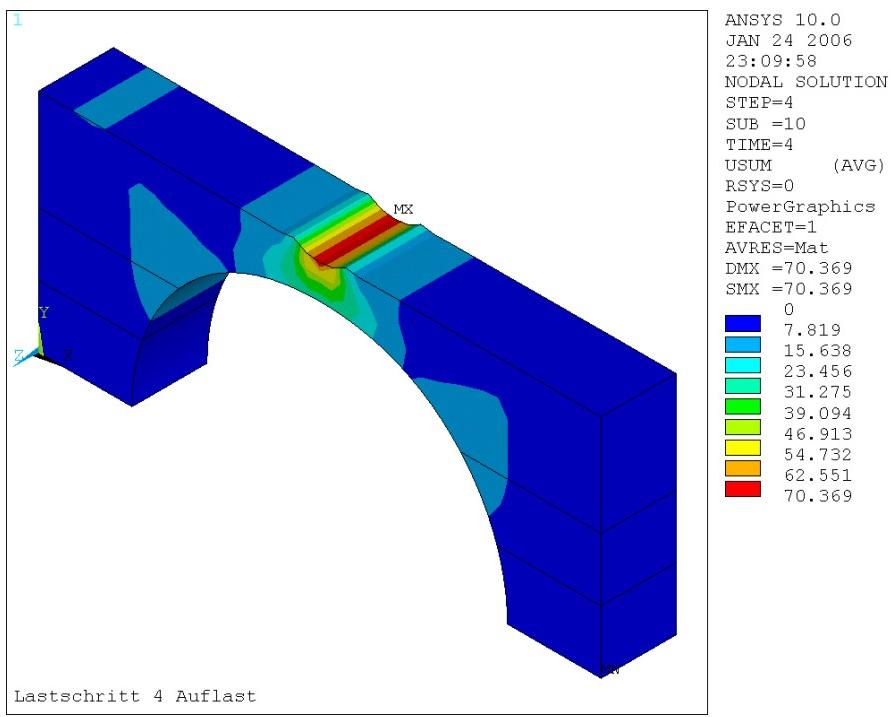
FE-Model

**\*\*Load history**

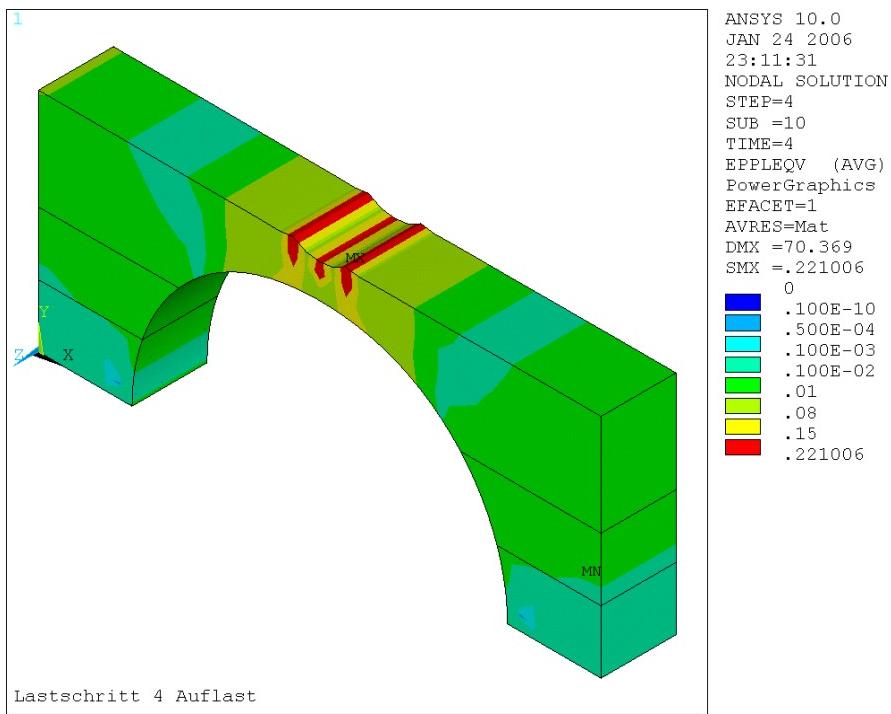
Load step 1: Self-weight, Installation layer MAT1, steel tube – arc, stiffened  
 Load step 2: Self-weight, Installation layer MAT3, steel tube – arc, stiffened  
 Load step 3: Self-weight, Installation layer MAT4, steel tube – arc, stiffened  
 Load step 4: Load



Vertical displacement  $u_y$  (mm) of the steel tube - arc



Total deformation usum (mm)

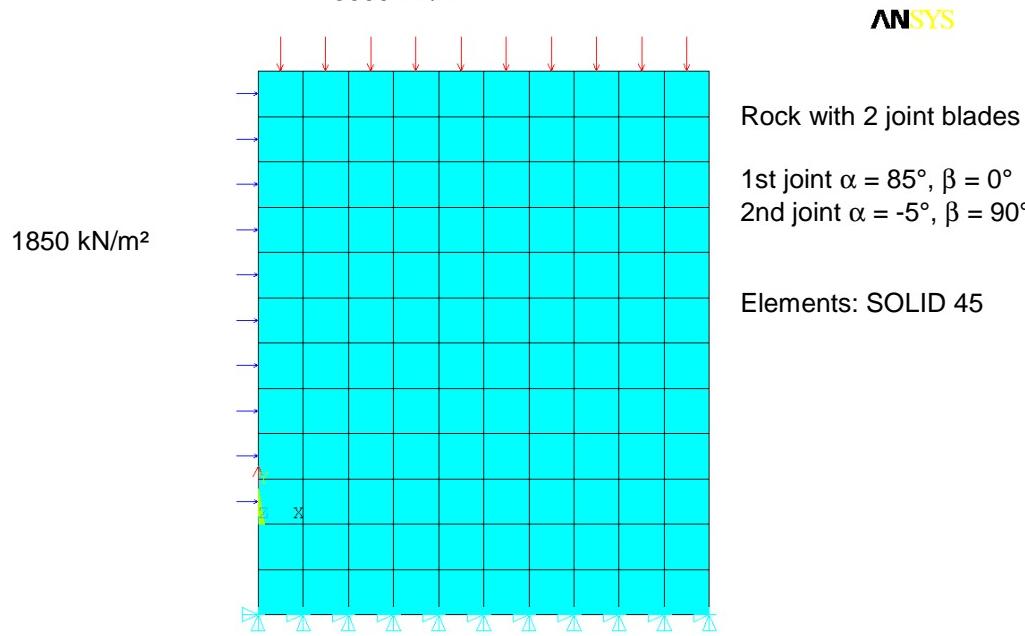


Equivalent plastic strain

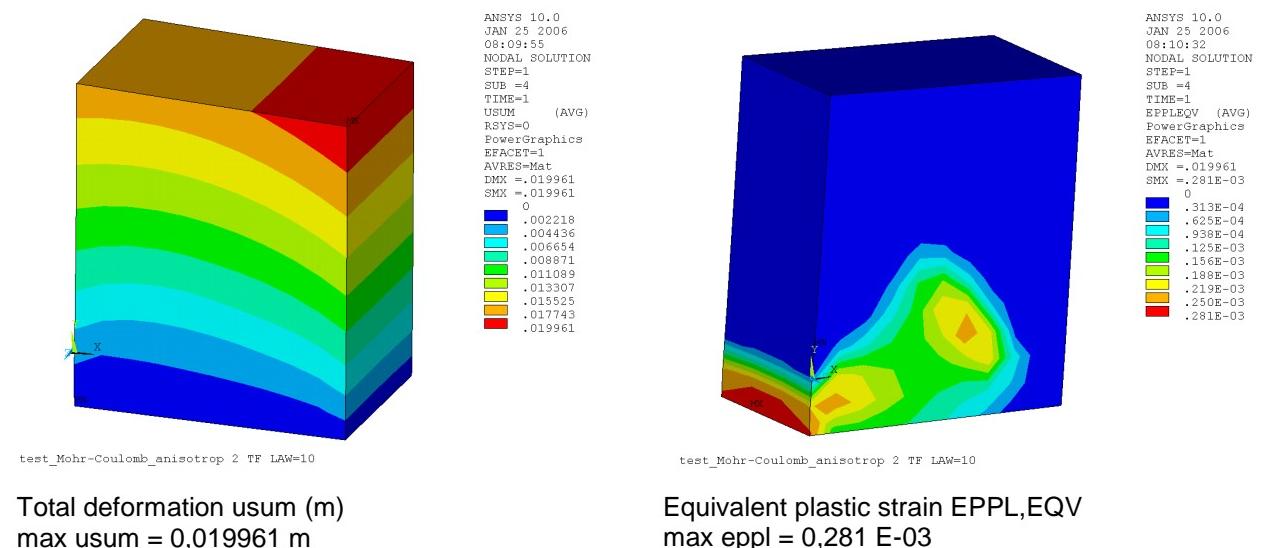
## 5.4 Example 9 - MOHR-COULOMB anisotropic

(bsp9.dat)

3000 kN/m<sup>2</sup>



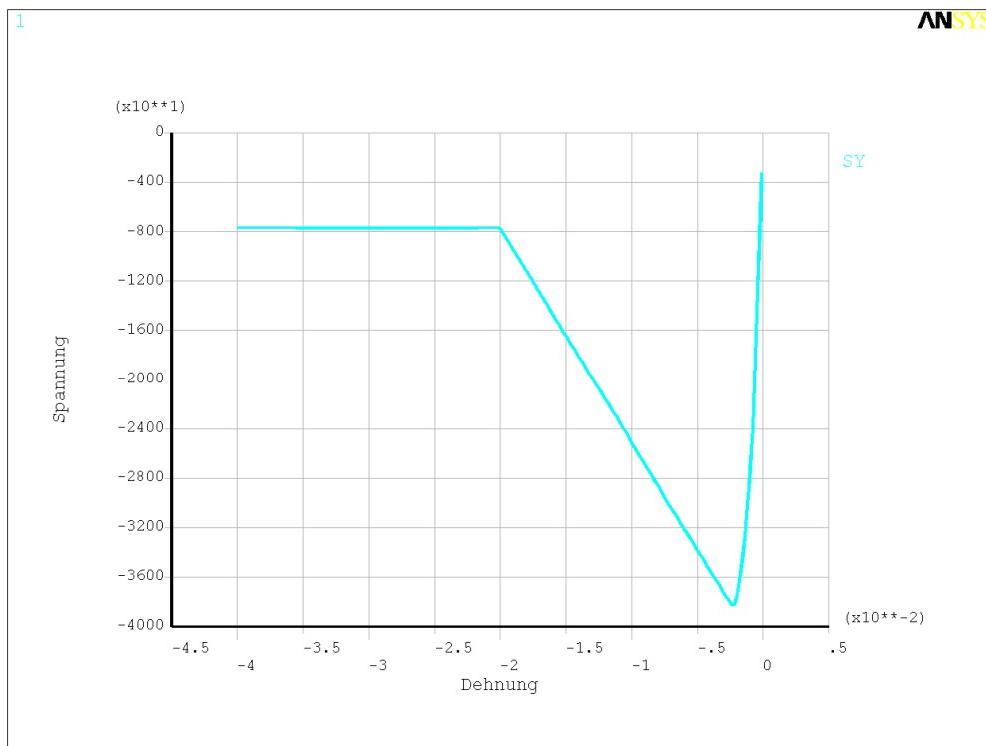
test\_Mohr-Coulomb\_anisotrop 2 TF LAW=10  
FE-model



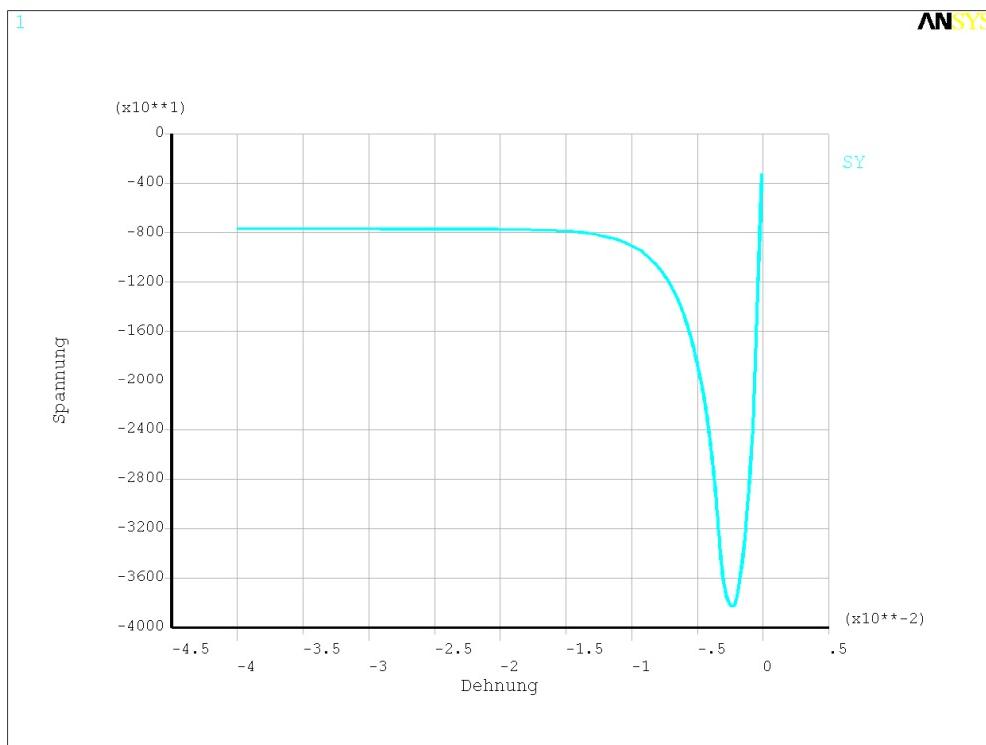
## 5.5 Example 10 – Concrete-model DRUCKER-PRAGER singular (LAW=9)

(eld.dat)

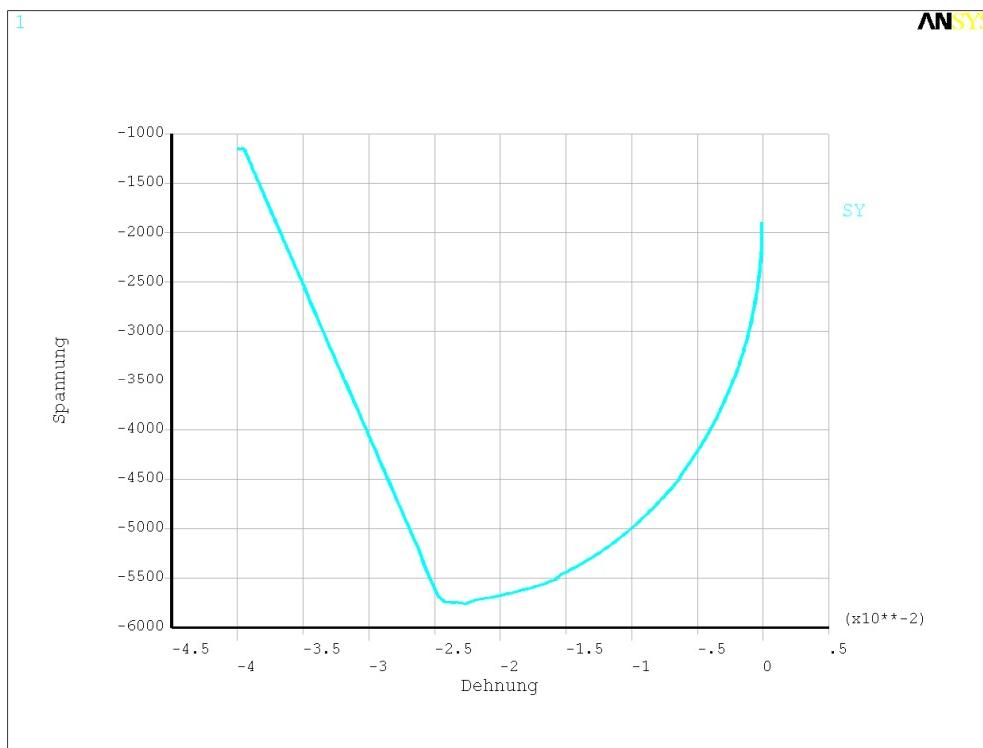
Uniaxial compressive tests:



Stress-strain diagram 20°C, mlaw = 0



Stress-strain diagram 20°C, mlaw = 1

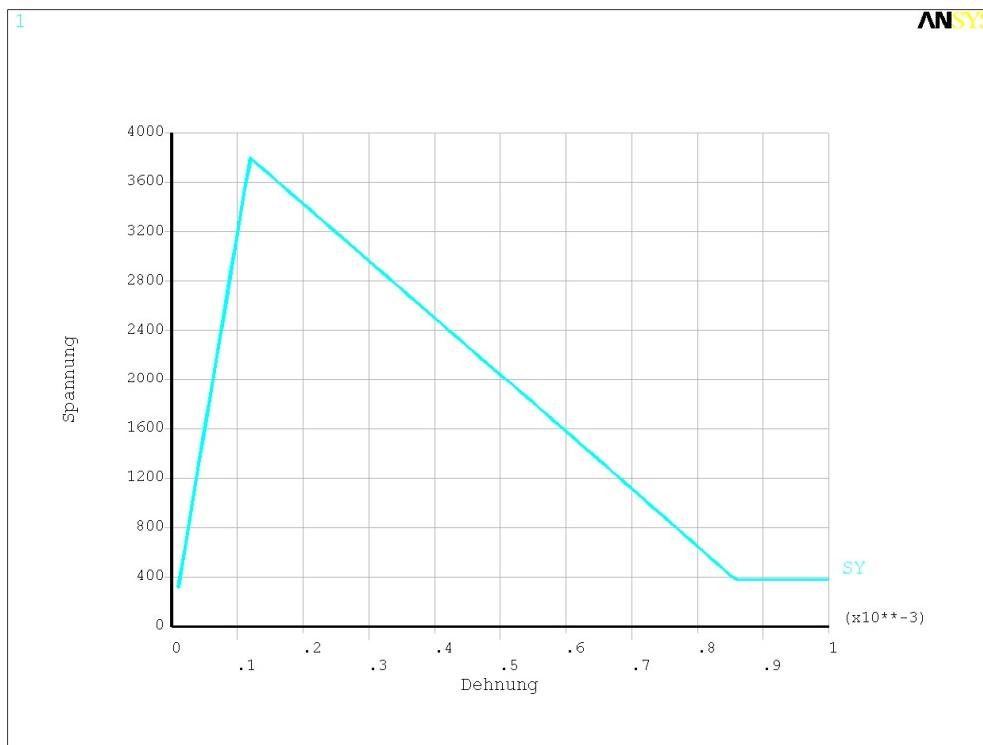


Stress-strain diagram 800°C, mlaw = 0

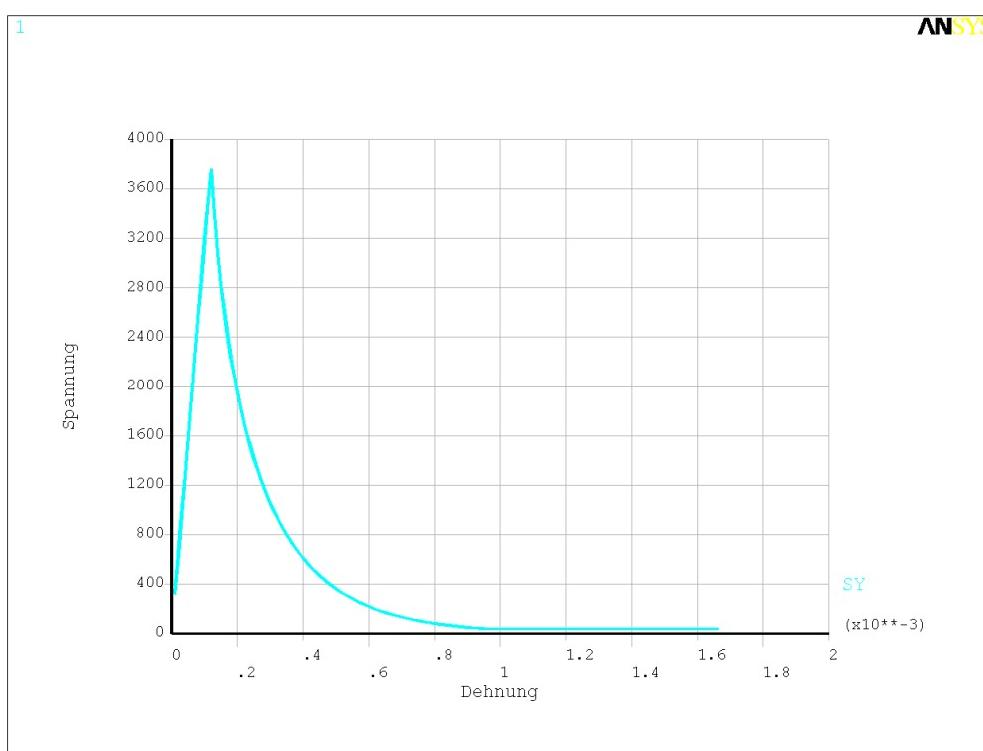
## 5.6 Example 11 – Concrete-model DRUCKER-PRAGER singular (LAW=9)

(elz.dat)

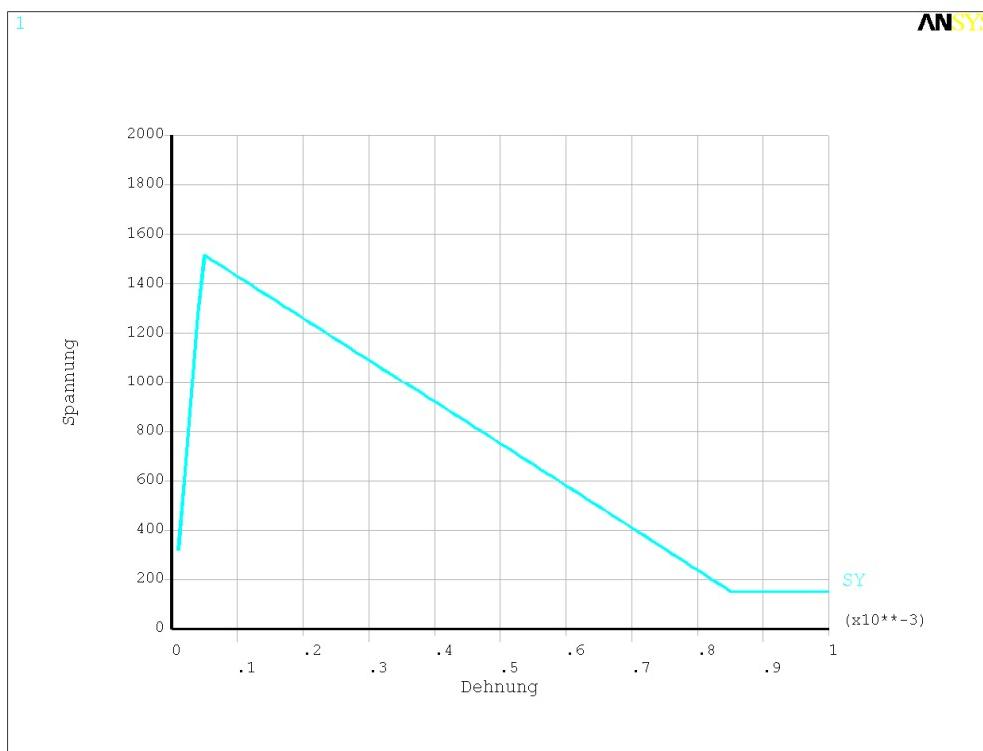
Uniaxial tensile tests:



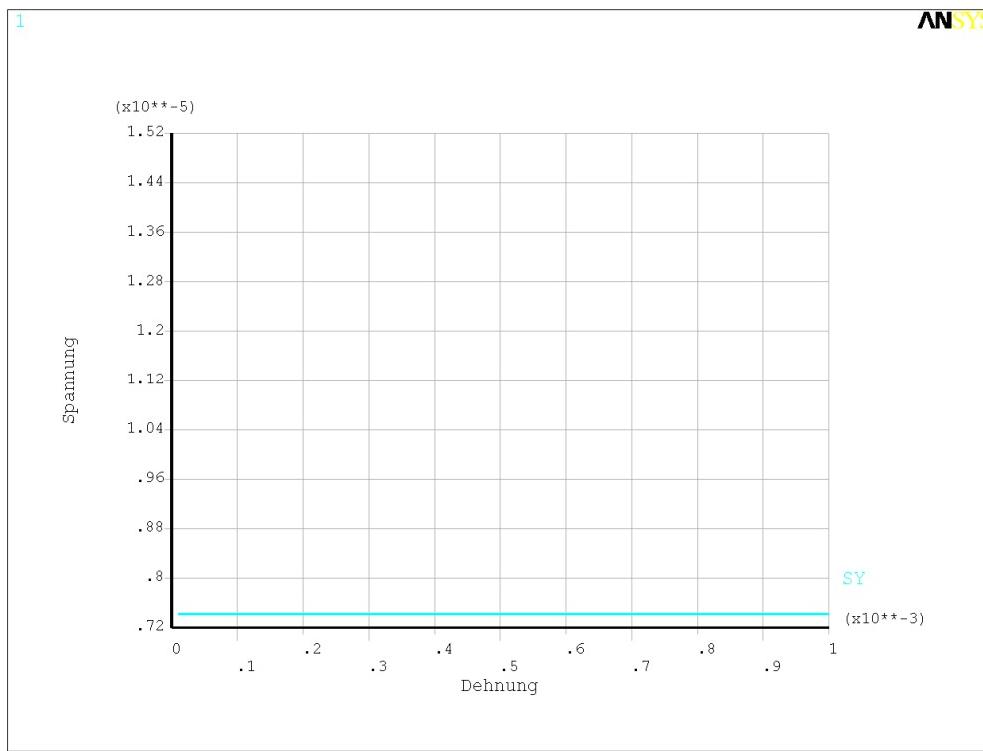
Stress-strain diagram 20°C, mlaw = 0



Stress-strain diagram 20°C, mlaw = 1



Stress-strain diagram 400°C, mlaw = 0

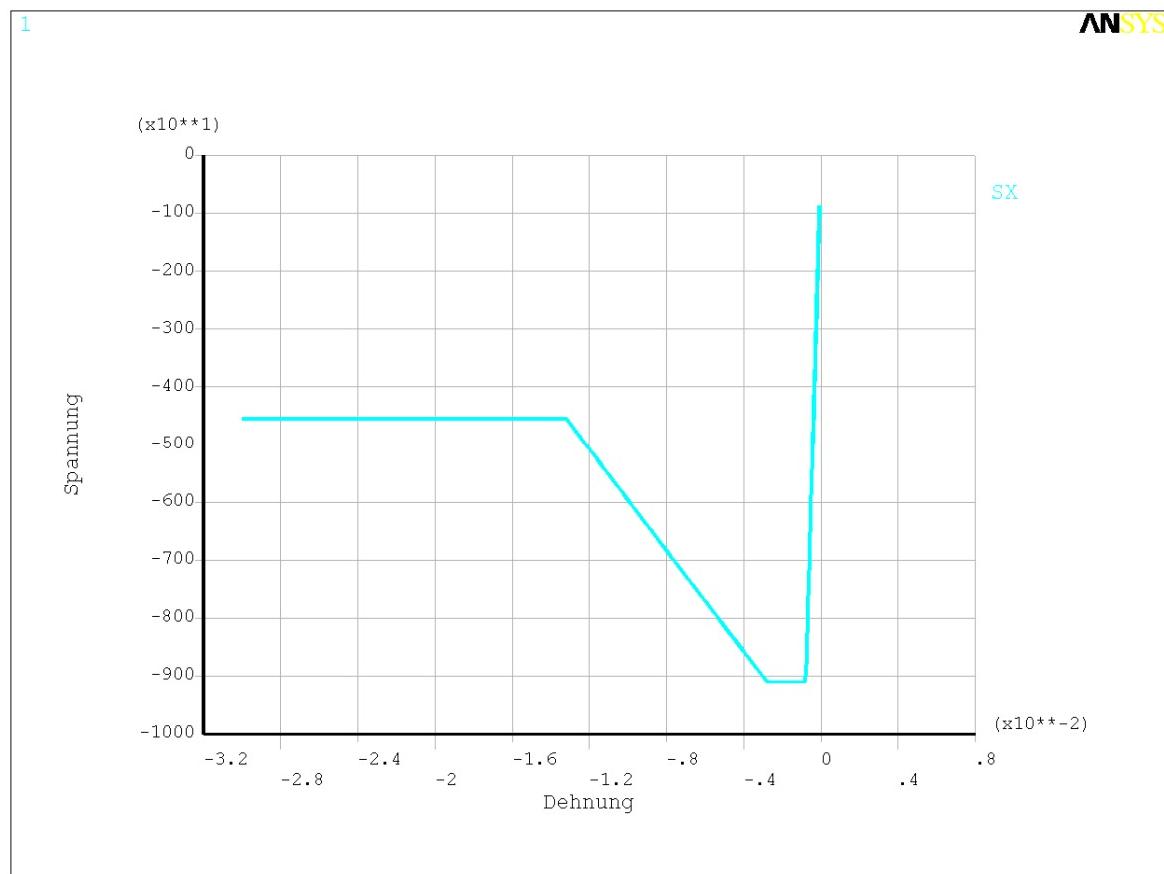


Stress-strain diagram 800°C, mlaw = 0

## 5.7 Example 12 – Masonry-model with softening (LAW=20)

(eld.dat)

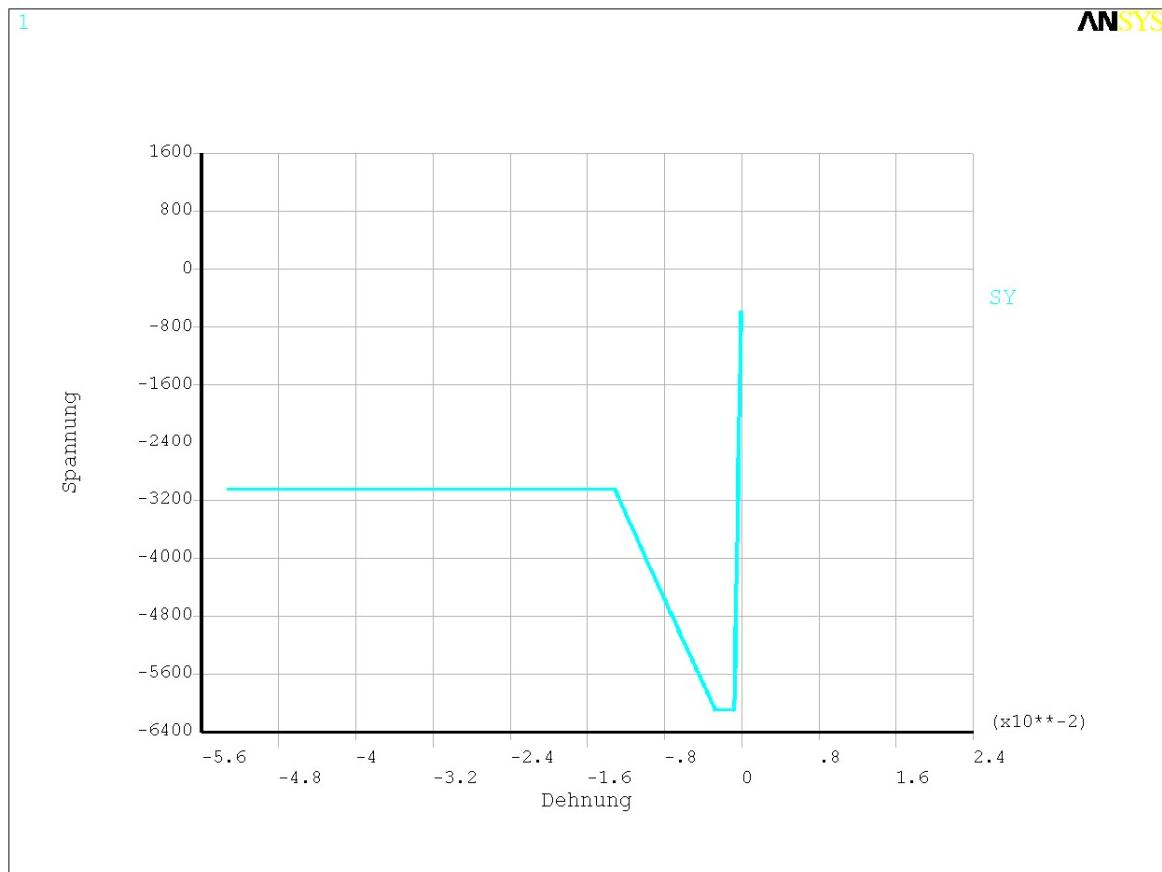
Uniaxial compressive test, vertical:



## 5.8 Example 13 – Masonry-model with softening (LAW=20)

(eld.dat)

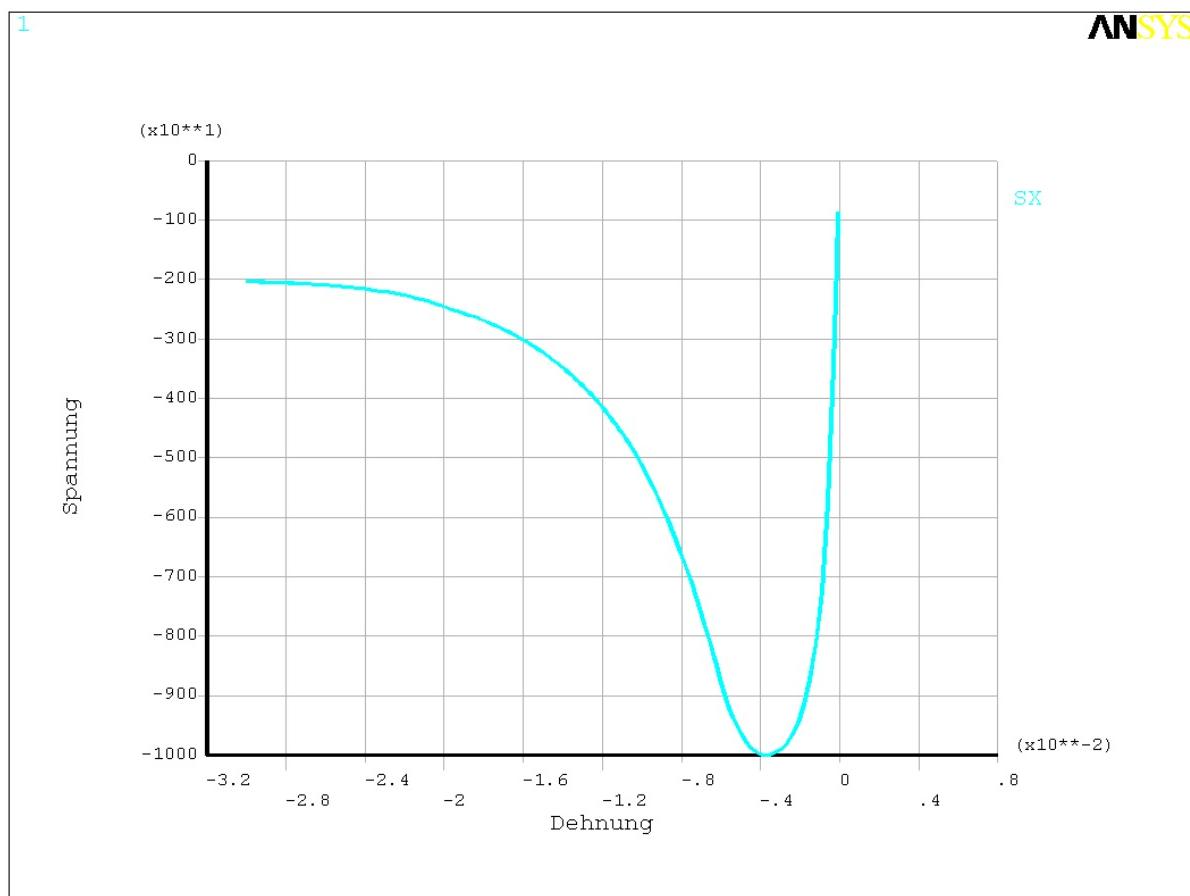
Uniaxial compressive test, horizontal:



## 5.9 Example 14 – Masonry-model with hardening and softening (LAW=22)

(eld.dat)

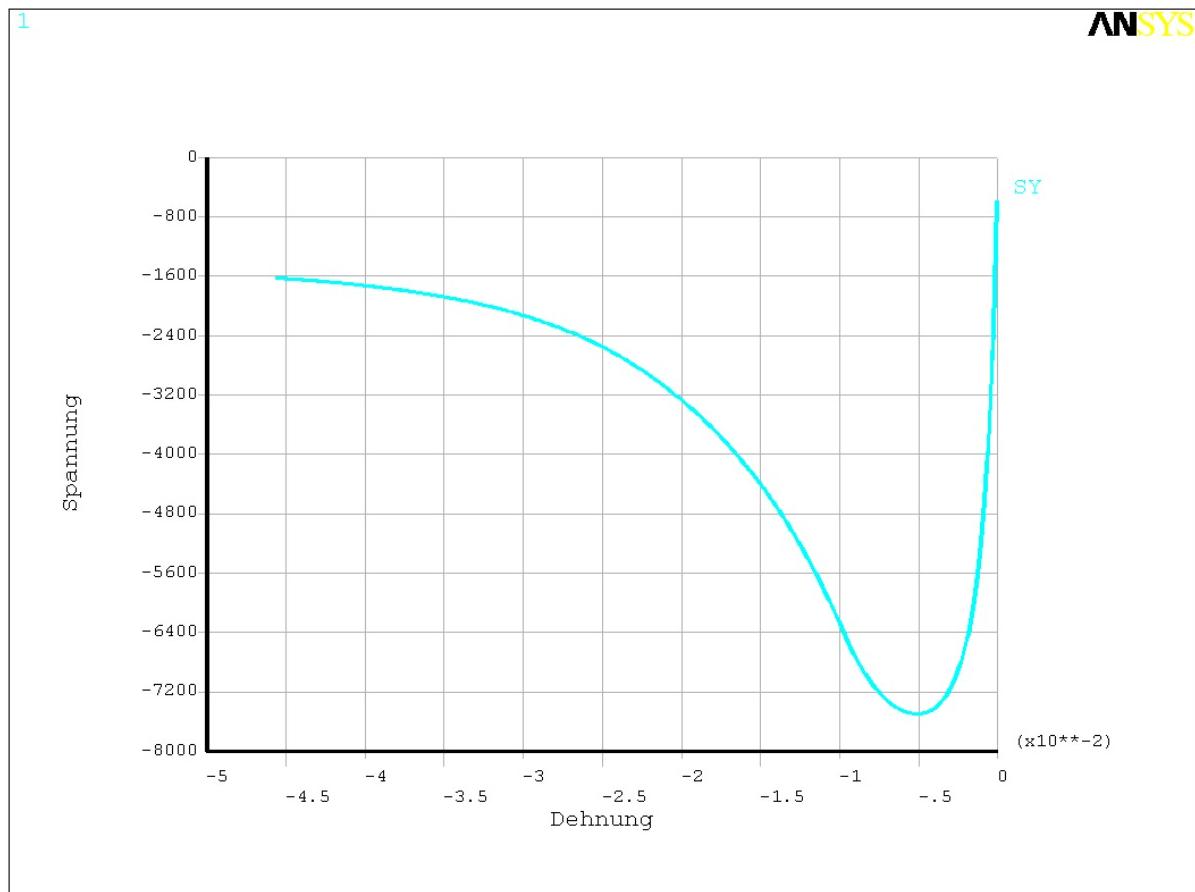
Uniaxial compressive test, vertical:



## 5.10 Example 15 – Masonry-model with hardening and softening (LAW=22)

(eld.dat)

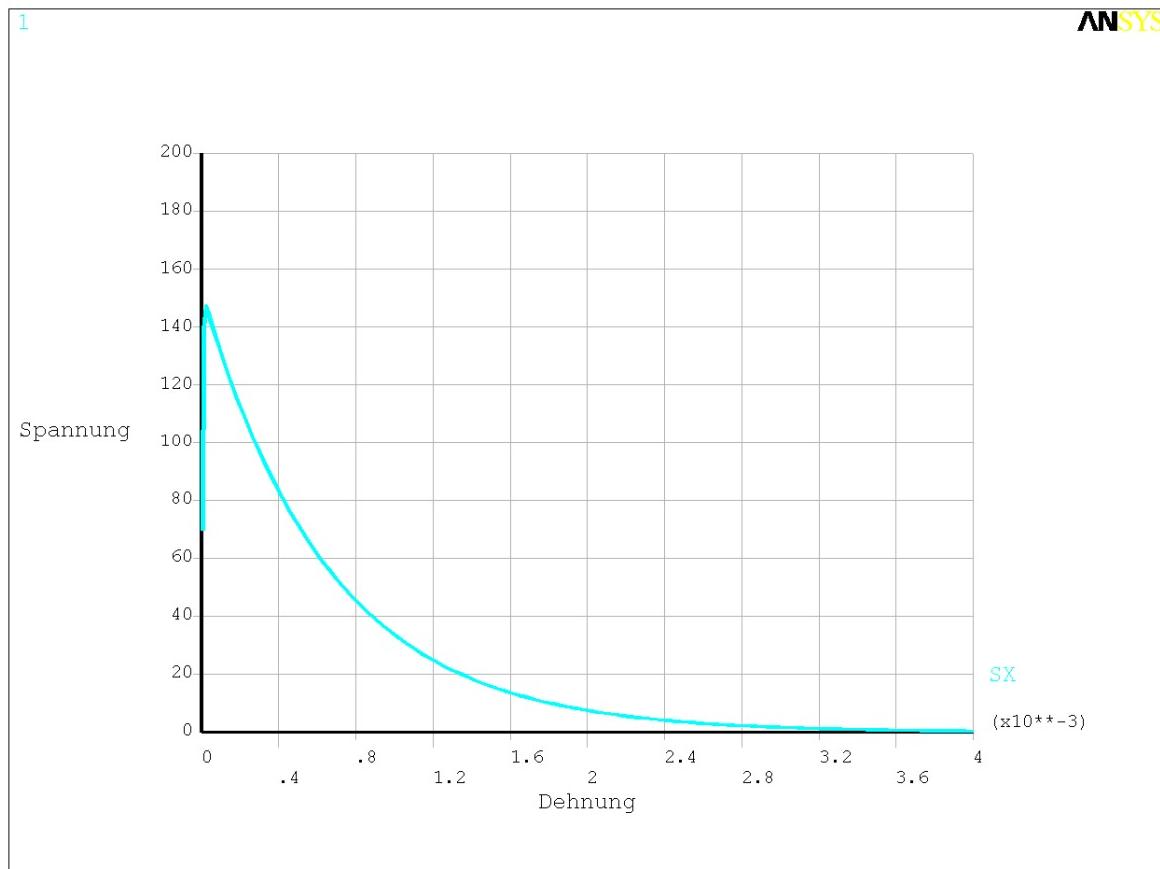
Uniaxial compressive test, horizontal:



## 5.11 Example 16 – Masonry-model with hardening and softening (LAW=22)

(elz.dat)

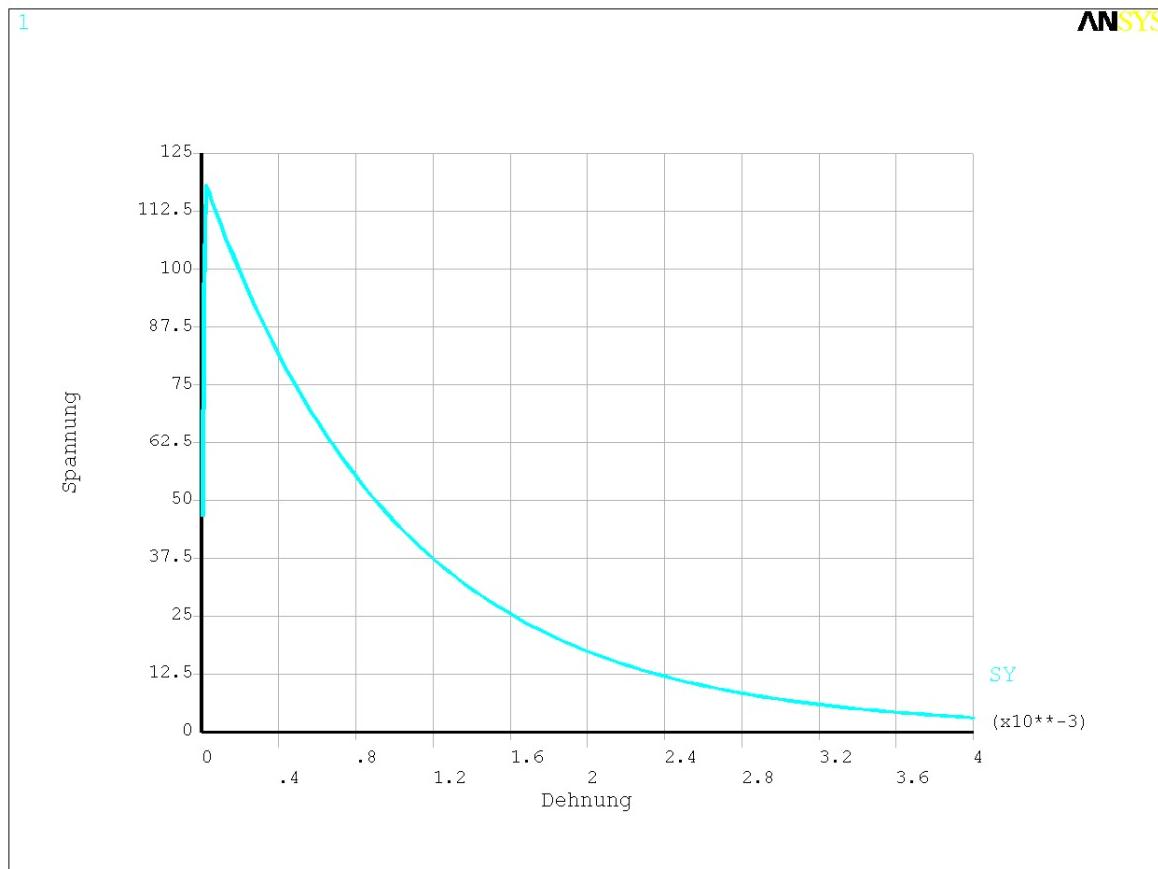
Uniaxial tensile test, vertical:



## 5.12 Example 17 – Masonry-model with hardening and softening (LAW=22)

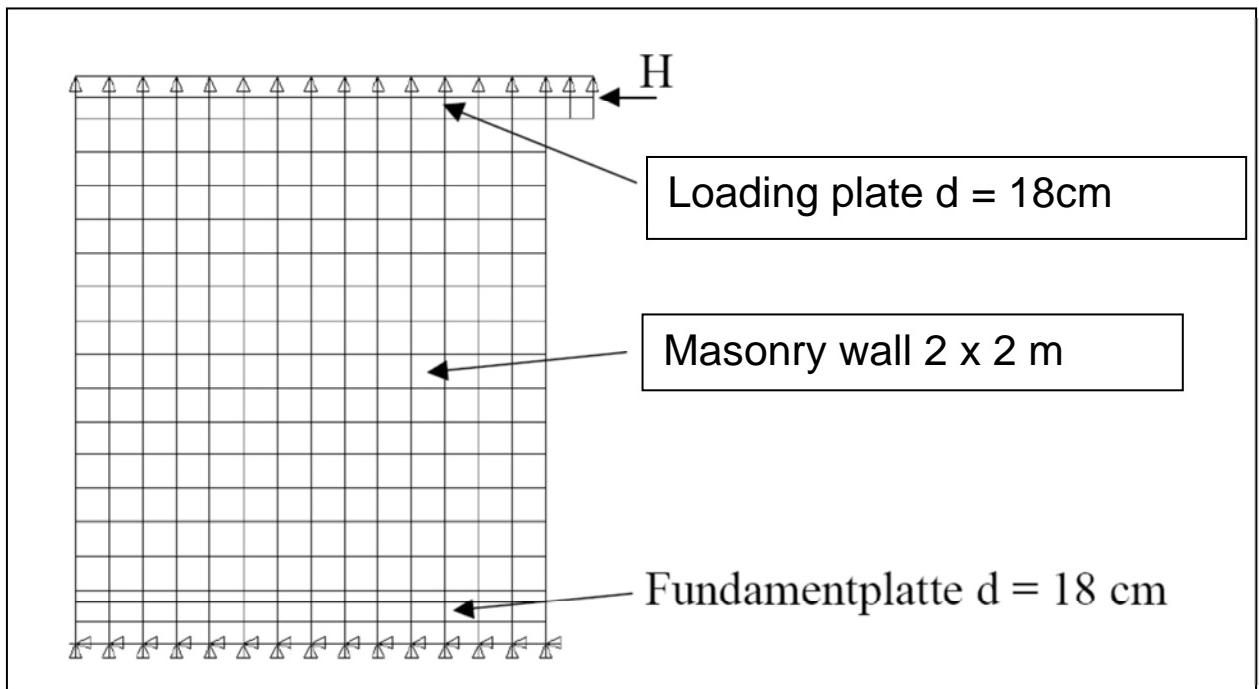
(elz.dat)

Uniaxial tensile test, horizontal:

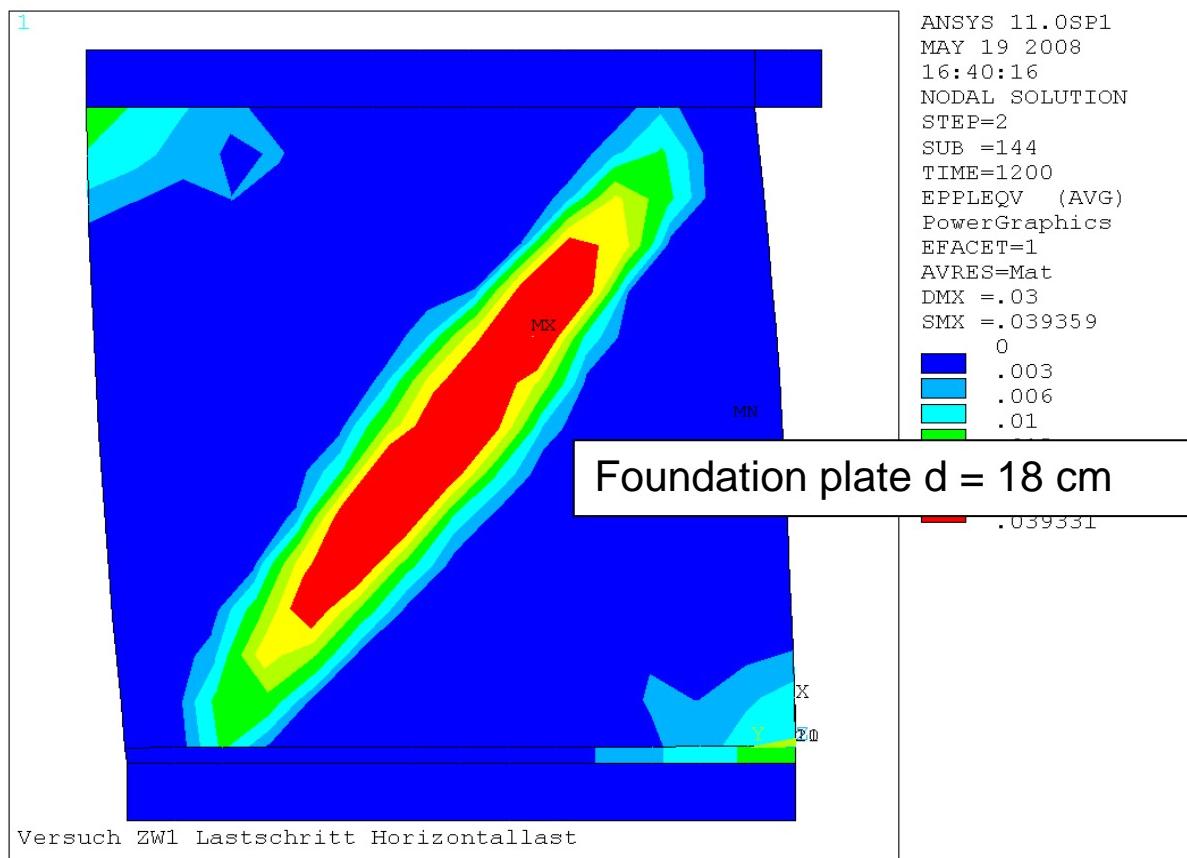


## 5.13 Example 18 – Masonry-model (LAW=20) shear test 1

Benchmark test according to [6-17], S.140f.

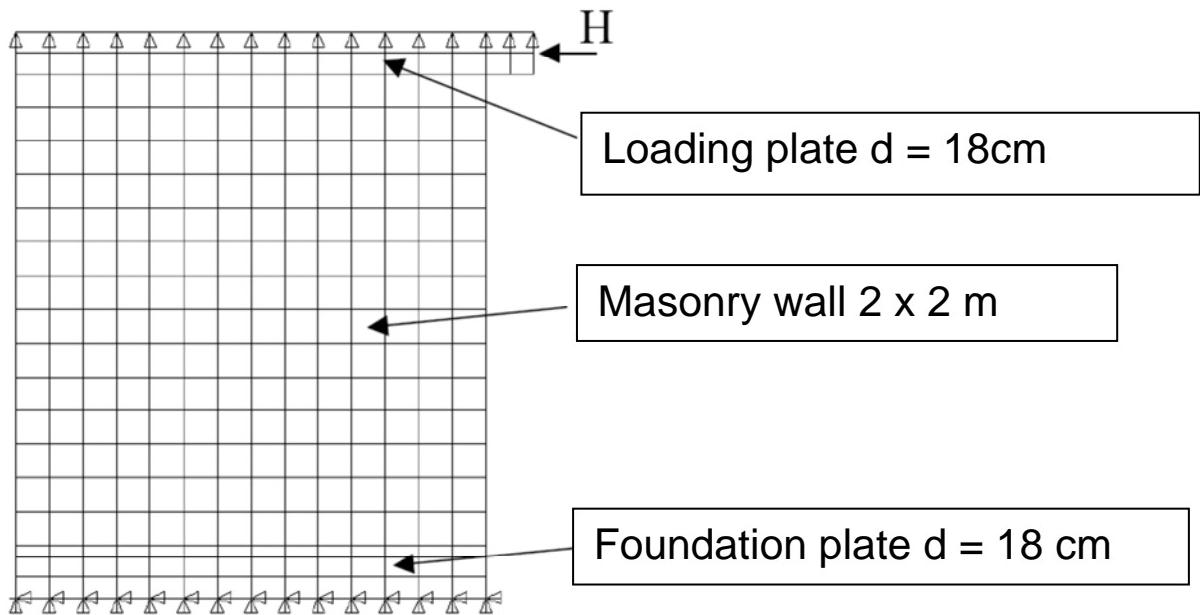


Stone format: 40x20

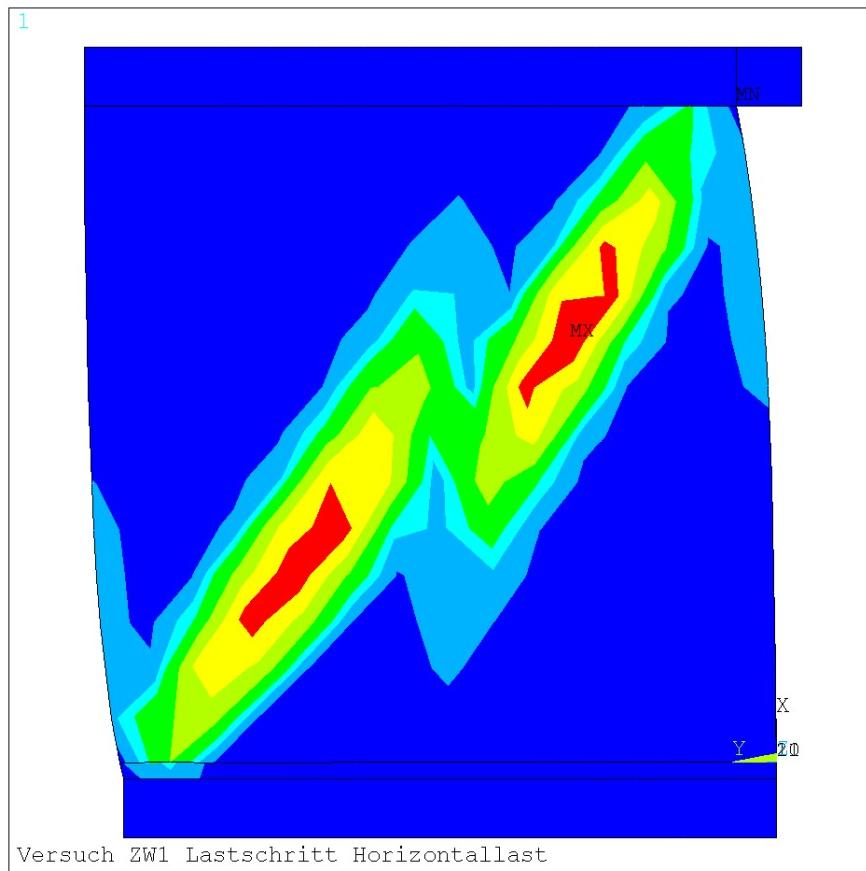


## 5.14 Example 19 – Masonry-model (LAW=20) Shear test 2

Benchmark test according to [6-17], S.140f.

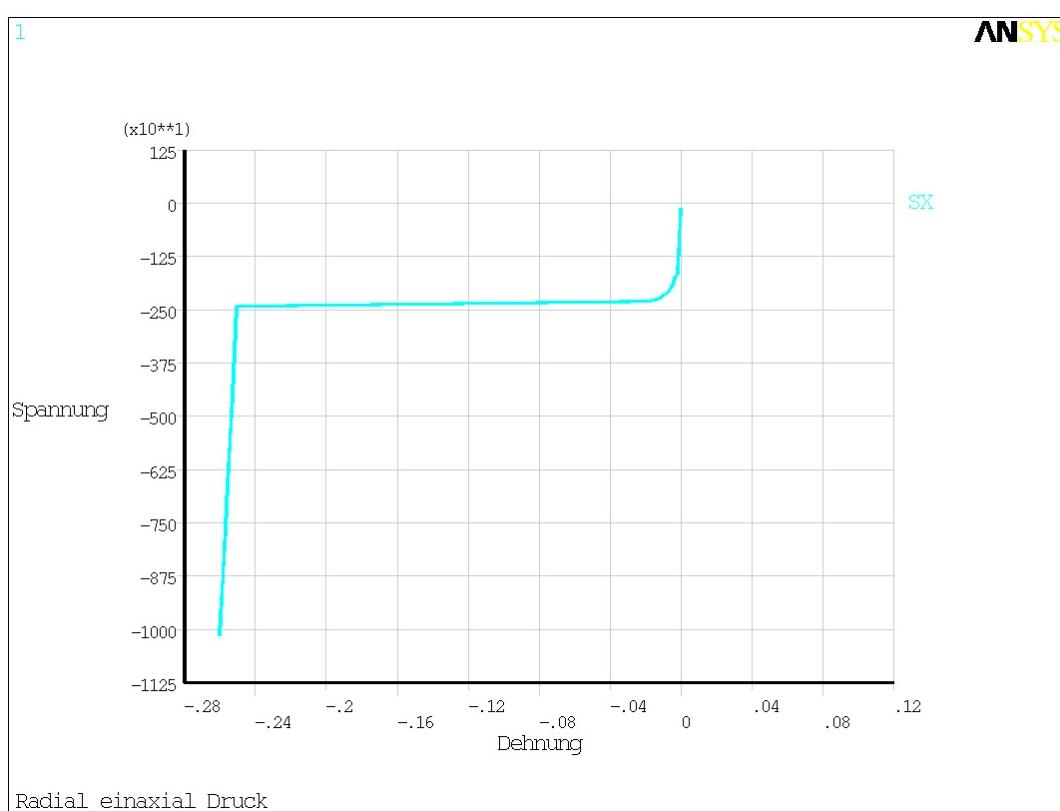
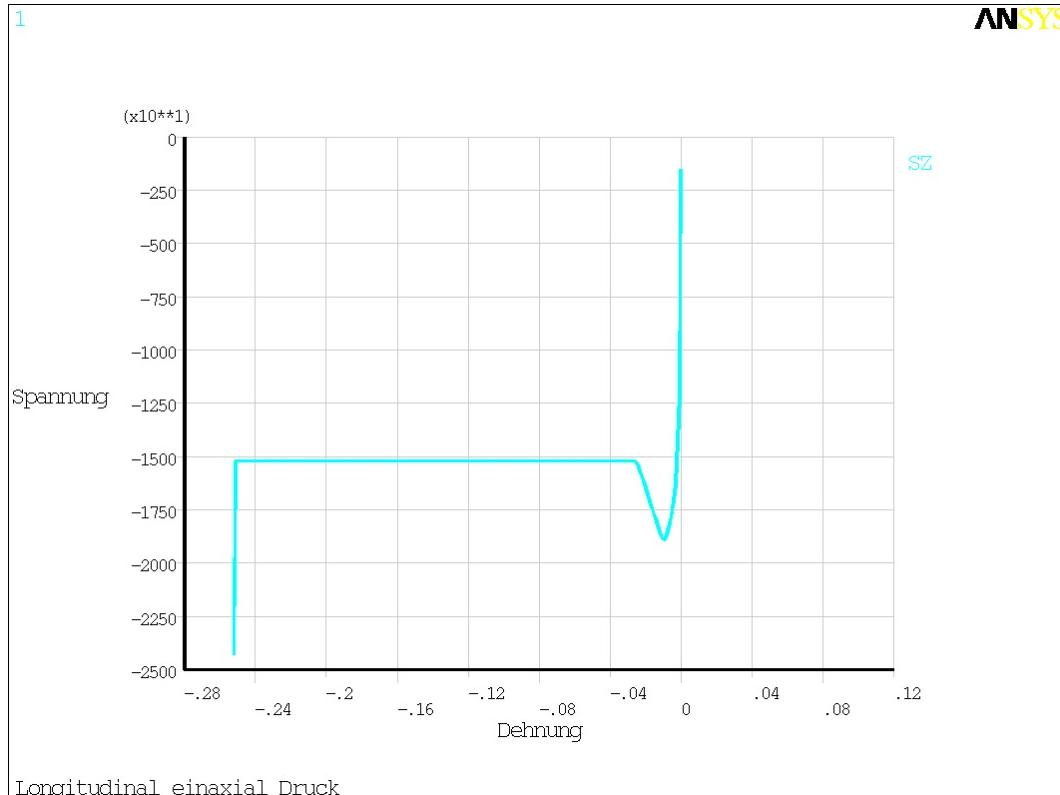


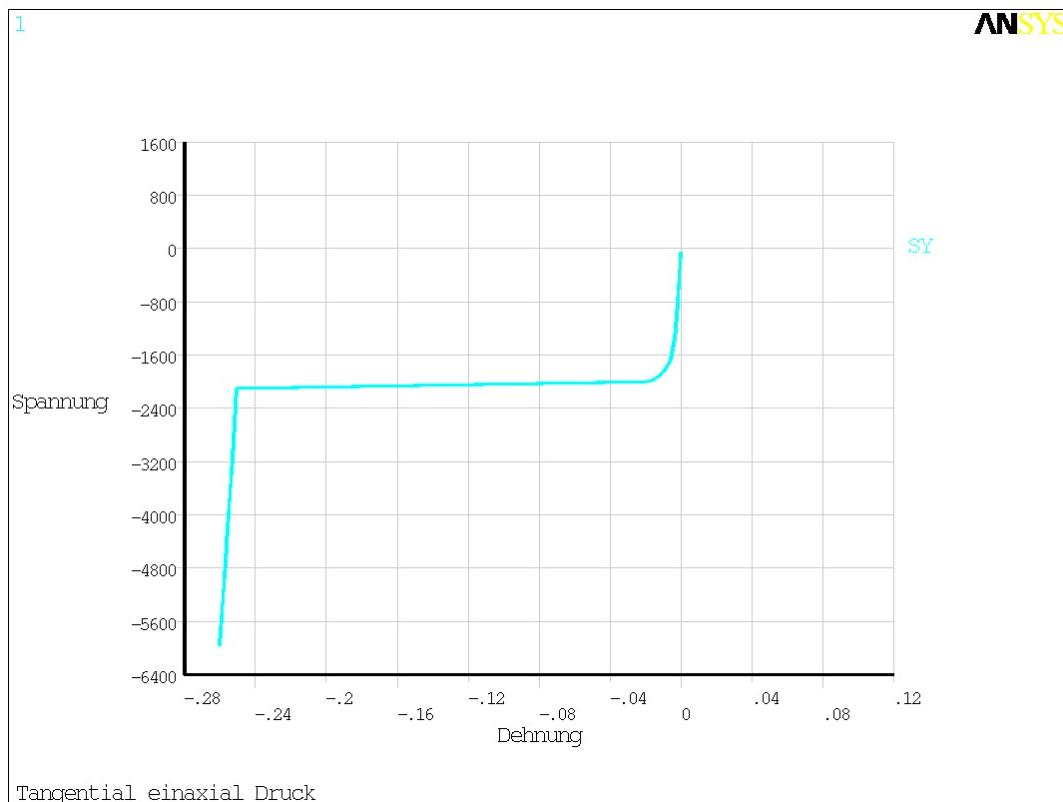
Stone format 20x20



## 5.15 Example 20 – Wood-model (LAW=33) uniaxial compressive tests

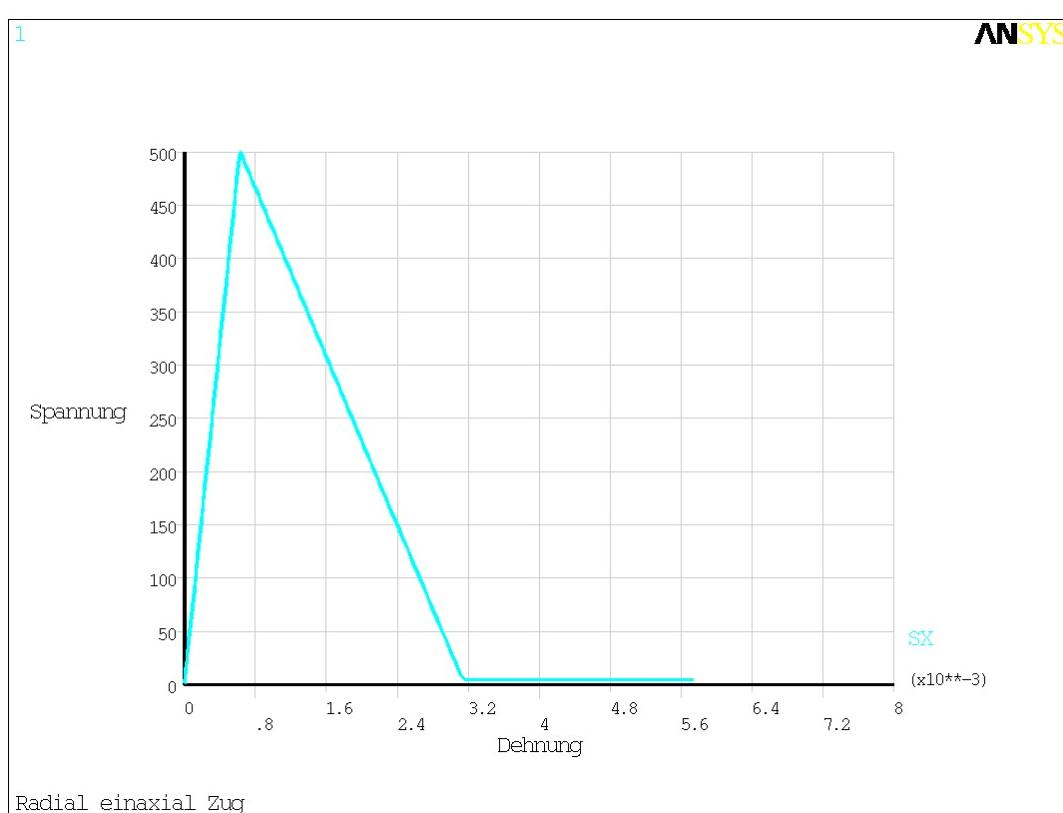
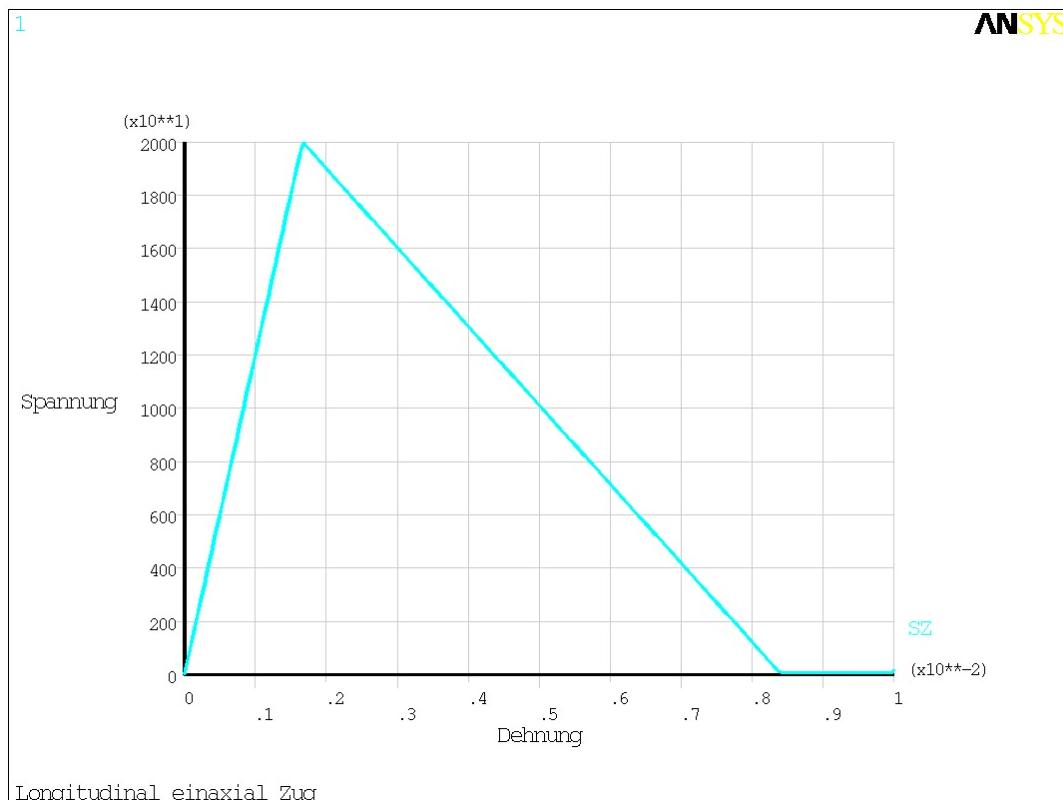
(el\_test\_holz33.dat)

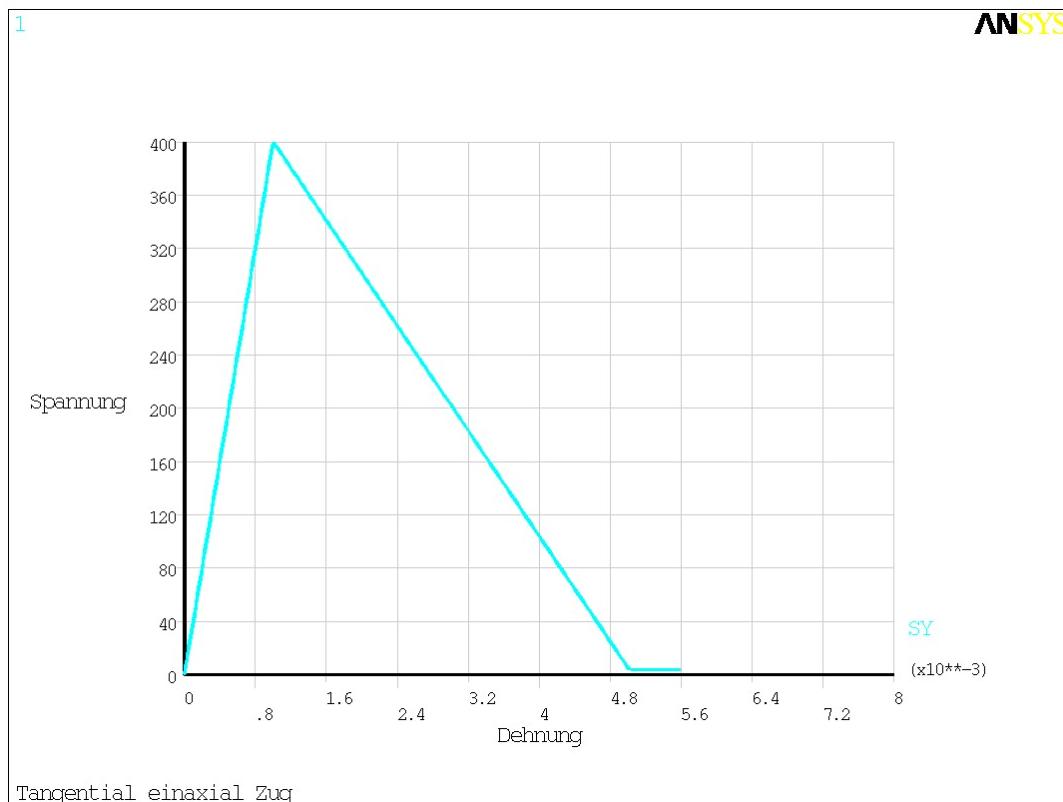




## 5.16 Example 21 – Wood-model (LAW=33) uniaxial tensile tests

(el\_test\_holz33.dat)

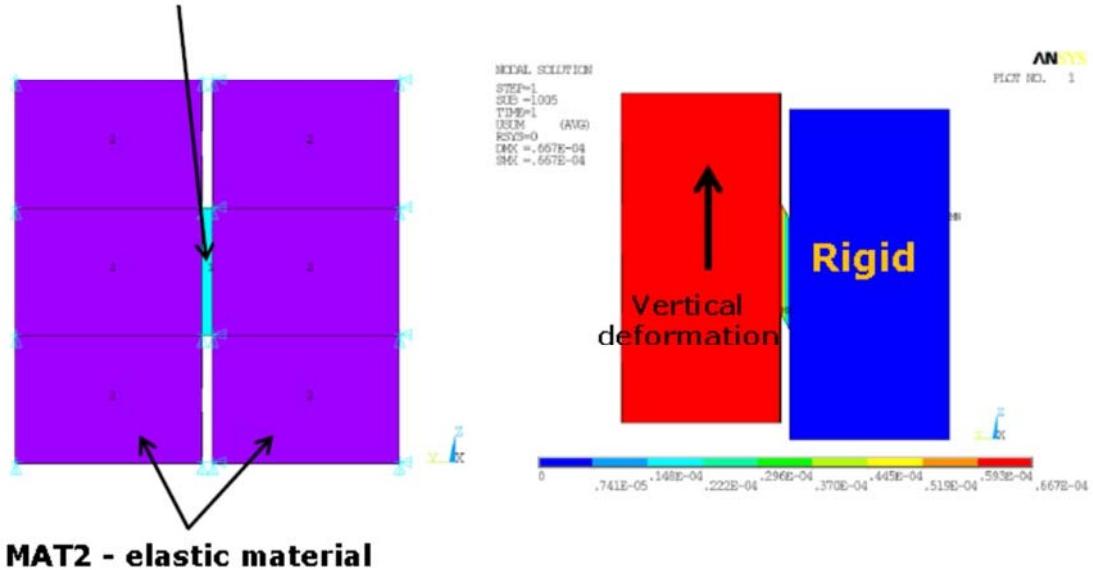




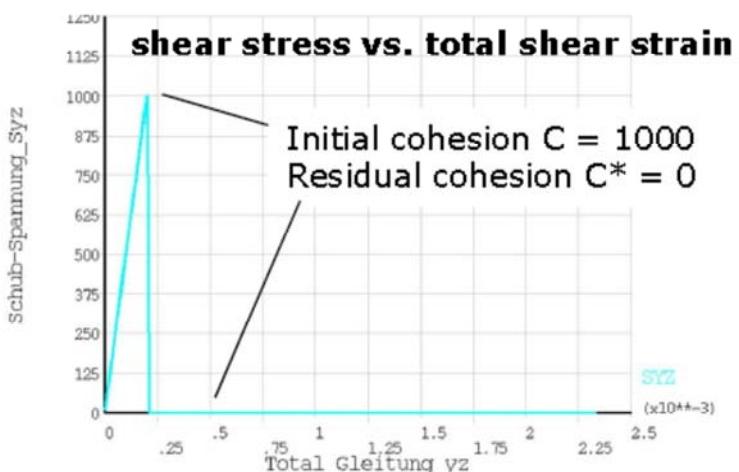
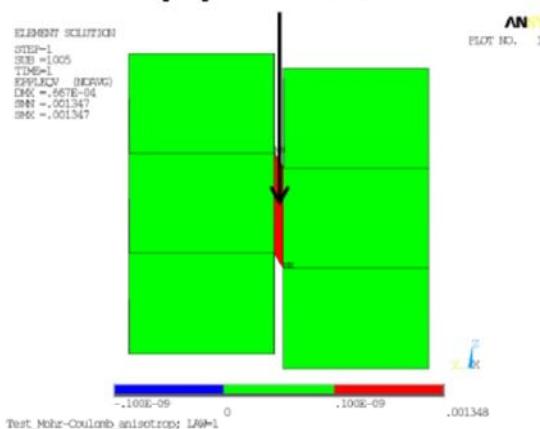
## 5.17 Example 22 – Single Joint Shear-Test (LAW=1, 10)

(bsp22.dat)

**MAT1 - multiPlas material  
LAW1**



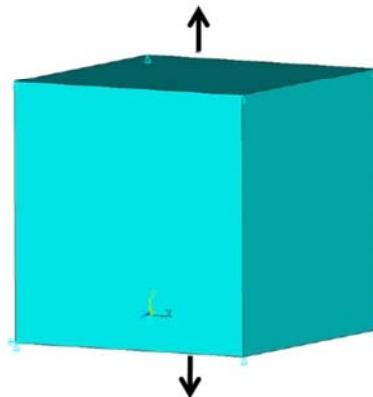
**eqv plastic strains**



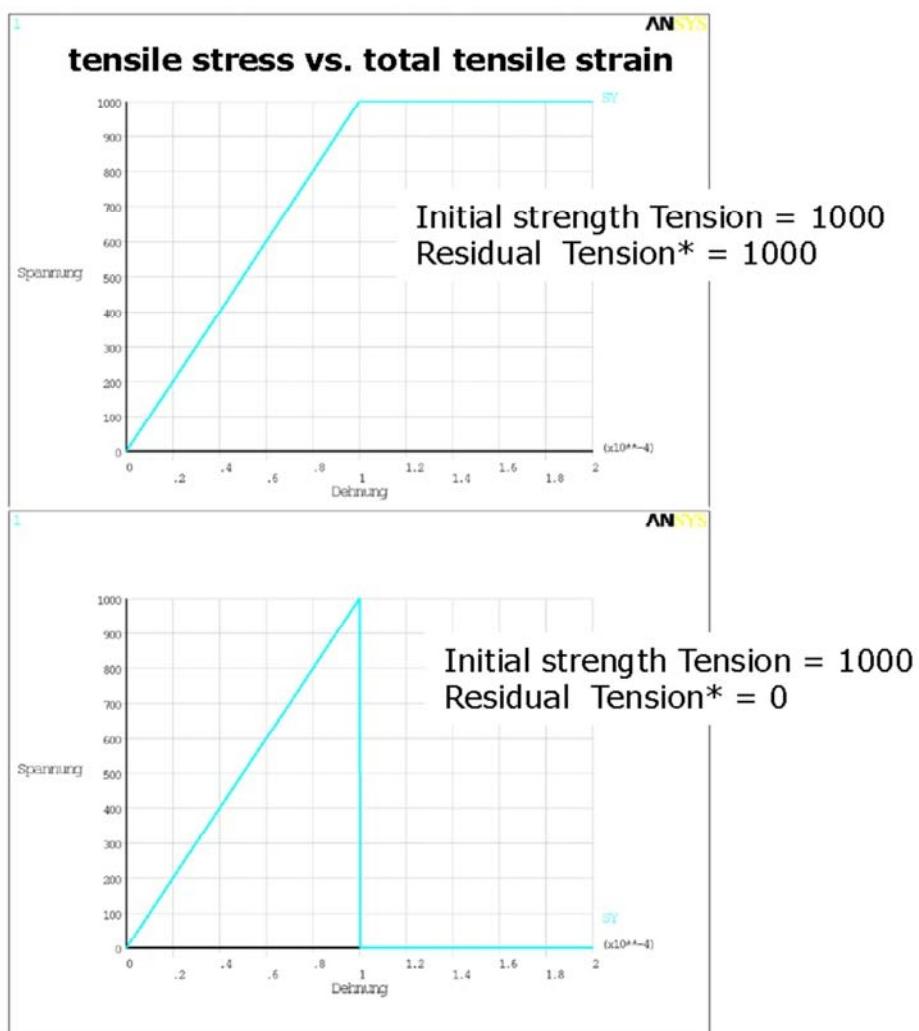
## 5.18 Example 23 – Single Joint Tensile-Test (LAW=1, 10)

(elz.dat)

**MAT1 - multiPlas material  
LAW1**



**single element under  
uniaxial tension load**



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- 
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## 7 APENDIX USER INFERFACE - USERMPLS

### 7.1.1 LAW = 99 – User-Material

| Feld            | 1    | 2     | 3   | 4    | 5     | 6      | 7     | 8      | 9    | 10     |
|-----------------|------|-------|-----|------|-------|--------|-------|--------|------|--------|
| 0-10<br>isotrop | LAW  | up1   | ... |      |       |        |       |        |      |        |
| 11-20<br>1.TF   |      |       |     |      |       |        |       |        |      |        |
| 21-30<br>2.TF   |      |       |     |      |       |        |       |        |      |        |
| 31-40<br>3.TF   |      |       |     |      |       |        |       |        |      |        |
| 41-50<br>4.TF   |      |       |     |      |       |        |       |        |      |        |
| 51-60           |      |       |     |      |       |        |       |        | up58 | wr     |
| 61-70           | Elem | Intpt | eps | geps | maxit | cutmax | dtmin | maxinc |      | ktuser |
| 71-80           |      |       |     |      |       |        |       |        |      |        |

up1 – 58 - free definable material parameters

### 7.1.2 Requirements of ANSYS (Release 13)

[Installation Guides](#) | [ANSYS, Inc. Windows Installation Guide](#) |

**Table 2.1 Operating System Requirements**

| Platform/OS  | ANSYS/Workbench Compilers*  |
|--|---|
| Intel EM64T, AMD64 / Windows XP<br>x64 Edition Version 2003<br>Intel EM64T, AMD64/Windows Vista<br>x64 | Intel Fortran v10.1<br>Microsoft Visual Studio 2005<br>Professional Edition |
| Intel IA-32 bit / Windows XP (Build<br>2600) Version 5.1<br>Intel IA-32 bit / Windows Vista            | Intel Fortran v10.1<br>Microsoft Visual Studio 2005<br>Professional Edition |

\* Compilers are required only if you will be using User Programmable Features or other customization options.

### **14.1. User-Programmable Features (UPFs)**

User-programmable features (UPFs) are ANSYS capabilities for which you can write your own FORTRAN routines. UPFs allow you to customize the ANSYS program to your needs, which may be a user-defined material-behavior option, element, failure criterion (for composites), and so on. You can even write your own design-optimization algorithm that calls the entire ANSYS program as a subroutine. UPFs are available in the ANSYS Multiphysics, ANSYS Mechanical, ANSYS Structural, ANSYS PrepPost, and ANSYS Academic (Associate, Research, Teaching Advanced, and Teaching Mechanical versions) products. For detailed information, see the *Guide to ANSYS User Programmable Features*.

#### **7.1.3 User materials in multiPlas**

The user interface „usermpls“ is in the actual version multiPlas Release 2.0 a non-sufficient tested  $\beta$ -Feature. This interface offers the user a personal enhancement of the material library multiPlas in ANSYS.

The results of own implementations are in the responsibility of the user.

```

SUBROUTINE usermpls (LAW,up,F,DF,ka,eppli,FK,DK,nfail,eps,ncomp,
X           sigtr,sigm,sigdev,inv2,inv3,sigs,ta0,iott,wr)
c
c *** User definierte (mehrflaechige) Fliessbedingung in multiplas
c *** mehrflaechige Fliessbedingung mit max. 18 Flieskriterien
c *** Basis: userpl
c
c   input arguments:
c     variable (type,sze,intent)      description
c
c     LAW      (int,sc,in)          - Materialmodell-Nr. hier =99
c     up       (dp,ar(58),in)        - tbdata-Input-Werte
c     eppli    (dp,ar(18,6),in)     - Vektor plastischer Dehnungskomponenten
c                               d. einz. Fliesskriterien
c     eps      (dp,sc,in)          - Abbruch-Toleranz f. F>0
c     sigtr   (dp,ar(ncomp),in)     - Trial-Spannungsvektor
c     sigm    (dp,sc,in)          - Hydrostat. Spannung
c     sigdev  (dp,ar(6),in)         - Deviatorspannung
c     inv2    (dp,sc,in)          - J2 zweite Deviatorinvariante
c     inv3    (dp,sc,in)          - J3 dritte Deviatorinvariante
c     ta0     (dp,sc,in)          - ta0=sqrt(2.0d0/3.0d0*inv2)
c     iott    (int,sc,in)          - Ausgabesteuerung
c     wr      (int,sc,in)          - Schalter fuer Ausgabeumfang
c
c   output arguments:
c     variable (type,sze,intent)      description
c
c     F       (dp,ar(18),out)        - Fliesskriterien
c     DF      (dp,ar(6,25),out)      - Partielle Ableitungen
c                               d. Fliesskriterien u. plast. Potentiale
c     ka      (dp,ar(5),inout)       - History-Variablen kappa
c                               (plast. Dehnungsanteile Ver-/Entfest.)
c     FK      (dp,ar(18),out)       - Partielle Ableitungen dF/dkappa
c     DK      (dp,ar(5,18),out)      - Partielle Ableitungen dkappa/dLambda
c     nfail   (int,sc,inout)        - Zaehler verletzter Fliesskriterien
c
c
c   INTEGER LAW,nfail,wr,iott
c   DOUBLE PRECISION up(58),F(18),DF(6,25),ka(5),eppli(18,6),
X   FK(18),DK(5,18),eps,sigtr(6),sigm,sigdev,inv2,inv3,sigs,ta0,
X   hyd
c
c *** Funktionen von ANSYS (s. ANSYS UPF-Programmers-Manual)
cc      EXTERNAL VZERO
c
c *** weitere erf. interne Variablen
c     DOUBLE PRECISION F1,ftx
c
c *** Bsp. fuer Kontrollausgabe (Entwickler-Mode)
cc     if (wr.ge.1) then
cc       write(iott,*)
cc       x '***** START usermpls *****'
cc     endif
c
c *** update strain-Softening parameter kappa
cc     ka(1)=ka(1)+eppli(1,1)
cc     Oftx=dexp(-h*ftx/G(1)*ka(1))
c
c *** Bsp. fuer Kontrollausgabe (Entwickler-Mode)
cc     if (wr.ge.4) then
cc       write (iott,*) '*** Kontrollausgabe Softeningfkt. in jexp ***'
cc       write (iott,2000) Oftx
cc       write (iott,2010) (ka(1))
cc     endif
cc2000  format('2000 Oftx ',1(1x,F14.7))
cc2010  format('2010 kappa(1) = ',1(1x,1pe14.7))
c
c *** Abfrage Kriterium F1
cc     ftx=up(1)
cc     F1=sigtr(1)-ftx*Oftx
c
cc     IF (F1.ge.eps) THEN
c *** Zugversagen (Kriterium F1)
cc       F(1)=F1

```

```

cc      nfail=nfail+1
C *** dF/dS (assoziiert)
cc          DF(1,1)=1.0d0
cc          DF(2,1)=0.0d0
cc          DF(3,1)=0.0d0
cc          DF(4,1)=0.0d0
cc          DF(5,1)=0.0d0
cc          DF(6,1)=0.0d0
C *** dF1/dKappa1
cc          FK(1)=ftx**2*h*Oftx/G(1)
C *** dkappa1/dLambda
cc          DK(1,1)=1.0d0
cc      ENDIF

C *** Abfrage Kriterium Fn
C     ...
cc     IF (Fn.ge.eps) THEN
C *** Versagen (Kriterium Fn
cc         F(n)=Fn
cc         nfail=nfail+1
C *** dF/dS
cc         DF(1,n)=...
cc         DF(2,n)=...
cc         DF(3,n)=...
cc         DF(4,n)=...
cc         DF(5,n)=...
cc         DF(6,n)=...
c *** z.B. nicht assoziierte Fliessregel
C *** dQ/dS
cc         DF(1,20)=...
cc         DF(2,20)=...
cc         DF(3,20)=...
cc         DF(4,20)=...
cc         DF(5,20)=...
cc         DF(6,20)=...

C *** dFn/dKappa
cc         FK(n)=...
C *** dkappa/dLambda
cc         DK(...,...)=...
cc      ENDIF

      RETURN
END

```

